## English

## Single correct answer type:

1. Out of the four alternatives, choose the one which expresses the right meaning of the given word.

Dubious
(A) Doubtful
(B) Disputable
(C) Duplicate
(D) Dangerous

Solution: (A)

Doubtful
2. Out of the four alternatives, choose the one which expresses the right meaning of the given word.
Flabbergasted
(A) Scared
(B) Embarrassed
(C) Dumbfounded
(D) Humiliated

Solution: (C)

Dumbfounded
3. Out of the four alternatives, choose the one which expresses the right meaning of the given word.
Eternal
(A) Innumerable
(B) Unmeasurable
(C) Prolonged
(D) Perpetual

Solution: (D)

## Perpetual

4. Choose the word opposite in meaning to the given word.

Despair
(A) Belief
(B) Trust
(C) Hope
(D) Faith

Solution: (C)

Hope
5. Choose the word opposite in meaning to the given word.

In toto
(A) Bluntly
(B) Partially
(C) Entirely
(D) Strongly

Solution: (B)
Partially
6. Choose the word opposite in meaning to the given word.

Protean
(A) Amateur
(B) Catholic
(C) Unchanging
(D) Rapid

Solution: (C)
Unchanging
7. A part of the sentence is underlined. Below are given alternatives to the improve the sentence.

Choose the correct alternative. In case no improvement is needed, your answer is ' d ' He declined all the allegations against him.
(A) spurned
(B) refused
(C) refuted
(D) no improvement

Solution: (D) no improvement
8. A part of the sentence is underlined. Below are given alternatives to the improve the sentence. Choose the correct alternative. In case no improvement is needed, your answer is ' $d$ '.
It is time we <u>leave.</u>
(A) left
(B) have to leave
(C) would leave
(D) no improvement

Solution: (A) left
9. A part of the sentence is underlined. Below are given alternatives to the improve the sentence. Choose the correct alternative. In case no improvement is needed, your answer is ' $d$ '.
We spent an hour discussing about his character.
(A) on his character
(B) of his character
(C) his character
(D) no improvement

Solution: (C)
his character
10. Sentences are given with blanks to be filled in with an appropriate and suitable word. Four alternatives are suggested for each question. Choose the correct alternative out of the four. Are your really desirous $\qquad$ visiting Japan?
(A) of
(B) in
(C) to
(D) about

Solution: (A)
of
11. Sentences are given with blanks to be filled in with an appropriate and suitable word. Four alternatives are suggested for each question. Choose the correct alternative out of the four. When Indians from the South move North, they find certain aspects of life quite $\qquad$ from their own.
(A) strange
(B) separate
(C) different
(D) divergent

Solution: (A)
strange
12. Sentences are given with blanks to be filled in with an appropriate and suitable word. Four alternatives are suggested for each question. Choose the correct alternative out of the four. The sky is overcast, we $\qquad$ The storm will soon burst.
(A) expect
(B) hope
(C) trust
(D) suspect

Solution: (D)

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suspect
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13. The first and the last parts of the sentence are numbered 1 to 6 . The rest of the sentence is spelt into four parts and named $P, Q, R$ and $S$. These four parts are not given in their proper order. Read the parts and find out which of the four combinations is correct. Then find the correct answer.
14. Early to bed, early to rise, makes a man healthy, wealthy and wise.
P. But for the morning tea, I had to wait for someone to get up before me.
Q. This saying inspired me to rise early.
R. That day I was the first to get up.
S. One day I got up early in the morning.
15. Then I realized that it was a waste of time to get up early and wait for the morning tea.
(A) QSRP
(B) QPRS
(C) PQRS
(D) SPQR

Solution: (A)
14. 1. A wood-cutter was cutting a tree on a river bank.
P. He knelt down and prayed.
Q. His axe slipped and fell into the water.
R. God Mercury appeared before him and asked about the matter.
S. He could not get it back as the river was very deep.
6. He dived into the water and came up with an axe of good.
(A) RPQS
(B) RPSQ
(C) QSRP
(D) QSPR

Solution: (D)
QSPR
15. 1. A dog stole a piece of meat from a butcher's shop.
P. He barked in anger.
Q. He ran to the jungle with the piece of meat.
R. He saw his reflection.
S. He crossed a river on the way.
6. He lost his piece of meat.
(A) QPSR
(B) QSRP
(C) QPRS
(D) SRPQ

Solution: (B)
QSRP
16. In a certain code MONKEY is XDJMNL. How is ‘TIGER’ written as?
(A) QDFHS
(B) SDFHS
(C) SHFDQ
(D) UJHFS

Solution: (A)


Similarly,

17. Find the missing number from the given responses.

(A) 31
(B) 229
(C) 234
(D) 312

Solution: (C)
$13 \times 17=221$
$12 \times 19=228$
Similarly, $13 \times 18=234$
18. If the day before yesterday was Thursday, when will Sunday be?
(A) tomorrow
(B) day after tomorrow
(C) today
(D) two days after today

Solution: (A)
If the day before yesterday was Thursday. Then, today will be Saturday and the Sunday will be tomorrow.
19. In a row of children Ravi is fourth from right and Shyam is second from left. When they interchange positions Ravi is ninth from right. What will be Shyam position from left?
(A) Fifth
(B) Sixth
(C) Seventh
(D) Eighth

Solution: (C)
When Ravi and Shyam interchange their position than Ravi's new position (ninth from right) is the same as Shyam's initial position (second from left)
$\therefore$ Total number of students in the row
$=8+1+1$
$=10$
So, Shyam's new position is same as Ravi's initial position (fourth from right) third from left. So, Shyam's new position from left $=10-3=7$ th
20.

(A)

(B)

(C)

(D)


Solution: (D)
Answer figure (d) will appear when a piece of paper folded and cut as shown in the question figure.
21. Which represents carrot, food, vegetable ?
(A)

(B)

(C)

(D)


Solution: (A)

22. "All the members of the Tennis club are members of the badminton club too". No woman plays badminton"?
(A) Some women play Tennis
(B) No member of the Tennis club plays badminton
(C) Some women are members of the Tennis club
(D) No woman is a member of Tennis club

Solution: (D)

23. Which number is wrong in the given series?
$1,9,25,50,81$
(A) 1
(B) 25
(C) 50
(D) 81

Solution: (C)
The pattern of series is


Hence, 50 is the wrong number.
24. In the following question and $\Delta$ stands for any of the Mathematical signs at different places, which are given as choices under each question. Select the choice with the correct sequence of signs which when substituted makes the question as correct equation?
$24 \Delta 4 \Delta 5 \Delta 4$
(A) $\mathrm{X}+=$
(B) $=X+$
(C) $+X=$
(D) $=+X$

Solution: (B)
Given equation, $24 \Delta 4 \Delta 5 \Delta 4$
From option $(=+X)$,
$24=4+5 \times 4$
$24=4+20$
$24=24$
25. Which answer figure is the exact mirror image of the given figure when the mirror is held from the right at PQ?


Solution: (C)
Answer figure (C) is correct mirror image of question figure.

## Mathematics

## Single correct answer type:

1. The equation of the base $B C$ of an equilateral $\triangle A B C$ is $x+y=2$ and $A$ is $(2,-1)$. The length of the side of the triangle is
(A) $\sqrt{2}$
(B) $\left(\frac{3}{2}\right)^{\frac{1}{2}}$
(C) $\left(\frac{1}{2}\right)^{\frac{1}{2}}$
(D) $\left(\frac{2}{3}\right)^{\frac{1}{2}}$

Solution: (D)
Length of perpendicular from $A(2,-1)$ to the line $x+y-2=0$ is

$\mathrm{AD}=\left|\frac{2-1-2}{\sqrt{1+1}}\right|=\frac{1}{\sqrt{2}}$
In $\triangle \mathrm{ABD}, \frac{\mathrm{AD}}{\mathrm{AB}}=\sin 60^{\circ}$
$\Rightarrow \frac{1}{\sqrt{2} \mathrm{AB}}=\frac{\sqrt{3}}{2}$
$\therefore \mathrm{AB}=\sqrt{\frac{2}{3}}$
2. The equation of the circle circumscribing the triangle formed by the lines $x+y=6,2 x+y=4$ and $x+2 y=5$ is
(A) $x^{2}+y^{2}+17 x+19 y-50=0$
(B) $x^{2}+y^{2}-17 x-19 y-50=0$
(C) $x^{2}+y^{2}+17 x-19 y-50=0$
(D) $x^{2}+y^{2}-17 x-19 y+50=0$

Solution: (D)
Lines, $x+y=6,2 x+y=4$ and $x+2 y=5$
Intersect at points $(-2,8),(7,-1)$ and $(1,2)$.
Now, all these points lie on
$x^{2}+y^{2}-17 x-19 y+50=0$
3. The length of the tangent from $(5,1)$ to the circle $x^{2}+y^{2}+6 x-4 y-3=0$ is
(A) 7
(B) 49
(C) 63
(D) 21

Solution: (A)
Required length of tangent is $\sqrt{\mathrm{S}_{1}}$, where
$\mathrm{S}_{1}=25+1+30-4-3=49$
$\therefore \sqrt{\mathrm{S}_{1}}=7$
4. If the length of the major axis of the ellipse $\left(\frac{x^{2}}{a^{2}}\right)+\left(\frac{y^{2}}{b^{2}}\right)=1$ is three times the length of minor axis, its eccentricity is
(A) $\frac{1}{3}$
(B) $\frac{1}{\sqrt{3}}$
(C) $\sqrt{\frac{2}{3}}$
(D) $\frac{2 \sqrt{2}}{3}$

Solution: (D)
Length of minor axis $=2 b$ and according to the given condition length of major axis $=3(2 b)=$ 6b
$\therefore \mathrm{e}=\sqrt{1-\frac{\mathrm{b}^{2}}{(3 \mathrm{~b})^{2}}}=\sqrt{\frac{8}{9}}=\frac{2 \sqrt{2}}{3}$
5. $S$ and $T$ are the foci of the ellipse $\left(\frac{x^{2}}{a^{2}}\right)+\left(\frac{y^{2}}{b^{2}}\right)=1$ and $B$ is an end of the minor axis. If STB is equilateral triangle, then eccentricity of the ellipse is
(A) $\frac{1}{4}$
(B) $\frac{1}{3}$
(C) $\frac{1}{2}$
(D) $\sqrt{\frac{3}{2}}$

Solution: (C)
$\ln \triangle$ BOT,
$\frac{\mathrm{b}}{\mathrm{ae}}=\tan 60^{\circ} \Rightarrow \mathrm{b}=\mathrm{ae} \sqrt{3}$

$\therefore e=\sqrt{1-\frac{b^{2}}{a^{2}}}=\sqrt{1-\frac{a^{2} e^{2} 3}{a^{2}}}$
$\Rightarrow e^{2}=1-3 e^{2} \Rightarrow 4 e^{2}=1 \Rightarrow \quad e= \pm \frac{1}{2}$
$\Rightarrow \quad \mathrm{e}=\frac{1}{2} \quad(\because \mathrm{e}$ cannot be negative)
6. The difference of the focal distance of any point on the hyperbola is equal to its
(A) latusrectum
(B) eccentricity
(C) length of the transverse axis
(D) half the length of the transverse axis

Solution: (C)
The difference of the focal distance at any point on the hyperbola is same as length of the transverse axis. i.e., $2 a$
7. If $\mathrm{A}+\mathrm{B}+\mathrm{C}=180^{\circ}$, then $\frac{\cot \mathrm{A}+\cot \mathrm{B}+\cot \mathrm{C}}{\cot \mathrm{A} \cot \mathrm{B} \cot \mathrm{C}}$ is equal to
(A) 1
(B) $\cot \mathrm{A} \cos \mathrm{B} \cot \mathrm{C}$
(C) -1
(D) 0

Solution: (A)

$$
\begin{aligned}
& \text { Since, } A+B+C=180^{\circ} \\
& \Rightarrow \cot (A+B+C) \\
& =\frac{\Sigma \cot A \cot B-1}{\cot A \cot B \cot C-\Sigma \cot A}=\frac{1}{0} \\
& \Rightarrow \cot A \cot B \cot C-\Sigma \cot A=0 \\
& \Rightarrow \frac{\cot A \cot B+\cot C}{\cot A \cot B \cot C}=1
\end{aligned}
$$

8. The angles of a triangle are in AP and the least angle is $30^{\circ}$. The greatest angle in radians is
(A) $\frac{7 \pi}{12}$
(B) $\frac{2 \pi}{3}$
(C) $\frac{5 \pi}{6}$
(D) $\frac{\pi}{2}$

Solution: (D)
Now, $30^{\circ}=30^{\circ} \times \frac{\pi}{180} \mathrm{rad}=\frac{\pi}{6}$
Let angle be $a, a+d, a+2 d$ area in AP
Now, $3 a+3 d=\pi \quad(\because A+B+C=\pi)$
$\Rightarrow 3 \times \frac{\pi}{6}+3 \mathrm{~d}=\pi$
$\Rightarrow \mathrm{d}=\frac{1}{3}\left(\pi-\frac{\pi}{2}\right)=\frac{\pi}{6}$
$\therefore$ Greatest angle $=\mathrm{a}+\mathrm{zd}$
$=\frac{\pi}{6}+2 \cdot \frac{\pi}{6}=\frac{\pi}{2}$
9. If $\tan 20^{\circ}=p$, then $\frac{\tan 160^{\circ}-\tan 110^{\circ}}{1+\tan 160^{\circ} \tan 110^{\circ}}$ is equal to
(A) $\left(\frac{1-p^{2}}{2 p}\right)$
(B) $\left(\frac{2 \mathrm{p}}{1+\mathrm{p}^{2}}\right)$
(C) $\left(\frac{1+\mathrm{p}}{2 \mathrm{p}}\right)$
(D) $\left(\frac{1-\mathrm{P}}{2 \mathrm{p}}\right)$

## Solution: (A)

Given that, $\tan 20^{\circ}=p$

$$
\begin{aligned}
& \therefore \frac{\tan 160^{\circ}-\tan 110^{\circ}}{1+\tan 160^{\circ} \tan 110^{\circ}} \\
& =\frac{\tan \left(180^{\circ}-20^{\circ}\right)-\tan \left(90^{\circ}+20^{\circ}\right)}{1+\tan \left(180^{\circ}-20^{\circ}\right) \tan \left(90^{\circ}+20^{\circ}\right)} \\
& =\frac{-\tan 20^{\circ}+\cot 20^{\circ}}{1+\tan 20^{\circ} \cot 20^{\circ}} \\
& =\frac{-\mathrm{p}+\frac{1}{\mathrm{p}}}{1+1}=\frac{1-\mathrm{p}^{2}}{2 \mathrm{p}}
\end{aligned}
$$

10. If $4 \sin ^{-1} x+\cos ^{-1} x=\pi$, then $x$ is equal to
(A) $\frac{1}{2}$
(B) 2
(C) 1
(D) $\frac{1}{3}$

Solution: (A)
Given, $4 \sin ^{-1} \mathrm{x}+\cos ^{-1} \mathrm{x}=\pi$

$$
\begin{aligned}
& \Rightarrow \frac{4 \sin ^{-1} x+\pi}{2}-\sin ^{-1} x=\pi \\
& \Rightarrow 3 \sin ^{-1} x=\frac{\pi}{2} \\
& \Rightarrow x=\sin \left(\frac{\pi}{6}\right)=\frac{1}{2}
\end{aligned}
$$

11. In a $\triangle \mathrm{ABC}, \mathrm{a}=2, \mathrm{~b}=3$ and $\sin \mathrm{A}=\frac{2}{3}$. Then, $\cos \mathrm{C}$ is equal to
(A) $\frac{1}{2}$
(B) $\frac{2}{3}$
(C) $\frac{2}{\sqrt{13}}$
(D) $\frac{1}{\sqrt{13}}$

Solution: (B)
$\mathrm{a}=2, \mathrm{~b}=3, \sin \mathrm{~A}=\frac{2}{3} \Rightarrow \sin ^{2} \mathrm{~A}=\frac{4}{9}$
$\therefore \cos ^{2} \mathrm{~A}=1-\sin ^{2} \mathrm{~A}=\frac{5}{9}$

$\Rightarrow \cos \mathrm{A}=\frac{\sqrt{5}}{3}$
By sine rule, $\frac{\sin A}{a}=\frac{\sin B}{b}$
$\Rightarrow \frac{2}{3} \times \frac{1}{2}=\frac{\sin B}{3}$
$\Rightarrow \sin B=1 \Rightarrow B=90^{\circ}$
In $\triangle A B C, \cos C=\frac{a}{b}=\frac{2}{3}$
12. The vector equation $\vec{r}=\hat{\imath}-2 \hat{\jmath}-\hat{k}+t(6 \hat{\jmath}-\hat{k})$ represents a straight line passing through the points
(A) $(0,6,-1)$ and $(1,-2,-1)$
(B) $(0,6,-1)$ and $(-1,-4,-2)$
(C) $(1,-2,-1)$ and $(1,4,-2)$
(D) $(1,-2,-1)$ and $(0,-6,1)$

Solution: (C)
Equation of the line passing through $a$ and $b$ is $a+t(b-a)$
Here, $\mathrm{b}-\mathrm{a}=6 \mathrm{j}-\mathrm{k}$
$\Rightarrow \mathrm{b}=6 \mathrm{j}-\mathrm{k}+\mathrm{i}-2 \mathrm{j}-\mathrm{k}$
$=\mathrm{i}+4 \mathrm{j}-2 \mathrm{k}$
$\therefore$ Given line passes through $(1,-2,-1)$ and $(1,4,-2)$
13. The work done by the force $4 \mathrm{i}-3 \mathrm{j}+2 \mathrm{k}$ in moving a particle along a straight line from the point $(3,2,-1)$ to $(2,-1,4)$ is
(A) 0 units
(B) 4 units
(C) 15 units
(D) 19 units

Solution: (C)
Work done $=($ Force displacement $)$
$=(4 \mathrm{i}-34 \mathrm{j}+2 \mathrm{k})-\{(2 \mathrm{i}-\mathrm{j}+4 \mathrm{k})-(3 \mathrm{i}+2 \mathrm{j}-\mathrm{k})\}$
$=(4 \mathrm{i}-3 \mathrm{j}+2 \mathrm{k})-(-\mathrm{i}-3 \mathrm{j}+5 \mathrm{k})$
$=(-4+9+10)=15$ units
14. $\lim _{\mathrm{x} \rightarrow 0}\left(\frac{(2+\mathrm{x}) \sin (2+\mathrm{x})-2 \sin 2}{\mathrm{x}}\right)$ is equal to
(A) $\sin 2$
(B) $\cos 2$
(C) 1
(D) $2 \cos 2+\sin 2$

Solution: (D)

$$
\begin{aligned}
& \lim _{x \rightarrow 0} \frac{(2+x) \sin (2+x)-2 \sin 2}{x} \quad\left(\frac{0}{0} \text { form }\right) \\
& =\lim _{x \rightarrow 0} \frac{\sin (2+x)+(2+x) \cos (2+x)}{1} \\
& =\sin 2+2 \cos 2
\end{aligned}
$$

15. If $f(x)=\frac{3 x+\tan ^{2} x}{x}$ is continuous at $x=0$, then $f(0)$ is equal to
(A) 3
(B) 2
(C) 4
(D) 0

Solution: (A)
Now, $\lim _{x \rightarrow 0} f(x)=\lim _{x \rightarrow 0} \frac{3 x+\tan ^{2} x}{x} \quad\left(\frac{0}{0}\right.$ form $)$
$=\lim _{x \rightarrow 0} \frac{3+2 \tan x \sec ^{2} x}{1}=3$
Since, $f(x)$ is continuous at $x=0$
$\therefore \mathrm{f}(0)=3$
16. If $x$ is measured in degree, then $\frac{d}{d x}(\cos x)$ is equal to
(A) $-\sin x$
(B) $-\frac{180}{\pi} \sin x$
(C) $-\frac{\pi}{180} \sin x$
(D) $\sin x$

Solution: (C)
$\frac{d}{d x}(\cos x)=-\frac{\pi}{180} \sin \pi$
17. $\left(\frac{d}{d x}\right)[\log (\sec x-\tan x)]$ is equal to
(A) $-\sec x$
(B) $\sec x+\tan x$
(C) $\sec x$
(D) $\sec x-\tan x$

Solution: (A)
$\frac{d}{d x}[\log (\sec x-\tan x)]$
$=\frac{1}{\sec x-\tan x}\left[\sec x \tan x-\sec ^{2} x\right]$
$=\frac{\sec x[\tan x-\sec x]}{\sec x-\tan x}=-\sec x$
18. If $x=\cos ^{2} \theta$ and $y=\sin ^{3} \theta$, then $1+\left(\frac{d y}{d x}\right)^{2}$ is equal to
(A) $\tan ^{2} \theta$
(B) $\cot ^{2} \theta$
(C) $\sec ^{2} \theta$
(D) $\operatorname{cosec}^{2} \theta$

Solution: (C)
Given, $x=\cos ^{3} \theta, y=\sin ^{3} \theta$
On differentiating w.r.t. $\theta$ respectively, we get
$\frac{d x}{d \theta}=-3 \cos ^{2} \theta \sin \theta$
And $\frac{\mathrm{dy}}{\mathrm{d} \theta}=3 \sin ^{2} \theta \cos \theta$
Now, $\frac{d y}{d x}=-\frac{3 \sin ^{2} \theta \cos \theta}{3 \cos ^{2} \theta \sin \theta}=-\tan \theta$
$\therefore 1+\left(\frac{d y}{d x}\right)^{2}=1+\tan ^{2} \theta=\sec ^{2} \theta$
19. If $x=a t^{2}, y=2 a t$, then $\frac{d^{2} y}{d x^{2}}$ is equal to
(A) $-\frac{1}{t^{2}}$
(B) $-\frac{1}{2 \mathrm{at}^{3}}$
(C) $\frac{1}{\mathrm{t}^{2}}$
(D) $-\frac{a}{2 t^{3}}$

Solution: (B)
$x=a t^{2}, y=2 a t$
On differentiating w.r.t. t, respectively
$\Rightarrow \frac{\mathrm{dx}}{\mathrm{dt}}=2 \mathrm{at}, \frac{\mathrm{dy}}{\mathrm{dt}}=2 \mathrm{a}$
$\therefore \frac{\mathrm{dy}}{\mathrm{dx}}=\frac{2 \mathrm{a}}{2 \mathrm{at}}=\frac{1}{\mathrm{t}}$
$\Rightarrow \frac{\mathrm{d}^{2} \mathrm{y}}{\mathrm{dx}^{2}}=-\frac{1}{\mathrm{t}^{2}} \frac{\mathrm{dt}}{\mathrm{dx}}$
$=-\frac{1}{\mathrm{t}^{2}} \cdot \frac{1}{2 \mathrm{at}}$
$=-\frac{1}{2 \mathrm{at}^{3}}$
20. If the rate of change in the circumference of a circle of $0.3 \mathrm{~cm} / \mathrm{s}$, then the rate of change in the area of the circle when the radius is 5 cm , is
(A) $1.5 \mathrm{sq} \mathrm{cm} / \mathrm{s}$
(B) $0.5 \mathrm{sq} \mathrm{cm} / \mathrm{s}$
(C) $5 \mathrm{sq} \mathrm{cm} / \mathrm{s}$
(D) $3 \mathrm{sq} \mathrm{cm} / \mathrm{s}$

Solution: (A)
Circumference of circle, $\mathrm{C}=2 \pi \mathrm{r}$
$\Rightarrow \frac{\mathrm{dC}}{\mathrm{dt}}=2 \pi \frac{\mathrm{dr}}{\mathrm{dt}}$
$\Rightarrow \frac{0.3}{2 \pi}=\frac{\mathrm{dr}}{\mathrm{dt}} \quad\left(\because \frac{\mathrm{dC}}{\mathrm{dt}}=0.3 \mathrm{~cm} / \mathrm{s}\right.$ given $)$
Now $A=\pi r^{2}$
$\frac{d \mathrm{~A}}{\mathrm{dt}}=2 \pi \mathrm{r} \frac{\mathrm{dr}}{\mathrm{dt}}$
$\Rightarrow \frac{\mathrm{dA}}{\mathrm{dt}}=\mathrm{r} \times 0.3$
$\Rightarrow\left[\frac{\mathrm{dA}}{\mathrm{dt}}\right]_{\mathrm{r}=5}=5 \times 0.3=1.5 \mathrm{sq} \mathrm{cm} / \mathrm{s}$
21. If $y=x^{3}-a x^{2}+48 x+7$ is an increasing function for all real values of $x$, then a lies in
(A) $(-14,14)$
(B) $(-12,12)$
(C) $(-16,16)$
(D) $(-21,21)$

Solution: (B)
$\frac{d y}{d x}=3 x^{2}-2 a x+48>0$
( $\because \mathrm{y}$ is an increasing function)
$\therefore$ Discriminant, $\mathrm{D}<0$
$\Rightarrow 4 \mathrm{a}^{2}-4 \times 3 \times 48<0$
$\Rightarrow \mathrm{a}^{2}-144<0$
$\Rightarrow \mathrm{a} \in(-12,12)$
22. Rolle's theorem is not applicable for the function $f(x)=|x|$ in the interval $[-1,1]$ because
(A) $f^{\prime}(1)$ does not exist
(B) $\mathrm{f}^{\prime}(-1)$ does not exist
(C) $\mathrm{f}(\mathrm{x})$ is discontinuous at $\mathrm{x}=0$
(D) $\mathrm{f}^{\prime}(0)$ does not exist

Solution: (D)
Rolle's theorem is not applicable for the function $\mathrm{f}(\mathrm{x})=|\mathrm{x}|$ inn $[-1,1]$
$\because f(0)$ does not exist.
23. $\int \frac{2 d x}{\left(e^{x}+e^{-x}\right)^{2}}$ is equal to
(A) $-\frac{\mathrm{e}^{-\mathrm{x}}}{\left(\mathrm{e}^{\mathrm{x}}+\mathrm{e}^{-x}\right)}+\mathrm{C}$
(B) $\frac{1}{\left(\mathrm{e}^{\mathrm{x}}+\mathrm{e}^{-x}\right)}+\mathrm{C}$
(C) $\frac{1}{\left(\mathrm{e}^{\mathrm{x}}+1\right)^{2}}+\mathrm{C}$
(D) $\frac{1}{\left(e^{x}-e^{-x}\right)^{2}}+C$

Solution: (A)
Let $\mathrm{I}=\int \frac{2 \mathrm{dx}}{\left(\mathrm{e}^{\mathrm{x}}+\mathrm{e}^{-\mathrm{x}}\right)^{2}}$
$=\int \frac{2 \mathrm{dx}}{\mathrm{e}^{2 \mathrm{x}}+\mathrm{e}^{-2 \mathrm{x}}+2}$
$=\int \frac{2 e^{2 x} d x}{e^{4 x}+2 e^{2 x}+1}$
Put $e^{2 x}=t \Rightarrow 2 e^{2 x} d x=d t$
$\therefore \quad \mathrm{I}=\int \frac{\mathrm{dt}}{\mathrm{t}^{2}+2 \mathrm{t}+1}=\int \frac{\mathrm{dt}}{(\mathrm{t}-1)^{2}}=-\frac{1}{\mathrm{t}+1}+\mathrm{C}$
$=-\frac{1}{e^{2 x}+1}=-\frac{e^{-x}}{e^{x}+e^{-x}}+C$
24. $\int_{0}^{\frac{\pi}{2}} \frac{\sin ^{\mathrm{n}} \theta}{\sin ^{\mathrm{n}} \theta+\cos ^{\mathrm{n}} \theta} \mathrm{d} \theta$ is equal to
(A) 1
(B) 0
(C) $\frac{\pi}{2}$
(D) $\frac{\pi}{4}$

Solution: (D)

Let $=\int_{0}^{\frac{\pi}{2}} \frac{\sin ^{n} \theta}{\sin ^{n} \theta+\cos ^{n} \theta} d \theta$
$=\int_{0}^{\frac{\pi}{2}} \frac{\sin ^{n}(\pi / 2-\theta)}{\sin ^{n}(\pi / 2-\theta)+\cos ^{n}(\pi / 2-\theta)} d \theta$
$=\int_{0}^{\frac{\pi}{2}} \frac{\cos ^{\mathrm{n}} \theta}{\cos ^{\mathrm{n}} \theta+\sin ^{\mathrm{n}} \theta} \mathrm{d} \theta$
On adding eqs. (i) and (ii) we get
$2 \mathrm{I}=\int_{0}^{\frac{\pi}{2}} \frac{\sin ^{\mathrm{n}} \theta+\cos ^{\mathrm{n}} \theta}{\cos ^{\mathrm{n}} \theta+\sin ^{\mathrm{n}} \theta} \mathrm{d} \theta$
$=\int_{0}^{\frac{\pi}{2}} \mathrm{~d} \theta=\frac{\pi}{2} \Rightarrow I=\frac{\pi}{4}$
25. $\int_{0}^{\pi} \cos ^{101} \mathrm{xdx}$ is equal to
(A) $\frac{\pi}{4}$
(B) $\frac{1}{102}$
(C) $\left(\frac{\pi}{3}\right)^{101}$
(D) 0

Solution: (D)

$$
\begin{aligned}
& \text { Let } I=\int_{0}^{\pi} \cos ^{101} x d x \\
& \Rightarrow \quad I=\int_{0}^{\pi}[\cos (\pi-x)]^{101} d x \\
& \Rightarrow \quad I \int_{0}^{\pi}-\cos ^{101} x d x \\
& \therefore \quad 2 I=\int_{0}^{\pi}\left(\cos ^{101} x-\cos ^{101} x\right) d x \\
& \Rightarrow \quad I=0
\end{aligned}
$$

26. $\lim _{n \rightarrow \infty}\left[\frac{1}{n+1}+\frac{1}{n+2}+\cdots+\frac{1}{6 n}\right]$
(A) $\log 2$
(B) $\log (1+\sqrt{5})$
(C) $\log 6$
(D) 0

Solution: (C)
$\lim _{n \times \infty}\left[\frac{1}{n+1}+\frac{1}{n+2}+\cdots+\frac{1}{6 n}\right]$
$\lim _{\mathrm{n} \times \infty} \sum_{\mathrm{r}=0}^{5 \mathrm{n}} \frac{1}{\mathrm{n}+\mathrm{r}}=\lim _{\mathrm{n} \times \infty}\left[\frac{1}{\mathrm{n}} \sum_{\mathrm{r}=0}^{5 \mathrm{n}} \frac{\mathrm{n}}{\mathrm{n}+\mathrm{r}}\right]$
$\lim _{\mathrm{n} \times \infty}\left[\frac{1}{\mathrm{n}} \sum_{\mathrm{r}=0}^{5 \mathrm{n}} \frac{1}{1+(\mathrm{r} / \mathrm{n})}\right]$
$=\int_{0}^{5} \frac{1}{1+x} d x=[\log (1+x)]_{0}^{5}$
$=\log 6-\log 1=\log 6$
27. By eliminating the arbitrary constant $A$ and $B$ from $y=A x^{2}+B x$, we get the differential equation
(A) $\frac{\mathrm{d}^{3} y}{\mathrm{dx}^{3}}=0$
(B) $x^{2} \frac{d^{2} y}{d x^{2}}-2 x \frac{d y}{d x}+2 y=0$
(C) $\frac{d^{2} y}{d^{2}}=0$
(D) $x^{2} \frac{d^{2} y}{d x^{2}}+y=0$

Solution: (B)
Given, $y=A x^{2}+B x$
On differentiating, we get
$\frac{d y}{d x}=2 A x+B$
$\Rightarrow \quad \frac{\mathrm{d}^{2} \mathrm{y}}{\mathrm{dx}^{2}}=2 \mathrm{~A}$
$\therefore \quad \frac{\mathrm{dy}}{\mathrm{dx}}-\frac{\mathrm{d}^{2} \mathrm{y}}{\mathrm{dx}^{2}} \mathrm{x}=\mathrm{B}$
From eq. (i), we get

$$
\begin{aligned}
& y=\frac{1}{2} \frac{d^{2} y}{d x^{2}} x^{2}+x\left[\frac{d y}{d x}-\frac{d^{2} y}{d x}-\frac{d^{2} y}{d x^{2}} x\right] \\
& \Rightarrow y=-\frac{1}{2} x^{2} \frac{d^{2} y}{d x^{2}}+x \frac{d y}{d x} \\
& \therefore \quad x^{2} \frac{d^{2} y}{d x^{2}}-2 x \frac{d y}{d x}+2 y=0
\end{aligned}
$$

28. If $f(x)=\frac{\log (1+a x)-\log (1-b x)}{x}$ for $x \neq 0$ and $f(0)=k$ and $f(x)$ is continuous at $x=0$, then $k$ is equal to
(A) $a+b$
(B) $a-b$
(C) a
(D) b

Solution: (A)
Given, $\mathrm{f}(\mathrm{x})=\frac{\log (1+\mathrm{ax})-\log (1-\mathrm{bx})}{\mathrm{x}}$
$f(x)$ is continuous at $x=k$ and $f(0)=k$
$\therefore \lim _{x \rightarrow 0} f(x)=\lim _{x \rightarrow 0} \frac{\log (1+a x)-\log (1-b x)}{x} \quad\left(\frac{0}{0}\right.$ form $)$
$=\lim _{x \rightarrow 0}\left(\frac{1}{1+a x} a+\frac{b}{1-b x}\right)$
$=\mathrm{a}+\mathrm{b}$
$\therefore \quad \mathrm{a}+\mathrm{b}=\mathrm{f}(0)=\mathrm{k}$
29. If $4-5 i$ is a root of the quadratic equation $x^{2}+a x+b=0$, then $(a, b)$ is equal to
(A) $(8,41)$
(B) $(-8,41)$
(C) $(41,8)$
(D) $(-41,8)$

Solution: (B)
If $4-5 i$ is root of $x^{2}+a x+b=0$, then $4+5 i$ is also the root.
$\therefore$ Sum of roots $=-a-8$
$\Rightarrow \quad \mathrm{a}=-8$

And product of roots $=16+25$
$=\mathrm{b}=41$
$\therefore \quad(\mathrm{a}, \mathrm{b})=(-8,41)$
30. If $\alpha$ and $\beta$ are the roots of the quadratic equation $4 x^{2}+3 x+7=0$, then the value of $\frac{1}{\alpha}+\frac{1}{\beta}$ is
(A) $-\frac{3}{4}$
(B) $-\frac{3}{7}$
(C) $\frac{3}{7}$
(D) $\frac{4}{7}$

Solution: (B)
Given equation can be rewritten as
$x^{2}+\frac{3}{4} x+\frac{7}{4}=0$
$\Rightarrow \alpha+\beta=-\frac{3}{4}, \alpha \beta=\frac{7}{4}$
Now, $\frac{1}{\alpha}+\frac{1}{\beta}=\frac{\alpha+\beta}{\alpha \beta}=-\frac{3}{7}$
31. If $\alpha, \beta$ are the roots of $\mathrm{ax}^{2}+\mathrm{bx}+\mathrm{c}=0$ and $\alpha+\mathrm{k}, \beta+\mathrm{k}$ are the roots of $\mathrm{px}{ }^{2}+\mathrm{qx}+\mathrm{r}=0$, then $\frac{b^{2}-4 a c}{q^{2}-4 p r}$ is equal to
(A) $\frac{\mathrm{a}}{\mathrm{p}}$
(B) 1
(C) $\left(\frac{a}{p}\right)^{2}$
(D) 0

Solution: (C)
Since, $\alpha, \beta$ are the roots of the equation
$a x^{2}+b x+c=0$
Then, $\left.\alpha=-\frac{b}{2 a}+\frac{\sqrt{b^{2}-4 a c}}{2 a}\right\}$
and $\left.\beta=-\frac{b}{2 a}-\frac{\sqrt{b^{2}-4 a c}}{2 a}\right\}$
And $\alpha+\mathrm{k}, \beta+\mathrm{k}$ are the roots of the equation $\mathrm{px}^{2}+\mathrm{qx}+\mathrm{r}=0$
Then, $\alpha+\mathrm{k}=-\frac{\mathrm{q}}{2 \mathrm{p}}+\frac{\sqrt{\mathrm{q}^{2}-4 \mathrm{pr}}}{2 \mathrm{p}}$
And $\beta+\mathrm{k}=-\frac{\mathrm{q}}{2 \mathrm{p}}-\frac{\sqrt{\mathrm{q}^{2}-4 \mathrm{pr}}}{2 \mathrm{p}}$
$\Rightarrow \quad \mathrm{k}=-\frac{\mathrm{q}}{2 \mathrm{p}}+\frac{\sqrt{\mathrm{q}^{2}-4 \mathrm{pr}}}{2 \mathrm{p}}+\frac{\mathrm{b}}{2 \mathrm{a}}-\frac{\sqrt{\mathrm{b}^{2}-4 \mathrm{ac}}}{2 \mathrm{a}} \quad$ [from eq. (i)]
$\Rightarrow \quad \frac{\sqrt{q^{2}-4 p r}}{2 p}-\frac{\sqrt{b^{2}-4 a c}}{2 a}$

$$
\begin{aligned}
& =\frac{-\sqrt{q^{2}-4 p r}}{2 p}+\frac{\sqrt{b^{2}-4 a c}}{2 a} \\
& \Rightarrow \quad \frac{\sqrt{q^{2}-4 p r}}{p}=\frac{\sqrt{b^{2}-4 a c}}{a} \\
& \Rightarrow \quad \frac{q^{2}-4 p r}{p^{2}}=\frac{b^{2}-4 a c}{a^{2}} \\
& \therefore \quad \frac{b^{2}-4 a c}{q^{2}-4 q r}=\left(\frac{a}{p}\right)^{2}
\end{aligned}
$$

32. Area of the triangle in the argand diagram formed by the complex number $z$, is $z+i z$, where $z=x+i y$ is
(A) $|z|$
(B) $|z|^{2}$
(C) $2|z|^{2}$
(D) $\frac{1}{2}|z|^{2}$

Solution: (D)
Since, $\mathrm{iz}=\mathrm{ze}^{\mathrm{i} \pi / 2}$
This implies that iz is the vector obtained by rotating vector $z$ in anti-clockwise direction through $90^{\circ}$.

$\therefore \mathrm{OA} \perp \mathrm{AB}$
So, area of $\triangle \mathrm{OAB}=\frac{1}{2} \mathrm{OA} \times O B$
$=\frac{1}{2}|z||i z|=\frac{1}{2}|z|^{2}$
33. The sum of $n$ terms of the series $\frac{1}{2}+\frac{3}{4}+\frac{7}{8}+\frac{15}{16}+\cdots$ is
(A) $n-1+2^{-n}$
(B) 1
(C) $n-1$
(D) $1+2^{-n}$

Solution: (A)
Let $S_{n}$ be the sum of first n terms of the series.
$\therefore S_{n}=\frac{1}{2}+\frac{3}{4}+\frac{7}{8}+\frac{15}{16}+\cdots$
$\Rightarrow S_{n}=\left(1-\frac{1}{2}\right)+\left(1-\frac{1}{4}\right)+\left(1-\frac{1}{8}\right)+\cdots$
$S_{n}=n-\frac{1}{2} \frac{(1-1 / 2)}{2(1-1 / 2)}=n-1+\frac{1}{2^{n}}$
$\Rightarrow=n-1+2^{-n}$
34. $0.2+0.22+0.222+\cdots$ to n terms is equal to
(A) $\left(\frac{2}{9}\right)-\left(\frac{2}{81}\right)\left(1-10^{-n}\right)$
(B) $n-\left(\frac{1}{9}\right)\left(1-10^{-n}\right)$
(C) $\left(\frac{2}{9}\right)\left[n-\left(\frac{1}{9}\right)\left(1-10^{-n}\right)\right]$
(D) $\left(\frac{2}{9}\right)$

Solution: (C)
$0.2+0.22+0.222+\cdots n$ terms
$=2(0.1+0.11+0.111+\cdots n$ terms $)$
$=2\left(\frac{1}{10}+\frac{11}{100}+\frac{111}{100}+\cdots n\right.$ terms $)$
$=\frac{2}{9}\left(\frac{9}{10}+\frac{99}{100}+\frac{999}{1000}+\cdots n\right.$ terms $)$
$=\frac{2}{9}\left(1-\frac{1}{10}+1-\frac{1}{100}+1-\frac{1}{1000}+\cdots n\right.$ terms $)$
$=\frac{2}{9}\left[n-\left(\frac{1}{10}+\frac{1}{100}+\frac{1}{1000}+\cdots n\right)\right]$
$=\frac{2}{9}\left[n-\frac{1}{10} \frac{\left\{1-\left(\frac{1}{10}\right)^{n}\right\}}{\left(1-\frac{1}{10}\right)}\right]$
$=\frac{2}{9}\left[n-\frac{1}{10} \times \frac{10}{9} \cdot\left(\frac{10^{n}-1}{10^{n}}\right)\right]$
$=\frac{2}{9}\left[n-\frac{1}{9}\left(1-10^{-n}\right)\right]$
35. The number of ways in which a term of 11 players can be selected from 22 players including 2 of them and excluding 4 of them is
(A) ${ }^{16} C_{11}$
(B) ${ }^{16} C_{5}$
(C) ${ }^{16} C_{9}$
(D) ${ }^{20} C_{8}$

Solution: (C)
Number of required ways
$={ }^{22-4-2} C_{11-2}={ }^{16} C_{9}$
36. The number of ways four boys can be seated around a round table in four chairs of different colours is
(A) 24
(B) 12
(C) 23
(D) 64

Solution: (A)
$\therefore$ Required number of ways
$=4!=24$
37. If the coefficient of second, third and fourth terms in the expansion of $(1+x)^{n}$ are in $A P$, then $n$ is equal to
(A) 7
(B) 4
(C) 5
(D) 6

Solution: (A)
Since, $T_{2}={ }^{n} C_{1}$
And $T_{3}={ }^{n} C_{2} x, T_{4}={ }^{n} C_{3} x$
Also, $T_{2}, T_{3}, T_{4}$ are in AP.

$$
\begin{aligned}
& \Rightarrow \quad \frac{{ }^{n} C_{1}+{ }^{n} C_{3}}{2}={ }^{n} C_{2} \\
& { }^{n} C_{1}+{ }^{n} C_{3}=2 \cdot{ }^{n} C_{2} \\
& \Rightarrow \quad \frac{n!}{(n-1)!(1)!}+\frac{n!}{(n-3)!3!}=\frac{2 n!}{2!(n-2)!} \\
& \Rightarrow \quad \frac{1}{(n-1)(n-2)}+\frac{1}{31}=\frac{1}{(n-2)} \\
& \Rightarrow \quad 1+\frac{(n-1)(n-2)}{6}=(n-1) \\
& \Rightarrow \quad 6+n^{2}-3 n+2=6 n-6 \\
& \Rightarrow \quad n^{2}-3 n-6 n+8+6=0 \\
& \Rightarrow \quad n^{2}-9 n+14=0 \\
& \Rightarrow \quad(n-7)(n-2)=0 \\
& \Rightarrow \quad n=7 \text { or } 2 \quad \\
& \therefore n=7 \quad(\because n \neq 2)
\end{aligned}
$$

38. If $\Delta=\left|\begin{array}{lll}1 & a & a^{2} \\ 1 & b & b^{2} \\ 1 & c & c^{2}\end{array}\right|=k(a-b)(b-c)(c-a)$, then k is equal to
(A) -2
(B) 1
(C) 2
(D) $a b c$

Solution: (B)

$$
\begin{aligned}
& \left.\Delta=\left|\begin{array}{lll}
1 & a & a^{2} \\
1 & b & b^{2} \\
1 & c & c^{2}
\end{array}\right|=\left|\begin{array}{ccc}
1 & a & a^{2} \\
0 & b-a & b^{2}-a^{2} \\
0 & c-a & c^{2}-a^{2}
\end{array}\right| \quad \text { (using } R_{2} \rightarrow R_{2}-R_{1} \text { and } R_{3} \rightarrow R_{3}-R_{1}\right) \\
& =(b-a)(c-a)\left|\begin{array}{ccc}
1 & a & a^{2} \\
0 & 1 & b+a \\
0 & 1 & c+a
\end{array}\right| \\
& =(b-a)(c-a)(c+a-b-a) \\
& \Rightarrow \quad(b-a)(c-a)(c-b) \\
& =k(a-b)(b-c)(c-a) \quad \text { (given) } \\
& \Rightarrow \quad k=1
\end{aligned}
$$

39. $\left|\begin{array}{ccc}a+b & a & b \\ a & a+c & c \\ b & c & b+c\end{array}\right|$ is equal to
(A) $4 a b c$
(B) $a b c$
(C) $a^{2} b^{2} c^{2}$
(D) $4 a^{2} b c$

Solution: (A)

$$
\begin{aligned}
& \left|\begin{array}{ccc}
a+b & a & b \\
a & a+c & c \\
b & c & b+c
\end{array}\right|=\left|\begin{array}{ccc}
b & -c & b-c \\
a & a+c & c \\
b & c & b+c
\end{array}\right| \quad\left(\text { by } R_{1} \rightarrow R_{1}-R_{2}\right) \\
& =\left|\begin{array}{ccc}
2 b & 0 & 2 b \\
a & a+c & c \\
2 b & 0 & 0
\end{array}\right| \quad\left(\text { by } R_{1} \rightarrow R_{1}+R_{2}\right)
\end{aligned}
$$

$$
=\left|\begin{array}{ccc}
2 b & 0 & 0 \\
a & a+c & c-a \\
b & c & c
\end{array}\right|\left(\text { by } C_{3} \rightarrow C_{3}-C_{1}\right)
$$

$$
=2 b\left(a c+c^{2}-c^{2}+a c\right)=4 a b c
$$

40. If $\Delta_{1}=\left|\begin{array}{lll}x & a & b \\ b & x & a \\ a & b & x\end{array}\right|$ and $\Delta_{2}=\left|\begin{array}{ll}x & b \\ a & x\end{array}\right|$ are the given determinants, then
(A) $\Delta_{1}=3\left(\Delta_{2}\right)^{2}$
(B) $\left(\frac{d}{d x}\right)\left(\Delta_{1}\right)=3 \Delta_{2}$
(C) $\left(\frac{d}{d x}\right)\left(\Delta_{1}\right)=3\left(\Delta_{2}\right)^{2}$
(D) $\Delta_{1}=3\left(\Delta_{2}\right)^{\frac{3}{2}}$

Solution: (B)
Given, $\Delta=\left|\begin{array}{lll}x & a & b \\ b & x & a \\ a & b & x\end{array}\right|, \quad \Delta_{2}=\left|\begin{array}{ll}x & b \\ a & x\end{array}\right|$
$\therefore \quad \frac{d}{d x}\left(\Delta_{1}\right)$
$=\left|\begin{array}{lll}1 & 0 & 0 \\ b & x & a \\ a & b & x\end{array}\right|+\left|\begin{array}{lll}x & a & b \\ 0 & 1 & 0 \\ a & b & x\end{array}\right|+\left|\begin{array}{ccc}x & a & b \\ b & x & a \\ 0 & 0 & 1\end{array}\right|$
$=\left|\begin{array}{ll}x & a \\ b & x\end{array}\right|+\left|\begin{array}{ll}x & b \\ a & x\end{array}\right|+\left|\begin{array}{ll}x & a \\ b & x\end{array}\right|=3 \Delta_{2}$
$\therefore \quad \frac{d}{d x}\left(\Delta_{1}\right)=3 \Delta_{2}$
41. The system $x+4 y-2 z=3,3 x+y+5 z=7$ and $2 x+3 y+z=5$ has
(A) infinite number of solutions
(B) unique solution
(C) trivial solution
(D) no solution

Solution: (D)
Given system equations are
$x+4 y-2 z=3$
$3 x+y+5 a=7$
And $2 x+3 y+z=5$
$\therefore \quad \Delta=\left|\begin{array}{ccc}1 & 4 & -2 \\ 3 & 1 & 5 \\ 2 & 3 & 1\end{array}\right|$
$=1(1-15)-4(3-10)-2(9-2)$
$=-14+28-14=0$
And $\Delta_{2}=\left|\begin{array}{ccc}1 & 3 & -2 \\ 3 & 7 & 5 \\ 2 & 5 & 1\end{array}\right|=1 \neq 0$
$\therefore$ No solution will exis.
42. If the three points $(k, 2 k),(2 k, 3 k),(3,1)$ are collinear, then k is equal to
(A) -2
(B) 1
(C) $\frac{1}{2}$
(D) $-\frac{1}{2}$

Solution: (A)
Area of triangle $=\frac{1}{2}\left|\begin{array}{ccc}k & 2 k & 1 \\ 2 k & 3 k & 1 \\ 3 & 1 & 1\end{array}\right|=0$
(using $R_{2} \rightarrow R_{2}-R_{1}$ and $R_{3} \rightarrow R_{3}-R_{1}$ )

$$
\begin{aligned}
& \Rightarrow \quad\left|\begin{array}{ccc}
\mathrm{k} & 2 \mathrm{k} & 1 \\
\mathrm{k} & \mathrm{k} & 0 \\
3-\mathrm{k} & 1-2 \mathrm{k} & 0
\end{array}\right|=0 \\
& \Rightarrow \quad 1[\mathrm{k}(1-2 \mathrm{k})-\mathrm{k}(3-\mathrm{k})]=0 \\
& \Rightarrow \quad \mathrm{k}-2 \mathrm{k}^{2}-3 \mathrm{k}+\mathrm{k}^{2}=0 \\
& \Rightarrow \quad-\mathrm{k}^{2}-2 \mathrm{k}=0 \\
& \Rightarrow \quad-\mathrm{k}(\mathrm{k}+2)=0 \quad \Rightarrow \quad \mathrm{k}=0,-2
\end{aligned}
$$

43. The foot of the perpendicular from the point $(3,4)$ on the line $3 x-4 y+5=0$ is
(A) $\left(\frac{81}{25}, \frac{92}{25}\right)$
(B) $\left(\frac{92}{25}, \frac{81}{25}\right)$
(C) $\left(\frac{46}{26}, \frac{54}{24}\right)$
(D) $\left(-\frac{81}{25},-\frac{92}{25}\right)$

Solution: (A)
Let M be the foot of perpendicular from $\mathrm{P}(3,4)$ on the line $3 x-4 y+5=0$. Then, M is the point of intersection $3 x-4 y+5=0$ and line passing through $P(3,4)$ and perpendicular to
$3 x-4 y+5=0$
Equation of the line perpendicular to
$3 x-4 y+5=0$ is $4 x+3 y+\lambda=0$
This passes through $(3,4)$
$\Rightarrow 12+12+\lambda$
$\Rightarrow \lambda=-24$
$\therefore$ Equation is $4 x+3 y-24=0$
On solving equations (i) and (ii), we get
$y=92 / 25$
$x=81 / 25$
$\therefore$ Required point is $\left(\frac{81}{25}, \frac{92}{25}\right)$.
44. A kite is flying at an inclination of $60^{\circ}$ with the horizontal. If the length of the thread is 120 m , then the height of the kite is
(A) $60 \sqrt{3} \mathrm{~m}$
(B) 60 m
(C) $\frac{60}{\sqrt{3}} \mathrm{~m}$
(D) 120 m

Solution: (A)
In $\triangle \mathrm{ABC}, \sin 60^{\circ}=\frac{\mathrm{h}}{120}$

$\Rightarrow \mathrm{h}=120 \times \frac{\sqrt{3}}{2}$
$\therefore \mathrm{h}=60 \sqrt{3} \mathrm{~m}$
45. If the focus of parabola is at $(0,-3)$ and its directrix is $y=3$, then its equation is
(A) $x^{2}=-12 y$
(B) $x^{2}=12 y$
(C) $\mathrm{y}^{2}=-12 \mathrm{y}$
(D) $y^{2}=12 x$

Solution: (A)
Let $\mathrm{P}(\mathrm{x}, \mathrm{y})$ be any point on the parabola. Then, by definition
$\sqrt{(x-0)^{2}+(y+3)^{2}}=(y-3)$
$\Rightarrow \quad x^{2}+(y+3)^{2}=(y-3)^{2}$
$\Rightarrow \quad x^{2}+y^{2}+6 y+9=y^{2}-6 y+9$
$\Rightarrow \quad x^{2}=-12 y$

## Chemistry

Single correct answer type:

1. The ionic conductance of $\mathrm{Ba}^{2+}$ and $\mathrm{Cl}^{-}$are respectively 127 and $76 \Omega^{-1} \mathrm{~cm}^{2}$ at infinite dilution. The equivalent conductance (in $\Omega^{-1} \mathrm{~cm}^{2}$ ) of $\mathrm{BaCl}_{2}$ at infinite dilution will be
(A) 330
(B) 203
(C) 139.5
(D) 51

Solution: (C)
$\Lambda_{\mathrm{m}}^{\infty}$ for $\mathrm{BaCl}_{2}=\Lambda_{\mathrm{m}}^{\infty} \mathrm{Ba}^{2+}+2 \Lambda_{\mathrm{m}}^{\infty} \mathrm{Cl}^{-}$
$\therefore \Lambda_{\mathrm{eq}}^{\infty}$ for $\mathrm{BaCl}_{2}=\frac{1}{2} \Lambda_{\mathrm{m}}^{\infty} \mathrm{Ba}^{2+}+\Lambda_{\mathrm{m}}^{\infty} \mathrm{Cl}^{-}$
$=\frac{1}{2} \times 127+76$
$=139.5 \Omega^{-1} \mathrm{~cm}^{2}$
2. If the elevation in boiling point of a solution of 10 g of solute (mol. $\mathrm{wt} .=100$ ) in 100 g of water is $\Delta T_{b}$, the ebullioscopic constant of water is
(A) $\frac{\Delta \mathrm{T}_{\mathrm{b}}}{10}$
(B) $\Delta \mathrm{T}_{\mathrm{b}}$
(C) $10 \Delta \mathrm{~T}_{\mathrm{b}}$
(D) $100 \Delta \mathrm{~T}_{\mathrm{b}}$

Solution: (B)
$\mathrm{m}=\frac{1000 \times \mathrm{K}_{\mathrm{b}} \times \mathrm{w}}{\mathrm{w} \times \Delta \mathrm{T}_{\mathrm{b}}}$
Or $\mathrm{K}_{\mathrm{b}}=\frac{\mathrm{m} \times \mathrm{W} \times \Delta \mathrm{T}_{\mathrm{b}}}{1000 \times 10}$
$=\Delta \mathrm{T}_{\mathrm{b}}$
3. Given that;
$\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightarrow \mathrm{H}^{+}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq}) ; \Delta \mathrm{H}=57.32 \mathrm{~kJ}$
$\mathrm{H}_{2}(\mathrm{~g})+\frac{1}{2} \mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{H}_{2} \mathrm{O}(\mathrm{l}) ; \Delta \mathrm{H}=-286.02 \mathrm{~kJ}$
Then calculate the enthalpy of formation of $\mathrm{OH}^{-}$at $25^{\circ} \mathrm{C}$.
(A) -22.8 kJ
(B) -343.52 kJ
(C) +228.8 kJ
(D) +343.52 kJ

Solution: (A)

Consider the formation of $\mathrm{H}_{2} \mathrm{O}$
$\mathrm{H}_{2}(\mathrm{~g})+\frac{1}{2} \mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{H}_{2} \mathrm{I}(\mathrm{l}) ; \Delta \mathrm{H}=-286.20 \mathrm{~kJ}$
$\Delta \mathrm{Hr}=\Delta \mathrm{H}_{\mathrm{f}}\left(\mathrm{H}_{2} \mathrm{O}(\mathrm{l})\right)-\Delta \mathrm{H}_{\mathrm{f}}\left(\mathrm{H}_{2}(\mathrm{~g})\right)-\frac{1}{2} \Delta \mathrm{H}_{\mathrm{f}}\left(\mathrm{O}_{2}(\mathrm{~g})\right)$
$-286.20=\Delta \mathrm{H}_{\mathrm{f}}\left(\mathrm{H}_{2} \mathrm{O}(\mathrm{l})\right)-0-0$
$\therefore \Delta \mathrm{H}_{\mathrm{f}}\left(\mathrm{H}_{2} \mathrm{O}(\mathrm{l})=-286.20\right.$

Now consider the ionization of $\mathrm{H}_{2} \mathrm{O}$
$\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightarrow \mathrm{H}^{+}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq}) ; \Delta \mathrm{H}=57.32 \mathrm{~kJ}$
$\Delta \mathrm{H}_{\mathrm{r}}-\Delta \mathrm{H}_{\mathrm{f}}\left(\mathrm{H}^{+}(\mathrm{aq})+\Delta \mathrm{H}_{\mathrm{f}}\left(\mathrm{OH}^{-}(\mathrm{aq})\right)-\Delta \mathrm{H}_{\mathrm{f}}\left(\mathrm{H}_{2} \mathrm{O}(\mathrm{l})\right)\right.$
$57.32=0+\Delta \mathrm{H}_{\mathrm{f}}\left(\mathrm{OH}_{\mathrm{aq}}^{-}\right)-(-286.20)$
Or $\Delta \mathrm{H}_{\mathrm{f}}\left(\mathrm{OH}^{-} \mathrm{aq}\right)=57.32-286.20$
$=-228.88 \mathrm{~kJ}$
4. Calculate the amount of heat evolved when $500 \mathrm{~cm}^{3}$ of 0.1 M HCl is mixed with $200 \mathrm{~cm}^{3}$ of 0.2 M NaOH .
(A) 57.3 kJ
(B) 2.865 kJ
(C) 2.292 kJ
(D) 0.573 kJ

Solution: (C)
$\mathrm{HCl}+\mathrm{NaOH} \rightarrow \mathrm{NaCl}+\mathrm{H}_{2} \mathrm{O}$
At $t=0$,

Number of moles

$$
\begin{array}{cc}
=\frac{500 \times 0.1}{1000} & \frac{200 \times 0.2}{1000} \\
=0.05 & =0.04
\end{array}
$$

$\because$ During neutralisation of 1 mole of NaOH by 1 mole of HCl , heat evolved $=57.3 \mathrm{~kJ}$
$\therefore$ To neutralized 0.04 , moles of NaOH by 0.04 mole of NaOH , heat evolved
$=57.3 \times 0.4$
$=2.292 \mathrm{~kJ}$
5. Which of the following will be the most effective in the coagulation of $\mathrm{Fe}(\mathrm{OH})_{3}$ sol?
(A) $\mathrm{Mg}_{3}\left(\mathrm{PO}_{4}\right)_{2}$
(B) $\mathrm{BaCl}_{2}$
(C) NaCl
(D) KCN

Solution: (A)
According to Hardy-Schulze rule, coagulation power of ions is directly proportional to charge onion.
$\because \mathrm{Fe}(\mathrm{OH})_{3}$ is positively charged colloid.
$\therefore$ It will be coagulated by anion.
(a) $\mathrm{Mg}_{3}\left(\mathrm{PO}_{4}\right)_{2} \rightleftharpoons 3 \mathrm{Mg}^{2}++2 \mathrm{PO}_{4}^{3-}$
(b) $\mathrm{BaCl}_{2} \rightleftharpoons \mathrm{Ba}^{2+}+2 \mathrm{Cl}^{-}$
(c) $\mathrm{NaCl} \rightleftharpoons \mathrm{Na}^{+}+\mathrm{Cl}^{-}$
(d) $\mathrm{KCN} \rightleftharpoons \mathrm{K}^{+}+\mathrm{CN}^{-}$
$\because \mathrm{PO}_{4}^{3-}$ has highest charge among the given anions.
$\therefore \mathrm{Mg}\left(\mathrm{PO}_{4}\right)_{2}$ is the most effective in coagulation of $\mathrm{Fe}(\mathrm{OH})_{3}$ sol.
6. Identify ' $C$ ' in the following reaction;

(A) benzamide
(B) benzoic acid
(C) chlorobenzene
(D) aniline

Solution: (D)

7. The following reaction is known as

(A) Friedel-Craft reaction
(B) Kolbe reaction
(C) Reamer-Tiemann reaction
(D) Wittig reaction

Solution: (B)
At $120-140^{\circ} \mathrm{C}$ temperature and 1.5 atm pressure, sodium phenoxide reacts with $\mathrm{CO}_{2}$ to yield sodium salicylate which on further hydrolysis gives salicylic acid.
8. Which of the following is isoelectronic of carbon?
(A) $\mathrm{Na}^{+}$
(B) $\mathrm{Al}^{3+}$
(C) $\mathrm{O}^{2-}$
(D) $\mathrm{N}^{+}$

Solution: (D)
Number of electrons in $\mathrm{C}=6$
Number of electrons in $\mathrm{Al}^{3+}=13-3=10$
Number of electrons in $\mathrm{O}^{2-}=8+2=10$
Number of electrons in $\mathrm{N}^{+}=7-1=6$
$\therefore \mathrm{N}^{+}$iso-electronic with C .
9. In which of the following species only one type of hybridization is present?
(A) $\mathrm{CH}_{3}-\mathrm{CH}_{2}-\mathrm{CH}=\mathrm{CH}_{2}$
(B)

$$
\mathrm{CH}_{3}-\mathrm{CH}=\mathrm{CH}-\stackrel{+}{\mathrm{CH}_{2}}
$$

(C) $\mathrm{CH}_{2}=\mathrm{CH}-\mathrm{CH}=\mathrm{CH}_{2}$
(D) $\mathrm{CH}_{3}-\mathrm{CH}=\mathrm{CH}-\mathrm{CH}_{2}^{-}$

Solution: (C)
(a) $\mathrm{sp}^{3} \mathrm{CH}_{3}-\underset{\mathrm{sp}^{3}}{\mathrm{CH}_{2}}-\underset{\mathrm{sp}^{2}}{\mathrm{CH}_{2}}=\underset{\mathrm{sp}^{2}}{\mathrm{CH}_{2}}$
(b) $\underset{\mathrm{sp}^{3}}{\mathrm{CH}_{3}}-\underset{\mathrm{sp}^{2}}{\mathrm{CH}}=\underset{\mathrm{sp}^{2}}{\mathrm{CH}}-\underset{\mathrm{sp}^{2}}{\mathrm{CH}_{2}^{+}}$
(c) $\underset{\mathrm{sp}^{2}}{\mathrm{CH}_{2}}=\underset{\mathrm{sp}^{2}}{\mathrm{CH}}-\underset{\mathrm{sp}^{2}}{\mathrm{CH}}=\underset{\mathrm{sp}^{2}}{\mathrm{CH}_{2}}$
(d)

$$
\underset{\mathrm{sp}^{3}}{\mathrm{CH}_{3}}-\underset{\mathrm{sp}^{2}}{\mathrm{CH}}=\underset{\mathrm{sp}^{2}}{\mathrm{CH}}-\underset{\mathrm{sp}^{3}}{\mathrm{CH}_{2}^{-}}
$$

10. $2 \mathrm{MnO}_{4}^{-}+5 \mathrm{H}_{2} \mathrm{O}+6 \mathrm{H}^{6} \rightarrow 2 \mathrm{Z}+5 \mathrm{O}_{2}+8 \mathrm{H}_{2} \mathrm{O}$

Identify Z in the above reaction
(A) $\mathrm{Mn}^{2+}$
(B) $\mathrm{Mn}^{4+}$
(C) Mn
(D) $\mathrm{MnO}_{2}$

Solution: (A)
$2 \mathrm{MnO}_{4}^{-}+5 \mathrm{H}_{2} \mathrm{O}_{2}+6 \mathrm{H}^{+} \rightarrow 2 \mathrm{Mn}^{2+}+5 \mathrm{O}_{2}+8 \mathrm{H}_{2} \mathrm{O}$
11. In the titration of NaOH and HCl , which of the following indicator will be used?
(A) Methyl orange
(B) Methyl red
(C) Both (methyl orange) and (methyl red)
(D) None of (methyl orange) and (methyl red)

Solution: (C)

In the titration of strong base with strong acid, we can use methyl orange, methyl red, phenolphthalein as indicator.
12. Which of the following is correct IUPAC name for $\mathrm{K}_{2}\left[\mathrm{Cr}(\mathrm{CN})_{2} \mathrm{O}_{2}(\mathrm{O})_{2} \mathrm{NH}_{3}\right]$ ?
(A) Potassium amminecyanoperoxodioxochromatic (IV)
(B) Potassium amminecyanoperoxodioxochromium (V)
(C) Potassium amminecyanoperoxodioxochromium (VI)
(D) Potassium amminedicyanodioxoper oxochromate (VI)

Solution: (D)
The IUPAC name of $\mathrm{K}_{2}\left[\mathrm{Cr}(\mathrm{CN})_{2} \mathrm{O}_{2} \mathrm{NH}_{3}\right]$ is potassium amminedicyanodioxoperoxochromate (VI).
13. Which of the following is process used for the preparation of acetone?
(A) Waber process
(B) Wacker process
(C) Wolf-Kishner reduction
(D) Gattermann-Koch synthesis

Solution: (B)

In Wacker process, when mixture of propane and air is passed through mixture of Pd and $\mathrm{CuCl}_{2}$ at high pressure, acetone is formed.
$\mathrm{Pd}+\mathrm{CuCL}_{2} \rightarrow \mathrm{PdCl}_{2}+2 \mathrm{CuCl}$
$4 \mathrm{CuCl}+\mathrm{HCl}+\mathrm{O}_{2} \rightarrow \longrightarrow 4 \mathrm{CuCl}_{2}+2 \mathrm{H}_{2} \mathrm{O}$
$\mathrm{CH}_{3} \mathrm{CH}=\mathrm{CH}_{2}+\mathrm{PdCl}_{2}+\mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{C} \longrightarrow \mathrm{H}_{3} \mathrm{COCH}_{3}+\mathrm{Pd}+2 \mathrm{HCl}$
propene
14. Lindane can be obtained by the reaction of benzene with
(A) $\mathrm{CH}_{2} \mathrm{Cl} /$ anhydrous $\mathrm{AlCl}_{3}$
(B) $\mathrm{C}_{2} \mathrm{H}_{4} \mathrm{I} /$ anhydrous $\mathrm{AlCl}_{3}$
(C) $\mathrm{CH}_{3} \mathrm{COCl} /$ anhydrous $\mathrm{AlCl}_{3}$
(D) $\mathrm{Cl}_{2}$ in sunlight

Solution: (D)
Lindane is $\gamma$-benzene hexachloride. It can be prepared by benzene with $\mathrm{Cl}_{2}$ in sunlight.

15. The structure of cis-bis (propenyl) ethane is
(A)

(B)

(C)

(D)


Solution: (B)
The two propenyl groups attached to 1,2 position of carbon in cis-form.

16. 5 moles of $\mathrm{Ba}(\mathrm{OH})_{2}$ are treated with excess of $\mathrm{CO}_{2}$. How much $\mathrm{BaCO}_{3}$ will be formed?
(A) 39.4 g
(B) 197 g
(C) 591 g
(D) 985 g

Solution: (D)

```
\(\mathrm{Ba}(\mathrm{OH})_{2}+\mathrm{CO}_{2} \rightarrow \mathrm{BaCO}_{3}+\mathrm{H}_{2} \mathrm{O}\)
\(\because\) moles of \(\mathrm{Ba}(\mathrm{OH})_{3}=5\) moles of \(\mathrm{BaCO}_{3}\)
\(\therefore\) Mass of \(\mathrm{BaCO}_{3}=\) moles of \(\mathrm{BaCO}_{3} \times\) molecules mass of \(\mathrm{BaCO}_{3}\)
\(=5 \times 197\)
\(=985 \mathrm{~g}\)
```

17. A diatomic molecule has a dipole moment of 1.2 D . If its distance is $1.0 \AA$, what fraction of an electronic charge, e exist on each atom?
(A) $25 \%$ of $e$
(B) $50 \%$ of e
(C) $60 \%$ of e
(D) $75 \%$ of $e$

Solution: (A)
$\delta=\frac{\text { Dipole moment }}{\mathrm{d}}$
$=\frac{1.2 \mathrm{D}}{1.0 \times 10^{-8} \mathrm{~cm}}$
$=\frac{1.2 \times 10^{-8} \mathrm{esu} \mathrm{cm}}{1.0 \times 10^{-8} \mathrm{~cm}}$
$=1.2 \times 10^{-8} \mathrm{esu}$
The fraction of electronic charge, e is
$=\frac{1.2 \times 10^{-10} \mathrm{esu}}{4.8 \times 10^{-10} \mathrm{esu} / \mathrm{e}}$
$=0.25 \mathrm{e}$
$=25 \%$ of e
18. A gas is heated through $1^{\circ} \mathrm{C}$ in a closed vessel and so the pressure increases by $0.4 \%$. The initial temperature of the gas was
(A) $-23^{\circ} \mathrm{C}$
(B) $+23^{\circ} \mathrm{C}$
(C) $250^{\circ} \mathrm{C}$
(D) $523^{\circ} \mathrm{C}$

Solution: (A)

$$
\begin{aligned}
& \text { Let } \mathrm{T}_{1}=\mathrm{T} \Rightarrow \mathrm{~T}_{2}=(\mathrm{T}+1) \\
& \text { And } \mathrm{p}_{1}=\mathrm{p} \Rightarrow \mathrm{p}_{2}=\mathrm{p}+\frac{0.4 \mathrm{p}}{100}=\frac{100.4}{100} \mathrm{p} \\
& \text { Form } \frac{\mathrm{p}_{1} \mathrm{~V}_{1}}{\mathrm{~T}_{1}}=\frac{\mathrm{p}_{2} \mathrm{~V}_{2}}{\mathrm{~T}_{2}} \\
& \frac{\mathrm{pV}}{\mathrm{~T}}=\frac{100.4 \mathrm{p}}{100} \times \frac{\mathrm{V}}{(\mathrm{~T}+1)} \\
& 100 \mathrm{~T}+100=100.4 \mathrm{~T} \\
& 0.4 \mathrm{~T}=100 \\
& \mathrm{~T}=\frac{100}{0.4}=250 \mathrm{~K} \\
& =(250-273)^{\circ} \mathrm{C} \\
& =-23^{\circ} \mathrm{C}
\end{aligned}
$$

19. For $2 \mathrm{NOBr}(\mathrm{g}) \rightleftharpoons 2 \mathrm{NO}(\mathrm{g})+\mathrm{Br}_{2}(\mathrm{~g})$ at equilibrium, $\mathrm{P}_{\mathrm{Br}_{2}}=\frac{\mathrm{p}}{\mathrm{q}}$ and p is the total pressure, the ratio $\frac{K_{p}}{\mathrm{p}}$ will be
(A) $\frac{1}{3}$
(B) $\frac{1}{9}$
(C) $\frac{1}{27}$
(D) $\frac{1}{81}$

Solution: (D)

$$
\begin{aligned}
& 2 \mathrm{NOBr}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NO}(\mathrm{~g}) \\
& \mathrm{p}=\left(\frac{2 \mathrm{p}}{9}+\frac{\mathrm{p}}{\mathrm{a}}\right) \quad \frac{2 \mathrm{p}}{9}+\underset{\frac{\mathrm{p}}{9}}{\mathrm{Br}_{2}(\mathrm{~g})} \\
& =\frac{6 \mathrm{p}}{9}
\end{aligned}
$$

And $\mathrm{K}_{\mathrm{p}}=\frac{\left(\mathrm{p}_{\mathrm{NO}}\right)^{2} \times\left(\mathrm{p}_{\mathrm{Br}_{2}}\right)}{\left(\mathrm{p}_{\mathrm{NOBr}}\right)^{2}}$
$=\frac{\left(\frac{2 \mathrm{p}}{9}\right)^{2} \times\left(\frac{\mathrm{p}}{9}\right)}{\left(\frac{6 \mathrm{p}}{9}\right)}=\frac{\mathrm{p}}{81}$
$\therefore \frac{\mathrm{K}_{\mathrm{p}}}{\mathrm{p}}=\frac{1}{81}$
20. The decomposition temperature is maximum for
(A) $\mathrm{MgCO}_{3}$
(B) $\mathrm{CaCO}_{3}$
(C) $\mathrm{BaCO}_{3}$
(D) $\mathrm{SrCO}_{3}$

Solution: (C)
Barium salts are quite stable because of great electropositive nature of Ba . Hence, Ba compounds possess high decomposition temperature.
21. When some amount of zinc is treated separately with excess of sulphuric acid and excess of sodium hydroxide solution, the ratio of volumes of hydrogen evolved is
(A) $1: 1$
(B) $1: 2$
(C) $2: 1$
(D) $2: 3$

Solution: (A)
$\mathrm{Zn}+\mathrm{H}_{2} \mathrm{SO}_{4} \rightarrow \mathrm{ZnSO}_{4}+\mathrm{H}_{2} \uparrow$
$\mathrm{Zn}+2 \mathrm{NaOH}+\rightarrow \mathrm{Na}_{2} \mathrm{ZnO}_{2}+\mathrm{H}_{2} \uparrow$
Hence, ratio of volumes of hydrogen evolved is $1: 1$.
22. A compound (A) when treated with $\mathrm{PCl}_{5}$ and then ammonia gave (B). (B) when treated with bromine and caustic potash produced (C). (C) on treatment with $\mathrm{NaNO}_{2}$ and HCl at $0^{\circ} \mathrm{C}$ and then boiling produce ortho-cresol. Compound (A)
(A) o-chlorotoluene
(B) o-toluic acid
(C) m-toluic acid
(D) o-bromotoluene

Solution: (B)

23. Alizarin is an example of
(A) triaryl dye
(B) azo dye
(C) vat dye
(D) anthraquinone dye

Solution: (D)
Alizarin is an anthraquinone dye. It gives a bright red colour with aluminium and a blue colour with barium.

24. What will be the main product when acetylene with hypochlorous acid?
(A) Trichloro acetaldehyde
(B) Acetaldehyde
(C) Dichloro acetaldehyde
(D) Chloro acetaldehyde

Solution: (C)

25. Barium titanate has the periovskite structure, i.e., a cubic lattice with $\mathrm{Ba}^{2+}$ ions at the corners of the unit cell, oxide ions at the face centres and titanium ions at the body centre. The molecular formula of barium titanate is
(A) $\mathrm{BaTiO}_{3}$
(B) $\mathrm{BaTiO}_{4}$
(C) $\mathrm{BaTiO}_{2}$
(D) BaTiO

Solution: (A)
Number of $\mathrm{Ba}^{2+}$ ions at the corner of unit cell
$=8 \times \frac{1}{8}=1$
Number of $\mathrm{O}^{2-}$ ions at the face centre
$=6 \times \frac{1}{2}=3$
Number of $\mathrm{Ti}^{4+}$ ions at the body centre $=1$
$\therefore$ Molecular formula of barium titanate
$=\mathrm{BaTiO}_{3}$
26. Which of the following hormone, is responsible for the growth of animals?
(A) Auxin
(B) Insulin
(C) Adrenaline
(D) Somatotropin

Solution: (D)
Somatotropin is the harmone, secreted by anterior lobe of pituitary gland. It is also called growth harmone as it stimulates protein synthesis, glycogenesis and some other biological activities. It deficiency causes midgets or dwarfism.
27. Which of the following have the largest ionic size?
(A) $\mathrm{F}^{-}$
(B) $\mathrm{O}^{2-}$
(C) $\mathrm{Na}^{+}$
(D) $\mathrm{Mg}^{2+}$

Solution: (B)
Number of electrons in $\mathrm{F}^{-}=9+1=10$
Number of electrons in $\mathrm{O}^{2}-=8+2=10$
Number of electrons in $\mathrm{Na}^{+}=11-1=10$
Number of electrons in $\mathrm{Mg}^{2}+=12-2=10$
Since, $\mathrm{F}^{-}, \mathrm{O}^{2-}, \mathrm{Na}^{+}, \mathrm{Mg}^{2+}$ are isoelectric and the size of isoelectric species decreases with increase in nuclear charge (i.e., number of protons), Hence correct order of size is $\mathrm{O}^{2-}>\mathrm{F}^{-}>$ $\mathrm{Na}^{+}<\mathrm{Mg}^{2+}$
28. If the radius of H is $0.53 \AA$ then what will be the radius of ${ }_{3} \mathrm{Li}^{2+}$ ?
(A) $0.17 \AA$
(B) $0.36 \AA$
(C) $0.53 \AA$
(D) $0.59 \AA$

Solution: (A)
The radius of hydrogen atom $=0.53 \AA .{ }_{3} \mathrm{Li}^{2+}$ ion also has only one electron but it has 3 protons in nucleus, hence, its electron feels three times more attraction from nucleus in comparison of hydrogen atom. Thus, the radius of ${ }_{3} \mathrm{Li}^{2+}$ will be
$=\frac{0.53}{3}=0.17 \AA$
29. Which of the following will have highest value of $\mathrm{pK}_{\mathrm{a}}$ ?
(A) $\mathrm{FCH}_{22} \mathrm{CH}_{2} \mathrm{COOH}$
(B) $\mathrm{CH}_{3} \mathrm{CH} \cdot \mathrm{F} \cdot \mathrm{COOH}$
(C) $\mathrm{CH}_{3} \mathrm{CH} \cdot \mathrm{Br} \cdot \mathrm{COOH}$
(D) $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{COOH}$

Solution: (D)
$\mathrm{pK} \mathrm{K}_{\mathrm{a}} \propto \frac{1}{\mathrm{~K}_{\mathrm{a}}}$
Stronger the acid, higher the $\mathrm{K}_{\mathrm{a}}$ values and lower the $\mathrm{pK}_{\mathrm{a}}$ value.
The order of acidity of given acids is as follows

$$
\mathrm{CH}_{3}<\mathrm{H} \cdot \mathrm{~F} \cdot \mathrm{COOH}>\mathrm{CH}_{3} \cdot \mathrm{CH} \cdot \mathrm{Br} \cdot \mathrm{COOH}>\mathrm{FCH}_{2} \mathrm{CH}_{2} \mathrm{COOH}>\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{COOH}
$$

Since, $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{COOH}$ is the weakest acid among the given, therefore its $\mathrm{p} \mathrm{K}_{\mathrm{a}}$ value will be highest.
30.

$$
\operatorname{Gas}(\mathrm{A})+\mathrm{NaOH} \rightarrow \mathrm{~B} \xrightarrow{\Delta} \mathrm{C} \xrightarrow{\Delta} \mathrm{D}_{\mathrm{C} \text { and } \mathrm{D} \text { decolourises acidified } \mathrm{KMnO}_{4} \text {. Identify } \mathrm{C}}
$$

and D .
(A) $\mathrm{Na}_{2} \mathrm{CO}_{3}, \mathrm{NaOH}$
(B) $(\mathrm{COOH})_{2},(\mathrm{COONa})_{2}$
(C) $(\mathrm{COONa})_{2},(\mathrm{COOH})_{2}$

Solution: (C)

$$
\underset{\mathrm{A}}{\mathrm{CO}}+\mathrm{NaOH} \rightarrow \underset{\mathrm{~B}}{\mathrm{HCOONa}} \underset{-\mathrm{H}_{2}}{\Delta}(\mathrm{COONa})_{2} \xrightarrow[\mathrm{C}]{\mathrm{H}^{+}} \underset{\mathrm{D}}{(\mathrm{COOH})_{2}}
$$

31. The polymer polyurethanes are formed by treating di-isocyanate with
(A) butadiene
(B) isoprene
(C) glycol
(D) acrylonitrile

Solution: (C)

32. What will be the volume of $\mathrm{O}_{2}$ at NTP liberated by 5 A current flowing for 193 s through acidulated water?
(A) 56 mL
(B) 112 mL
(C) 158 mL
(D) 965 mL

Solution: (A)
$W=\frac{\mathrm{C} \times \mathrm{t} \times \mathrm{E}}{\mathrm{F}}$
$=\frac{5 \times 193 \times 8}{96500}$
$\because$ At NTP, volume of
$32 \mathrm{~g} \mathrm{O}_{2}=22400 \mathrm{~mL}$
$\because$ Volume of $0.08 \mathrm{~g} \mathrm{O}_{2}=\frac{22400 \times 0.08}{32}$
$=56 \mathrm{~mL}$
33. $\mathrm{CO}_{2}$ goes to air, causes green house effect and gets dissolved in water. What will be the effect on soil fertility and pH of the water?
(A) Increase
(B) Decrease
(C) Remain same
(D) None of these

Solution: (B)
$\mathrm{CO}_{2}+\mathrm{H}_{2} \mathrm{O} \rightleftharpoons \mathrm{H}_{2} \mathrm{CO}_{3} \rightarrow \mathrm{H}^{+}+\mathrm{HCO}_{3}^{-}$
Here $\left[\mathrm{H}^{+}\right]$increases hence, pH decreases due to which soil fertility will also decreases.
34. $2 \mathrm{~N}_{2} \mathrm{O}_{5} \rightleftharpoons 4 \mathrm{NO}_{2}+\mathrm{O}_{2}$

If rate and rate constant for above reaction are $2.40 \times 10^{-5} \mathrm{~mol} \mathrm{~L}^{-1} \mathrm{~s}^{-1}$ and $3 \times 10^{-5} \mathrm{~S}^{-1}$ respectively, then calculate the concentration of $\mathrm{N}_{2} \mathrm{O}_{5}$.
(A) 1.4
(B) 1.2
(C) 0.04
(D) 0.8

Solution: (D)

The reaction is of first order and for a first order reaction,

Rate, $\mathrm{R}=\mathrm{k}\left[\mathrm{N}_{2} \mathrm{O}_{5}\right]$
$2.4 \times 10^{-5}=3 \times 10^{-5} \times\left[\mathrm{N}_{2} \mathrm{O}_{5}\right]$
$\left[\mathrm{N}_{2} \mathrm{O}_{5}\right]=\frac{2.4 \times 10^{-5}}{3 \times 10^{-5}}$
$=0.8 \mathrm{~mol} \mathrm{~L}^{-1}$
35. The molecule $\mathrm{BF}_{3}$ and $\mathrm{NF}_{3}$ both are covalent compounds, but $\mathrm{BF}_{3}$ is non-polar and $\mathrm{NF}_{3}$ is polar. The reason is that
(A) boron is a metal and nitrogen is a gas in uncombined state.
(B) $\mathrm{BF}_{3}$ bonds no dipole moment whereas $\mathrm{NF}_{3}$ bond have dipole moment.
(C) atomic size of boron is smaller than that of nitrogen
(D) $\mathrm{BF}_{3}$ is symmetrical molecule whereas $\mathrm{NF}_{3}$ is unsymmetrical.

Solution: (D)
$\mathrm{BF}_{3}$ is symmetrical planar, although it has polar bonds but resultant dipole moment is zero. In $\mathrm{NF}_{3}$, lone pair cause distortion, hence polarity arises.
36. $1.2 \% \mathrm{NaCl}$ solution is isotonic with $7.2 \%$ glucose solution. What will be the van't Hoff factor, i?
(A) 0.5
(B) 1
(C) 2
(D) 6

Solution: (C)

For $\mathrm{NaCl} \mathrm{pV}=\mathrm{nST} \times \mathrm{i}$
$\mathrm{p}_{\mathrm{i}} \times \frac{100}{1000}=\frac{1.2}{58.5} \times 0.0821 \times \mathrm{T} \times \mathrm{i}$
For glucose, $\mathrm{pV}=\mathrm{nST}$
$\mathrm{p}_{2} \times \frac{100}{1000}=\frac{7.2}{180} \times 0.0821 \times \mathrm{T}$
$\because \mathrm{NaCl}$ and glucose solutions are isotonic
$\therefore \mathrm{p}_{1}=\mathrm{p}_{2}$
On dividing Eq. (i) by (ii), we have
$i=\frac{7.2}{180} \times \frac{58.5}{1.2}=1.95=2$
37. Green vitriol is
(A) ferrous sulphate
(B) tin oxide
(C) zinc oxide
(D) ferrous carbonate

Solution: (A)
$\mathrm{FeSO}_{4} \cdot 7 \mathrm{H}_{2} \mathrm{O}$ is known as green vitriol.
38. 2-bromopentane with alcoholic KOH yields a mixture of three alkenes. Which of the following alkene is predominant?
(A) 1-pentene
(B) Cis-2-pentene
(C) Trans-2-pentene
(D) Cis-1-pentene

Solution: (C)


By Sautzeff's rule, substituted alkenes are more stable. Hence, out of cis and trans forms, trans product is more stable.
39. In which of the following compounds, the bond length between hybridized carbon atom and other carbon atom is minimum?
(A) Butane
(B) Propyne
(C) Propene
(D) Butane

Solution: (B)
We know $C-C$ bond length $=1.54 \AA$
That $C=C$ bond length $=1.34 \AA$
$\mathrm{C} \equiv \mathrm{C}$ bond length $=1.20 \AA$

Since, propyne has triple bond, therefore, it has minimum bond length.
40. Which of the following IUPAC name of compound?

(A) 1, 4-dichloro-2, 6-dioxo-4-carbonyl-1-oic acid
(B) 2,4-dioxo-1, 4-dichlorohexane-1-carboxylic acid
(C) 1-,-dichloro-2, 4, 6-dioxocyclohexane-1-carboxylic acid
(D) 1, 4-dichloro-4-formyl-2, 6-dioxy-cyclohexane-1-carboxylic acid

Solution: (D)

Hence IUPAC name is 1, 4-dichloro-4-formuyl 2, 6-dioxy -cyclohexane-1-carboxylic acid.


## Physics

## Single correct answer type:

1. A straight wire of mass 200 g and length 1.5 m carries a current of 2 A . It is suspended in mid-air by a uniform horizontal magnetic field $B$. The magnitude of $B$ (in tesla) is (assume $g=9.8 \mathrm{~ms}^{-2}$ )
(A) 2
(B) 1.5
(C) 0.55
(D) 0.65

Solution: (D)
Magnetic force on straight wire
$\mathrm{F}=$ Bil $\sin \theta=$ Bil $\sin 90^{\circ}-$ Bil
For equilibrium of wire in mid-air,
$\mathrm{F}=\mathrm{mg}$
Bil $=\mathrm{mg}$
$\therefore \mathrm{B}=\frac{\mathrm{mg}}{\mathrm{Bil}}=\frac{200 \times 10^{-3} \times 9.8}{2 \times 1.5}=0.65 \mathrm{~T}$
2. In the circuit shown the value of $\ell$ in ampere is

(A) 1
(B) 0.60
(C) 0.4
(D) 1.5

Solution: (C)


So, net resistance,
$\mathrm{R}=2.4+1.6=4.0 \Omega$

Therefore, current from the battery
$\mathrm{i}=\frac{\mathrm{V}}{\mathrm{R}}=\frac{4}{4}=1 \mathrm{~A}$

Now, from the circuit (b)

$$
\begin{aligned}
& 4 \mathrm{l}^{\prime}=6 \mathrm{l} \\
& \Rightarrow \mathrm{I}^{\prime}=\frac{3}{2} \mathrm{l} \\
& \text { But } \mathrm{i}=\mathrm{I}+\mathrm{I}^{\prime}-\mathrm{I}+\frac{3}{2} \mathrm{I}=\frac{5}{2} \mathrm{I} \\
& \therefore 1=\frac{5}{2} \mathrm{I} \\
& \Rightarrow \mathrm{I}=\frac{2}{5}-0.4 \mathrm{~A}
\end{aligned}
$$

3. When light of wavelength 300 nm falls on a photoelectric emitter, photoelectrons are liberated. For another emitter, light of wavelength 600 nm is sufficient for liberating photoelectrons. The ratio of the work function of the two emitters is
(A) $1: 2$
(B) $2: 1$
(C) $4: 1$
(D) $1: 4$

Solution: (B)

Work function is given by
$\phi=\frac{\mathrm{hc}}{\lambda}$ or $\phi \propto \frac{1}{\lambda}$
$\because \frac{\phi_{1}}{\phi_{2}}=\frac{\lambda_{2}}{\lambda_{1}}$
$=\frac{600}{300}=\frac{2}{1}$
4. A monatomic gas is suddenly compressed to $\left(\frac{1}{8}\right)$ th of its initial volume adiabatically. The ratio of its final pressure to the initial pressure is (Given, the ratio of the specific heats of the given gas to be $5 / 3$ )
(A) 32
(B) $40 / 3$
(C) $24 / 5$
(D) 8

Solution: (A)

In an adiabatic process,
$\mathrm{PV}^{\gamma}=$ constant
$\Rightarrow \frac{\mathrm{p}_{1}}{\mathrm{p}_{2}}=\left(\frac{\mathrm{V}_{2}}{\mathrm{v}_{1}}\right)^{\gamma}$
$\Rightarrow \frac{\mathrm{p}_{1}}{\mathrm{p}_{2}}=\left(\frac{1}{8}\right)^{5 / 3}$
$\Rightarrow \frac{\mathrm{p}_{1}}{\mathrm{p}_{2}}=\left(\frac{1}{2^{3}}\right)^{5 / 3}$
$=\frac{1}{32}$
$\therefore \frac{\mathrm{p}_{2}}{\mathrm{p}_{1}}=32$
5. The intensity of the magnetic induction field at the centre of a single turn circular coil of radius 5 cm carrying current of 0.9 A is
(A) $36 \pi \times 10^{-7} \mathrm{~T}$
(B) $9 \pi \times 10^{-7} \mathrm{~T}$
(C) $36 \pi \times 10^{-6} \mathrm{~T}$
(D) $9 \pi \times 10^{-6} \mathrm{~T}$

Solution: (A)
The intensity of magnetic induction field
$B=\frac{\mu_{0} i}{2 r}$
$=\frac{4 \pi \times 10^{-7} \times 0.9}{2 \times 5 \times 10^{-2}}$
$B=36 \pi \times 10^{-7} T$
6. A capacitor of capacity of $0.1 \mu \mathrm{~F}$ connected in series to a resistor of $10 \mathrm{M} \Omega$ is charged to a certain potential and then made to discharge through resistor. The time in which the potential will take to fall to half its original value is
(Given, $\log _{10} 2=0.3010$ )
(A) 2 s
(B) 0.693 s
(C) 0.5 s
(D) 1.0 s

Solution: (B)
By equation of charging,
$\mathrm{q}=\mathrm{q}_{0}\left(1-\mathrm{e}^{-\mathrm{t} / \mathrm{CR}}\right)$
According to question,

$$
\frac{\mathrm{q}}{\mathrm{q}_{\mathrm{o}}}=\frac{1}{2}=0.50
$$

$$
\therefore 0.50=1-\mathrm{e}^{-\mathrm{t} / C R}
$$

$$
e^{-t / C R}=1-0.50=0.50
$$

$$
e^{-t / C R}=2
$$

or $\frac{1}{C R}=\log _{e} 2$
or $\frac{\mathrm{t}}{\mathrm{CR}}=2.3026 \log _{10} 2$
or $\mathrm{t}=\mathrm{CR} \times 2.3026 \log _{10} 2$
or $t=0.1 \times 10^{-6} \times 10 \times 10^{6} \times 2.3026 \log _{10} 2$
or $\mathrm{t}=2.3026 \times 0.3010$
or $\mathrm{t}=0.693 \mathrm{~s}$
7. If the force is given by $\mathrm{F}=\mathrm{at}+\mathrm{bt}{ }^{2}$ with t as time. The dimensions of a and b are
(A) $\left[\mathrm{MLT}^{-4}\right],\left[\mathrm{MLT}^{-2}\right]$
(B) $\left[\mathrm{MLT}^{-3}\right],\left[\mathrm{MLT}^{-4}\right]$
(C) $\left[\mathrm{ML}^{2} \mathrm{~T}^{-3}\right],\left[\mathrm{ML}^{2} \mathrm{~T}^{-2}\right]$
(D) $\left[\mathrm{ML}^{2} \mathrm{~T}^{-3}\right],\left[\mathrm{ML}^{3} \mathrm{~T}^{-4}\right]$

Solution: (B)

Dimension of at $=$ Dimension of $F$

$$
[\mathrm{at}]=[\mathrm{F}]
$$

$[\mathrm{a}]=\left[\frac{\mathrm{F}}{\mathrm{t}}\right]$
$[\mathrm{a}]=\left[\frac{\mathrm{MLT}^{-2}}{\mathrm{~T}}\right]$
$[\mathrm{a}]=\left[\mathrm{MLT}^{-3}\right]$
Dimension of $\mathrm{bt}^{2}=$ Dimension of F
$\left[\mathrm{bt}^{2}\right]=[\mathrm{F}]$
$[\mathrm{b}]=\left[\frac{\mathrm{F}}{\mathrm{t}^{2}}\right]$
$[\mathrm{b}]=\left[\frac{\mathrm{MLT}^{-2}}{\mathrm{~T}^{2}}\right]$
$[\mathrm{b}]=\left[\mathrm{MLT}^{-4}\right]$
8. A ray of light is incident on the interface between water and glass at an angle I and refracted parallel to the water surface, then value of $\mu_{\mathrm{g}}$ will be

(A) $(4 / 3) \sin i$
(B) $\frac{1}{\sin i}$
(C) $\frac{4}{3}$
(D) 1

Solution: (B)

$$
\begin{aligned}
& { }_{\mathrm{g}} \mu_{\mathrm{w}}=\frac{\sin \mathrm{i}}{\sin \mathrm{r}} \\
& { }_{\mathrm{g}} \mu_{\mathrm{a}}=\frac{\sin \mathrm{r}}{\sin 90^{\circ}} \\
& \Rightarrow \quad{ }_{\mathrm{g}} \mu_{\mathrm{w}}=\times \quad{ }_{\mathrm{w}} \mu_{\mathrm{a}}=\frac{\sin \mathrm{i}}{\sin \mathrm{r}} \times \frac{\sin \mathrm{r}}{\sin 90^{\circ}}=\sin \mathrm{i} \\
& \text { or } \frac{\mu_{\mathrm{w}}}{\mu_{\mathrm{g}}} \times \frac{\mu_{\mathrm{a}}}{\mu_{\mathrm{w}}}=\sin \mathrm{i}
\end{aligned}
$$

$\Rightarrow \mu_{\mathrm{g}}=\frac{1}{\sin \mathrm{i}}$
9. A body is moved in straight line by constant power of machine. What will be the relation between the travelling distance and time?
(A) $s^{2} \propto t^{3}$
(B) $s^{2} \propto t$
(C) $s^{3} \propto t^{2}$
(D) $s \propto t^{3}$

Solution: (A)
Power $=\left[\mathrm{ML}^{2} \mathrm{~T}^{-3}\right]=$ constant
$\therefore\left[\frac{\mathrm{ML}^{2}}{\mathrm{~T}^{3}}\right]=\mathrm{constant}$
$\therefore\left[\mathrm{L}^{2}\right] \propto\left[\mathrm{T}^{3}\right]$
$\operatorname{Or} S^{2} \propto t^{3}$
10. Magnetic moment of bar magnet is M . The work done to turn the magnet by $90^{\circ}$ of magnet in direction of magnetic field $B$ will be
(A) Zero
(B) $\frac{1}{2} \mathrm{MB}$
(C) 2 MB
(D) MB

Solution: (D)

Work done,
$\mathrm{W}=\mathrm{MB}(1-\cos \theta)$
$\theta=90^{\circ}$
$\therefore \mathrm{W}=\mathrm{MB}$
11. Voltage V and current I in AC circuit are given by
$V=50 \sin (50 t)$ volt
$i=50 \sin \left(50 t+\frac{\pi}{3}\right) \mathrm{mA}$
The power dissipated in circuit is
(A) 5.0 W
(B) 2.5 W
(C) 1.25 W
(D) zero

Solution: (C)
Given, $V=50 \sin (50 t) V$
Maximum voltage, $\mathrm{V}_{0}=50 \mathrm{~V}$
$i=i_{0} \sin \left(50 t+\frac{\pi}{3}\right) m A$

Maximum current, $\mathrm{i}_{0}=50 \mathrm{~mA}=50 \times 10^{-3} \mathrm{~A}$
Power dissipated, $p=\frac{i_{0}}{\sqrt{2}} \times \frac{\mathrm{V}_{0}}{\sqrt{2}}$
$=\frac{50 \times 50 \times 10^{-3}}{2}$
$=\frac{2500 \times 10^{-3}}{2}=1.25 \mathrm{~W}$
12. A simple wave motion represents by $y=5(\sin 4 \pi t+\sqrt{3} \cos 4 \pi t)$. Its amplitude is
(A) 5
(B) $5 \sqrt{3}$
(C) $10 \sqrt{3}$
(D) 10

Solution: (D)

$$
\begin{aligned}
& y=5(\sin 4 \pi t+\sqrt{3} \cos 4 \pi t) \\
& y=5(\sin 4 \pi t+5 \sqrt{2} \cos 4 \pi t) \\
& A=\sqrt{A_{1}^{2}+A_{2}^{2}} \\
& A=\sqrt{(5)^{2}+(5 \sqrt{3})^{2}} \\
& =\sqrt{25+75}=\sqrt{100}=10
\end{aligned}
$$

13. A large open tank has two holes in the wall. One is a square hole of side $L$ at a depth $y$ from the top and the other is a circular hole of radius $R$ at a depth $4 y$ from the top. When the tank is completely filled with water, the quantities or water flowing out per second from the two holes are the same. Then, the value of $R$ is
(A) $\frac{\mathrm{L}}{\sqrt{2 \pi}}$
(B) $2 \pi \mathrm{~L}$
(C) $\mathrm{L} \sqrt{\frac{2}{\pi}}$
(D) $\frac{\mathrm{L}}{2 \pi}$

Solution: (A)
By the principle of continuity
$\mathrm{A}_{1} \mathrm{v}_{1}=\mathrm{A}_{2} \mathrm{v}_{2}$
According to question, $\mathrm{A}_{1}=\mathrm{L}^{2}$
$\mathrm{v}_{1}=\sqrt{2 \mathrm{gy}}$
And $\mathrm{A}_{2}=\pi \mathrm{R}^{2}$
$\mathrm{v}_{2}=\sqrt{2 \mathrm{~g} 4 \mathrm{y}}$
$\therefore \mathrm{L}^{3} \sqrt{2 \mathrm{gy}}=\pi \mathrm{R}^{2} \sqrt{2 \mathrm{~g} 4 \mathrm{y}}$
or $\mathrm{L}^{2}=2 \pi \mathrm{R}^{2}$
or $\mathrm{R}=\frac{\mathrm{L}}{\sqrt{2 \pi}}$
14. In the circuit shown below, the ammeter reading is zero. Then, the value of the resistance $R$ is

(A) $50 \Omega$
(B) $100 \Omega$
(C) $200 \Omega$
(D) $400 \Omega$

## Solution: (B)

Given that


In loop (1)
$12-500 i_{1}-\mathrm{Ri}_{1}=0$
$\Rightarrow 12=\mathrm{i}_{1}(500+\mathrm{R})$
In loop (2)
$12-500 \mathrm{i}_{1}-2=0$
$\Rightarrow 10=500 \mathrm{i}_{1}$
Or $\mathrm{i}_{1}=\frac{1}{50} \mathrm{~A}$
From equations (i) and (ii)
$12 \times \frac{1}{i_{1}}=(500+R)$
$\Rightarrow 12 \times 50=500+\mathrm{R}$
$\Rightarrow \mathrm{R}=100 \Omega$
15. The dimensional formula for inductance is
(A) $\left[\mathrm{ML}^{2} \mathrm{~T}^{-2} \mathrm{~A}^{-2}\right]$
(B) $\left[\mathrm{ML}^{2} \mathrm{TA}^{-2}\right]$
(C) $\left[\mathrm{ML}^{2} \mathrm{~T}^{-1} \mathrm{~A}^{-2}\right]$
(D) $\left[\mathrm{ML}^{2} \mathrm{~T}^{-2} \mathrm{~A}^{-2}\right]$

Solution: (A)
EMF induced in an electrical circuit

$$
\begin{aligned}
& \mathrm{e}=\mathrm{L} \frac{\mathrm{dt}}{\mathrm{dt}} \quad \text { (numerically) } \\
& \text { or } \mathrm{L}=\mathrm{e} \frac{\mathrm{dt}}{\mathrm{dt}} \\
& =\frac{\mathrm{W}}{\mathrm{Q}} \cdot \frac{\mathrm{dt}}{\mathrm{dt}} \quad\left(\because \mathrm{e}=\mathrm{V}=\frac{\mathrm{W}}{\mathrm{Q}}\right) \\
& =\frac{\mathrm{Wdt}}{\mathrm{It} \cdot \mathrm{dl}}=\frac{\left[\mathrm{ML}^{2} \mathrm{~T}^{-2}\right][\mathrm{T}]}{[\mathrm{A}][\mathrm{T}][\mathrm{A}]} \\
& =\left[\mathrm{ML}^{2} \mathrm{~T}^{-2} \mathrm{~A}^{-2}\right]
\end{aligned}
$$

16. The maximum current that can be measured by a galvanometer of resistance $40 \Omega$ is 10 mA . It is converted into a voltmeter that can read upto 50 V . The resistance to be connected in series with the galvanometer (in ohms) is
(A) 2010
(B) 4050
(C) 5040
(D) 4960

Solution: (D)
To convert a galvanometer into voltmeter, the necessary value of resistance to be connected in series with the galvanometer is
$\mathrm{R}=\frac{\mathrm{V}}{\mathrm{I}_{\mathrm{g}}}-\mathrm{G}$
$=\frac{50}{10 \times 10^{-3}}-40$
$=5000-40=4960 \Omega$
17. For a given velocity, a projectile has the same range $R$ for two angles of projection if $t_{1}$ and $t_{2}$ are the time of flight in the two case, then
(A) $t_{1} t_{2} \propto R$
(B) $\mathrm{t}_{1} \mathrm{t}_{2} \propto \mathrm{R}^{2}$
(C) $\mathrm{t}_{2} \mathrm{t}_{2} \propto \frac{1}{\mathrm{R}^{2}}$
(D) $t_{1} t_{2} \propto \frac{1}{R}$

Solution: (A)
$\mathrm{t}_{1}=\frac{2 \mathrm{u} \sin \alpha}{\mathrm{g}}$
$\mathrm{t}_{2}=\frac{2 \mathrm{u} \sin \left(90^{\circ}-\alpha\right)}{\mathrm{g}}$
So, $\mathrm{t}_{1} \times \mathrm{t}_{2}=2 \frac{\mathrm{u}^{2}}{\mathrm{~g}^{2}} \sin 2 \alpha$
or $\mathrm{t}_{1} \times \mathrm{t}_{2}=\frac{2 \mathrm{R}}{\mathrm{g}} \quad\left(\because \quad \mathrm{R}=\frac{\mathrm{u}^{2} \sin 2 \alpha}{\mathrm{~g}}\right)$
$t_{1} \times t_{2} \propto R$
18. A sample of ideal monoatomic gas is taken round the cycle ABCA as shown in the figure. The work done during the cycle is

(A) 3 pV
(B) zero
(C) 9 pV
(D) 6 pV

Solution: (A)
The work done $=$ area of $p-V$ graph
= area of triangle $A B C$
$=\frac{1}{2} \times 3 \mathrm{p} \times 2 \mathrm{~V}=3 \mathrm{pV}$
19. A sound source is moving towards stationary listener with $\frac{1}{20}$ th of the speed of sound. The ratio of apparent to real frequency is
(A) $\left(\frac{9}{10}\right)^{2}$
(B) $\frac{10}{9}$
(C) $\frac{11}{10}$
(D) $\left(\frac{11}{10}\right)^{2}$

Solution: (B)
Given, $\mathrm{n}_{\mathrm{s}}=\frac{\mathrm{n}}{10}$
Apparent frequency $\mathrm{n}^{\prime}=\mathrm{n}\left(\frac{\mathrm{v}}{\mathrm{v}-\mathrm{v}_{\mathrm{s}}}\right)$
Where, $\mathrm{n}=$ real frequency of source
$\mathrm{v}=$ velocity of sound
$\mathrm{v}_{\mathrm{s}}=$ velocity of source
So, $\frac{\mathrm{n}^{\prime}}{\mathrm{n}}=\frac{\mathrm{v}}{\mathrm{v}-\frac{\mathrm{v}}{10}}=\frac{10}{9}$
20. A satellite is in a circular orbit round the earth at an altitude $R$ above the earth's surface, where $R$ is the radius of the earth. If $g$ is the acceleration due to gravity on the surface of the earth, the speed of the satellite is
(A) $\sqrt{2 \mathrm{Rg}}$
(B) $\sqrt{\mathrm{Rg}}$
(C) $\sqrt{\frac{\mathrm{Rg}}{2}}$
(D) $\frac{\sqrt{\mathrm{Rg}}}{4}$

Solution: (C)
Orbital velocity $\left(\mathrm{v}_{0}\right)$ at a height h above the earth's surface is given by
$v_{0}=R_{e} \sqrt{\frac{g}{R_{e}+h}}$

Given, $\mathrm{h}=\mathrm{R}_{\mathrm{e}}$
$\therefore \quad \mathrm{v}_{0}=\mathrm{R} \sqrt{\frac{\mathrm{g}}{2 \mathrm{R}}}$
$=\sqrt{\frac{2 \mathrm{~g}}{2}}$
21. A 10 kg stone is suspended with a rope of breaking strength $30 \mathrm{~kg} . \mathrm{wt}$. The minimum time in which the stone can be raised through a height 10 m starting from rest is
(Taking g = $10 \mathrm{Nkg}^{-1}$ )
(A) 0.5 s
(B) 1.0 s
(C) $\sqrt{\frac{2}{3}} \mathrm{~s}$
(D) 2.0 s

Solution: (B)
Tension in the string $\mathrm{T}=\mathrm{mg}$
$=30 \times 10$
$=300 \mathrm{~N}$

$\mathrm{T}-\mathrm{Mg}=\mathrm{Ma}$
From the figure
$300-10 \times 10=10 a$
$\therefore \mathrm{a}=20 \mathrm{~ms}^{-2}$
Thus, the maximum acceleration with which the stone can be raised is $20 \mathrm{~ms}^{-2}$.
Given, $\mathrm{s}=10 \mathrm{~m}$
And $u=0$
$\therefore 10=\frac{1}{2}(20) \mathrm{t}^{2}$
$\Rightarrow \mathrm{t}=1 \mathrm{~s}$
22. How much work must be done by a force on 50 kg body in order to accelerate it from rest to $20 \mathrm{~m} / \mathrm{s}$ in 10 s ?
(A) $10^{3} \mathrm{~J}$
(B) $10^{4} \mathrm{~J}$
(C) $2 \times 10^{3} \mathrm{~J}$
(D) $5 \times 10^{4} \mathrm{~J}$

Solution: (B)
Now, $s=u t+\frac{1}{2} a^{2}$
$s=0+\frac{1}{2} \times 10 \times 10$
$\mathrm{s}=100 \mathrm{~m}$
Hence, work done
$\mathrm{W}=\mathrm{F} \times \mathrm{s}$
$\mathrm{W}=\mathrm{ma} \times \mathrm{s}$
$\therefore \mathrm{W}=50 \times 2 \times 100$
$\mathrm{W}=10000=10^{4} \mathrm{~J}$
23. $A$ and $B$ are two metals with threshold frequencies $1.8 \times 10^{14} \mathrm{~Hz}$ and $2.2 \times 10^{14} \mathrm{~Hz}$. Two identical photons of energy 0.825 eV are incident on them. Then photoelectrons are emitted by (Taking $\mathrm{h}=6.6 \times 10^{-34} \mathrm{~J}-\mathrm{s}$ )
(A) B alone
(B) A alone
(C) Neither A nor B
(D) Both $A$ and $B$

Solution: (B)
Threshold energy of $A$ is
$\mathrm{E}_{\mathrm{A}}=\mathrm{h} \mathrm{v}_{\mathrm{A}}$
$=6.6 \times 10^{-34} \times 1.8 \times 10^{14}$
$=11.88 \times 10^{-20} \mathrm{~J}$
$=\frac{11.88 \times 10^{-20}}{1.6 \times 10^{-19}} \mathrm{eV}$
$=0.74 \mathrm{eV}$
Similarly, $\mathrm{E}_{\mathrm{B}}=0.91 \mathrm{eV}$

Since, the incident photons have energy greater than $E_{A}$ but less than $E_{B}$.

So, photoelectrons will be emitted from metal A only.
24. The square of resultant of two equal forces is three times their product. Angle between the forces is
(A) $\pi$
(B) $\frac{\pi}{2}$
(C) $\frac{\pi}{4}$
(D) $\frac{\pi}{3}$

Solution: (D)
Let $\theta$ be the angle between vectors <b>P</b> and <b>B</b>
Whose resultant is $\langle b>R</ b>$.
Hence, $\mathrm{P}=\mathrm{Q}$ and $\mathrm{R}^{2}=3 \mathrm{PQ}=3 \mathrm{P}^{2}$
As $\mathrm{R}^{2}=\mathrm{P}^{2}+\mathrm{Q}^{2}+2 \mathrm{PQ} \cos \theta$
$\therefore 3 \mathrm{P}^{2}=\mathrm{P}^{2}+\mathrm{P}^{2}+2 \mathrm{P}^{2} \cos \theta$
or $3 \mathrm{P}^{2}-2 \mathrm{P}^{2}=2 \mathrm{P}^{2} \cos \theta$
or $\mathrm{P}^{2}=2 \mathrm{P}^{2} \cos \theta$
or $1=2 \cos \theta$
$\therefore \cos \theta=\frac{1}{2}$, thus. $\cos \theta=\cos 60^{\circ}$
or $\theta=60^{\circ}=\frac{\pi}{3}$
25. An object placed on a ground is in stable equilibrium. If the objects is given a slight push, then initially the position of centre of gravity
(A) moves nearer to ground
(B) rises higher above the ground
(C) Remains as such
(D) May remain at same level

Solution: (B)

In stable equilibrium, the centre of gravity of object, lies at minimum height from ground. As the object is given a slight push, its centre of gravity rises because it comes in unstable equilibrium.
26. The maximum height attained by a projectile when thrown at an angle $\theta$ with the horizontal is found to be half the horizontal range. Then, $\theta$ is equal to
(A) $\tan ^{-1}(2)$
(B) $\frac{\pi}{6}$
(C) $\frac{\pi}{4}$
(D) $\tan ^{-1}\left(\frac{1}{2}\right)$

Solution: (A)
Minimum height, $H_{0}=\frac{u^{2} \sin ^{2} \theta}{2 g}$
Range, $R=\frac{u^{2} \sin 2 \theta}{g}$
Given, $H_{0}=\frac{R}{2}$
$\therefore \frac{\mathrm{u}^{2} \sin ^{2} \theta}{2 \mathrm{~g}}=\frac{\mathrm{u}^{2} 2 \sin \theta \cos \theta}{2 \mathrm{~g}}$
$\Rightarrow \sin \theta=2 \cos \theta$
$\Rightarrow \tan \theta=2$
$\therefore \theta=\tan ^{-1}(2)$
27. A shell of mass 20 kg at rest explodes into two fragments whose masses are in the ratio $2: 3$. The smaller fragment moves with a velocity of $6 \mathrm{~ms}^{-1}$. The kinetic energy of the larger fragment is
(A) 96 J
(B) 216 J
(C) 144 J
(D) 360 J

Solution: (A)

Total mass of the shell $=20 \mathrm{~kg}$
Ratio of the masses of the fragments $=2: 3$
$\therefore$ Masses of the fragments are 8 kg and 12 kg
Now, according to the conservation of momentum
$m_{1} v_{1}=m_{2} v_{2}$
$\therefore 8 \times 6=12 \times \mathrm{v}$
v (velocity of the larger fragment) $=4 \mathrm{~m} / \mathrm{s}$
Kinetic energy $=\frac{1}{2} \mathrm{mv}^{2}$
$=\frac{1}{2} \times 12 \times(4)^{2}=96 \mathrm{~J}$
28. If the displacement of simple pendulum at any time is 0.02 m and acceleration is $2 \mathrm{~m} / \mathrm{s}^{2}$, then in this time angular velocity will be
(A) $100 \mathrm{rad} / \mathrm{s}$
(B) $10 \mathrm{rad} / \mathrm{s}$
(C) $1 \mathrm{rad} / \mathrm{s}$
(D) $0.1 \mathrm{rad} / \mathrm{s}$

Solution: (B)

$$
\text { Acceleration }|\alpha|=\omega^{2} \mathrm{x}
$$

or $\omega=\sqrt{\frac{\alpha}{x}}$
$=\sqrt{\frac{2}{0.002}}$
$=10 \mathrm{rad} / \mathrm{s}$
29. Which is constant, the earth revolving around the sun?
(A) Angular momentum
(B) Linear momentum
(C) Rotational kinetic energy
(D) Kinetic energy

Solution: (A)
Kepler's second law
$\frac{\mathrm{dA}}{\mathrm{dt}}=\frac{\mathrm{L}}{2 \mathrm{~m}}$
$\frac{\mathrm{dA}}{\mathrm{dt}}=$ constant
$L=$ constant
30. In non-elastic collision,
(A) momentum is conserved
(B) energy is conserved
(C) momentum and energy are conserved
(D) momentum and energy are non-conserved

Solution: (D)

Momentum is conserved is non-elasticity collision but kinetic energy is not conserved.
31. A mica slit of thickness $t$ and refractive index $\mu$ is introduced in the ray from the first source $S_{1}$. By how much distance of fringes pattern will be displaced?
(A) $\frac{d}{D}(\mu-1) t$
(B) $\frac{D}{d}(\mu-1) t$
(C) $\frac{d}{(\mu-1) D}$
(D) $\frac{\mathrm{D}}{\mathrm{t}}(\mu-1)$

Solution: (B)
Fringe displacement $\mathrm{x}_{0}=\frac{\mathrm{D}(\mu-1) \mathrm{t}}{\mathrm{d}}$
32. The refractive index of water is $4 / 3$ and that of glass is $5 / 3$. What will be the critical angle for the ray of light entering water from the glass?
(A) $\sin ^{-1}\left(\frac{4}{5}\right)$
(B) $\sin ^{-1}\left(\frac{5}{4}\right)$
(C) $\sin ^{-1}\left(\frac{1}{2}\right)$
(D) $\sin ^{-1}\left(\frac{2}{1}\right)$

Solution: (A)
$\mu=\frac{\mu_{1}}{\mu_{2}}=\frac{5 / 3}{4 / 3}=\frac{5}{4}$
$\sin C=\frac{1}{\mu}=\frac{4}{5}$
33. The produced rays in sonography are
(A) microwaves
(B) infrared wave
(C) sound waves
(D) ultra sound

Solution: (D)

The produced rays in sonography ultra sound.
34. The ratio of secondary of primary turns of step up transformer is $4: 1$. If a current of 4 A is applied to the primary, the induced current in secondary will be
(A) 8 A
(B) 2 A
(C) 1 A
(D) 0.5 A

Solution: (C)
$\frac{\mathrm{I}_{\mathrm{s}}}{\mathrm{I}_{\mathrm{p}}}=\frac{\mathrm{N}_{\mathrm{p}}}{\mathrm{N}_{\mathrm{s}}}=\frac{1}{4}$
$\mathrm{I}_{\mathrm{S}}=\frac{1}{4} \times 4=1 \mathrm{~A}$
35. The minimum force required to move a body up an inclined plane is three times the minimum force required to prevent it from sliding down the plane. If the coefficient of friction between the body and the inclined plane is $\frac{1}{2 \sqrt{3}}$, the angle of the inclined plane is
(A) $60^{\circ}$
(B) $45^{\circ}$
(C) $30^{\circ}$
(D) $15^{\circ}$

Solution: (C)
Minimum force required to move a body up a rough inclined plane
$\mathrm{F}_{1}=\mathrm{mg}(\sin \theta+\mu \cos \theta)$
Minimum force required to prevent the body from sliding down the rough inclined plane.
$\mathrm{F}_{2}=\mu \mathrm{mg} \cos \theta$
According to question,
$\mathrm{F}_{1}=3 \mathrm{~F}_{2}$
$\therefore m g(\sin \theta+\mu \cos \theta)=3(\mu \cos \theta)$
$\sin \theta+\mu \cos \theta=3 \mu \cos \theta$
$\sin \theta=2 \mu \cos \theta$
$=2 \times \frac{1}{2 \sqrt{3}}=\frac{1}{\sqrt{3}}$
$=\tan 30^{\circ}$
$\theta=30^{\circ}$
36. If $\mathrm{k}_{\mathrm{s}}$ and $\mathrm{k}_{\mathrm{p}}$ respectively are effective spring constant in series and parallel combination of springs as shown in figure, find $\frac{\mathrm{k}_{\mathrm{s}}}{\mathrm{k}_{\mathrm{p}}}$

(A) $\frac{9}{2}$
(B) $\frac{3}{7}$
(C) $\frac{2}{9}$
(D) $\frac{7}{3}$

Solution: (C)
The effective spring constant $\mathrm{k}_{\mathrm{s}}$ of this arrangement is
$\frac{1}{\mathrm{k}_{\mathrm{s}}}=\frac{1}{\mathrm{k}}+\frac{1}{2 \mathrm{k}}$
$\frac{1}{\mathrm{k}_{\mathrm{s}}}=\frac{2+1}{2 \mathrm{k}}=\frac{3}{2 \mathrm{k}}$
$\mathrm{k}_{\mathrm{s}}=\frac{2 \mathrm{k}}{3}$
The effective spring constant $\mathrm{k}_{\mathrm{p}}$ of this arrangement is
$\mathrm{k}_{\mathrm{p}}=\mathrm{k}_{1}+\mathrm{k}_{2}$
$=\mathrm{k}+2 \mathrm{k}=3 \mathrm{k}$
$\therefore \frac{\mathrm{k}_{\mathrm{s}}}{\mathrm{k}_{\mathrm{p}}}=\frac{2 \mathrm{k} / 3}{3 \mathrm{k}}=\frac{2}{9}$
37. The power dissipated across resistance R which is connected across a battery of potential V is P . If resistance is doubled, then the power becomes
(A) $1 / 2$
(B) 2
(C) $1 / 4$
(D) 1

Solution: (A)
Electric power
$P=\frac{V^{2}}{R}$
or $P \propto \frac{1}{R}$
or $\frac{\mathrm{P}_{2}}{\mathrm{P}_{1}}=\frac{\mathrm{R}_{1}}{\mathrm{R}_{2}}=\frac{\mathrm{R}}{2_{\mathrm{R}}}$
$P_{2}=\frac{P}{2}$
38. A body moves with uniform acceleration then which of the following graph is correct?
(A)

(B)

(C)

(D)


Solution: (C)
An object is said to be moving with a uniform acceleration, if its velocity change by equal amount in equal intervals of time. The velocity-time graph of uniformly accelerated motion is a straight line inclined to time axis. Acceleration of an object in a uniformly accelerated motion in one dimension is equal to the slope of the velocity-time graph with time axis.
39. The rate at which a black body emits radiation at a temperature T is proportional to
(A) $\frac{1}{T}$
(B) T
(C) $\mathrm{T}^{3}$
(D) $\mathrm{T}^{4}$

Solution: (D)
From Stefan's law the rate of emission of energy per unit surface area of a black body is inversely proportional to the fourth power of absolute temperature ( $T$ ) of the body.
$\mathrm{E}=\sigma \mathrm{T}^{4}(\sigma=$ Stefan's constant $)$
40. Two equal charges $q$ are kept fixed at $a$ and $+a$ along the $x$-axis. A particle of mass $m$ and charge $\frac{\mathrm{q}}{2}$ is brought to the origin and given a small displacement along the $x$-axis, then
(A) the particle executes oscillatory motion
(B) the particle remains stationary
(C) the particle executes SHM along $x$-axis
(D) the particle executes SHM along $y$-axis

Solution: (C)
From Coulomb's law
$\mathrm{F}=\frac{1}{4 \pi \varepsilon_{0}}=\frac{\mathrm{q}_{1} \mathrm{q}_{2}}{\mathrm{r}^{2}}$

$F=\frac{1}{4 \pi \varepsilon_{0}}=\frac{q \times \frac{q}{2}}{(a+x)^{2}}-\frac{1}{4 \pi \varepsilon_{0}} \cdot \frac{q \times \frac{q}{2}}{(a-x)^{2}}$
$=\frac{1}{4 \pi \varepsilon_{0}} \frac{\mathrm{q}^{2}}{2}\left[\frac{1}{(\mathrm{a}+\mathrm{x})^{2}}-\frac{1}{(\mathrm{a}-\mathrm{x})^{2}}\right]$
$=\frac{1}{4 \pi \varepsilon_{0}} \cdot \frac{\mathrm{q}^{2}}{2}\left[-\frac{4 \mathrm{ax}}{\left(\mathrm{a}^{2}-\mathrm{x}^{2}\right)^{2}}\right]$
When $\mathrm{x} \ll \mathrm{a}$, then
$F \propto=-\frac{2 q^{2}}{4 \pi \varepsilon_{0} a^{3}} \mathrm{X}$
$\Rightarrow \mathrm{F} \propto-\mathrm{x}$
Hence, SHM along x-axis

