

PHYSICS

1. A particle performs simple harmonic motion with amplitude A. Its speed is trebled at the instant that it is at a distance $\frac{2A}{3}$ from equilibrium position. The new amplitude of the motion is:

(1)
$$A\sqrt{3}$$

(2) $\frac{7A}{3}$
(3) $\frac{A}{3}\sqrt{41}$
(4) 3A
Solution: (2)
 $v = \omega\sqrt{A^2 - X^2}$;
 $v = \omega\sqrt{A^2 - \frac{4A^2}{9}}$
 $= \frac{\omega\sqrt{5A}}{3}$
New SHM will be,
 $3v - \omega\sqrt{A_N^2 - X_n^2}$;
 $\frac{3\omega\sqrt{5A}}{3} = \omega\sqrt{A_N^2 - \frac{4A^2}{9}}$
 $5A^2 = A_N^2 - \frac{4A^2}{9}$
 $A_N^2 = \frac{49A^2}{9}$
 $A_N = \frac{7A}{3}$

2. For a common emitter configuration, if α and β have their usual meanings, the incorrect relationship between α and β is:

(1)
$$\alpha = \frac{\beta}{1+\beta}$$

(2) $\alpha = \frac{\beta^2}{1+\beta^2}$



$$(3) \frac{1}{\alpha} = \frac{1}{\beta} + 1$$

$$(4) \alpha = \frac{\beta}{1-\beta}$$
Solution: (2, 4)
$$I_E = I_C + I_B;$$

$$\frac{I_E}{I_C} = 1 + \frac{I_B}{I_C}$$

$$\frac{1}{\alpha} = 1 + \frac{1}{\beta}; \frac{1}{\alpha} = \frac{\beta+1}{\beta}$$

$$\alpha = \frac{\beta}{1+\beta}$$

3. A student measures the time period of 100 oscillations of a simple pendulum four times. The data set is 90s, 91s, 95s and 92s. If the minimum division in the measuring clock is 1s, then the reported mean time should be:

1)	92 ± 3	1.8 s
2)	92 <u>+</u> 3	3 s
3)	92 ± 2	2 s
4)	92 + 5	5.0 s

Solution: (3)

Т	T _s	$T_i - T$	$(T_{i} - T)^{2}$		
t ₁	90	-2	4		
t ₂	91	-1	1		
t ₃	95	3	9		
t ₄	92	0	0		
T _i	92	$\Sigma T_i - T_{-0}$	$\frac{\Sigma(T_i - T)^2}{N} = 3.5$		
		$\frac{1}{N} = 0$	$\frac{1}{N} = 3.5$		
$\sum \sum (T_i - T)^2$					
$T_r = T + \left \frac{2(T_i - T_j)^2}{2(T_i - T_j)^2} \right $					

$$T_{\rm r} = T \pm \sqrt{\frac{\Sigma(T_{\rm i} - T)}{N}}$$

 $T_r = 92 \pm \sqrt{3.5}$

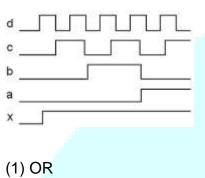
 $T_r = 92 \pm \sqrt{1.8}$

 $T_r = 92 \pm 2$

Because least count of clock is 1s.



4. If a, b, c are inputs to a gate and x is its output, then, as per the following time graph, the gate is:



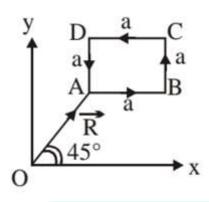
- (2) NAND
- (3) NOT
- (4) AND

Solution: (1)

а	b	С	d	Х		
0	0	0	0	0		
0	0	0	1	1		

When any input is one output is one hence the gate is 'OR' gate.

5. A particle of mass m is moving along the side of a square of side 'a', with a uniform speed v in the x-y plane as shown in the figure:



Which of the following statements is false for the angular momentum \vec{L} about the origin?

(1) $\vec{L} = m\upsilon \left[\frac{R}{\sqrt{2}} + a\right] \hat{k}$ when the particle is moving from B to C. (2) $\vec{L} = \frac{m\upsilon}{\sqrt{2}} R\hat{k}$ when the particle is moving from D to A. (3) $\vec{L} = -\frac{m\upsilon}{\sqrt{2}} R\hat{k}$ when the particle is moving from A to B.



(4) $\vec{L} = m\upsilon \left[\frac{R}{\sqrt{2}} - a\right] \hat{k}$ when the particle is moving from C to D.

Solution: (2, 4)

 $\vec{L} = \vec{r} \times \vec{P} \text{ or } \vec{L} = rp \sin \theta \hat{n}$

Or $\vec{L} = r_{\perp}(P)\hat{n}$

For D to A, $\vec{L} = \frac{R}{\sqrt{2}} mV(-\hat{k})$

For A to B, $\vec{L} = \frac{R}{\sqrt{2}} mV(-\hat{k})$

For C to D, $\vec{L} = \left(\frac{R}{\sqrt{2}} + a\right) mV(\hat{k})$

For B to C, $\vec{L} = \left(\frac{R}{\sqrt{2}} + a\right) mV(\hat{k})$

- 6. Choose the correct statement:
 - (1) In frequency modulation the amplitude of the high frequency carrier wave is made to vary in proportion to the amplitude of the audio signal.
 - (2) In frequency modulation the amplitude of the high frequency carrier wave is made to vary in proportion to the frequency of the audio signal.
 - (3) In amplitude modulation the amplitude of the high frequency carrier wave is made to vary in proportion to the amplitude of the audio signal.
 - (4) In amplitude modulation the frequency of the high frequency carrier wave is made to vary in proportion to the amplitude of the audio signal.

Solution: (3)

As per properties of A.M. in amplitude modulation the amplitude of high frequency carrier wave is made to vary in proportion to the amplitude of the audio signal.

7. Radiation of wavelength λ , is incident on a photocell. The fastest emitted electron has speed v. If the wavelength is changed to $\frac{3\lambda}{4}$, the speed of the fastest emitted electron will be:

$$(1) = v \left(\frac{4}{3}\right)^{\frac{1}{2}}$$
$$(2) = v \left(\frac{3}{4}\right)^{\frac{1}{2}}$$
$$(3) > v \left(\frac{4}{3}\right)^{\frac{1}{2}}$$
$$(4) < v \left(\frac{4}{3}\right)^{\frac{1}{2}}$$



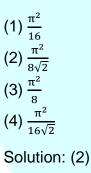
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Solution: (3)

 $\frac{1}{2}mv^2 = \frac{hc}{\lambda} - \phi \qquad \dots (i)$ $\frac{1}{2}mv'^2 = \frac{4}{3}\frac{hc}{\lambda} - \phi$...(ii) From eqn. (i) $\frac{hc}{\lambda} = \frac{1}{2}mv^2 + \phi$ On putting this equ. (ii) $\frac{1}{2}mv'^{2} = \frac{4}{3}\left(\frac{1}{2}mv^{2} + \phi\right) - \phi$

$$v' > v \sqrt{\frac{4}{3}}$$

8. Two identical wires A and B, each of length 'l', carry the same current I. Wire A is bent into a circle of radius R and wire B is bent to form a square of side 'a'. If B_A and B_B are the values of magnetic field at the centres of the circle and square respectively, then the ratio $\frac{B_A}{B_B}$ is :



 $2\pi R = 4a$

$$\frac{a}{R} = \frac{2\pi}{4} \frac{a}{R} = \frac{\pi}{2}$$

 $B_A = \frac{\mu_0 i}{2R}$

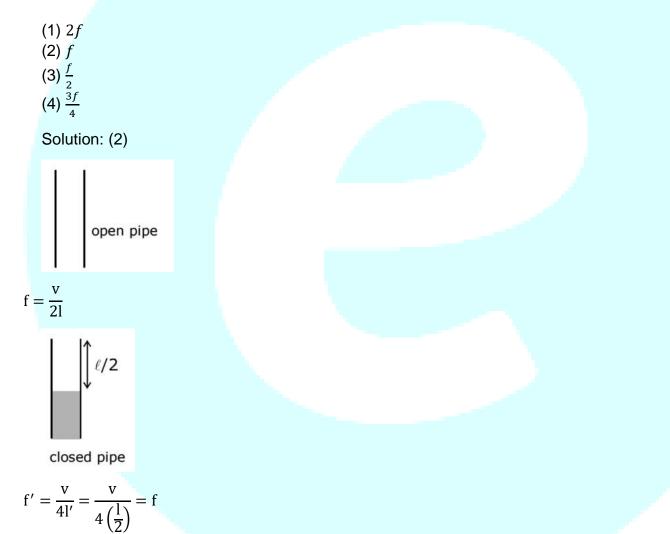


$$B_{\rm B} = \frac{\mu_0 i}{\pi a} \left(2\sqrt{2} \right)$$

 $\frac{B_A}{B_B} = \frac{\mu_0 i}{2R} \times \frac{\pi a}{2\sqrt{2} \mu_0 i}$

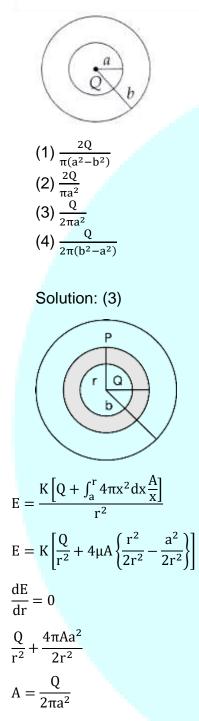
$$=\frac{\pi a}{4\sqrt{2}R}=\frac{\pi}{4\sqrt{2}}\left(\frac{\pi}{2}\right)=\frac{\pi^{2}}{8\sqrt{2}}$$

9. A pipe open at both ends has a fundamental frequency f in air. The pipe is dipped vertically in water so that half of it is in water. The fundamental frequency of the air column is now:



10. The region between two concentric spheres of radii 'a' and 'b', respectively (see figure), has volume charge density $\rho = \frac{A}{r}$, where A is a constant and r is the distance from the centre. At the centre of the spheres is a point charge Q. The value of A such that the electric field in the region between the spheres will be constant, is:





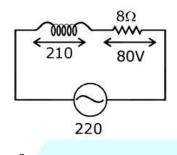
- 11. An arc lamp requires a direct current of 10 A at 80 V to function. If it is connected to a 220 V (rms), 50 Hz AC supply, the series inductor needed for it to work is close to:
 - (1) 0.044 H
 - (2) 0.065 H





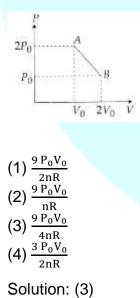
(3) 80 H (4) 0.08 H





 $V_{L}^{2} + 6400 = 220 \times 220$ IR = 80 $V_{L} = \sqrt{48400 - 6400}$ I = $\frac{80}{8} = 10 = \sqrt{42000} = 210$ I X_L = 210 X_L = 2πfL = 210 210

- $L = \frac{210}{10 \times 100 \ \pi} = 0.065 \ H$
- 12. 'n' moles of an ideal gas undergoes a process $A \rightarrow B$ as shown in the figure. The maximum temperature of the gas during the process will be:





 $T_{\mbox{max}}$ at mid point

$$T = \frac{pv}{nR} = \frac{\left(\frac{3}{2}P_0\right)\left(\frac{3V_0}{2}\right)}{nR}$$
$$= \frac{9}{4}\left(\frac{P_0V_0}{nR}\right)$$

13. A person trying to lose weight by burning fat lifts a mass of 10 kg upto a height of 1m 1000 times. Assume that the potential energy lost each time he lowers the mass is dissipated. How much fat will he use up considering the work done only when the weight is lifted up? Fat supplies 3.8×10^7 J of energy per kg which is converted to mechanical energy with a 20% efficiency rate. Take g = 9.8 ms^{-2} :

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(1) 9.89 \times 10^{-3} kg

(2) 12.89 \times 10^{-3} kg

(3) 2.45 \times 10^{-3} kg

(4) 6.45 \times 10^{-3} kg

Solution: (2)

m = 10kg, h = 1m, 1000 times

PE = 98 J \times 1000 = 98000 J = 98 kJ

= 9.8 \times 10^4 J

Fat burn = 3.8 \times 10^7 J \times 0.2

= 7.6 \times 10^6 J per kg

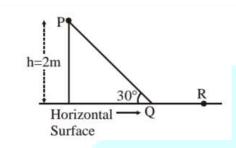
m = \frac{9.8 \times 10^4}{7.6 \times 10^6} = 1.289 \times 10^{-2}

= 12.89 \times 10^{-3} kg
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14. A point particle of mass m, moves along the uniformly rough track PQR as shown in the figure. The coefficient of friction, between the particle and the rough track equals μ. The particle is released, from rest, from the point P and it comes to rest at a point R. The energies, lost by the ball, over the parts, PQ and QR, of the track, are equal to each other, and no energy is lost when particle changes direction from PQ to QR.

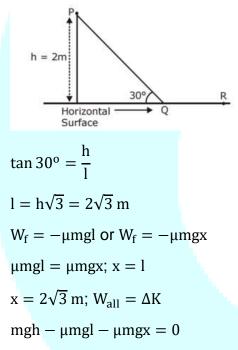
The values of the coefficient of friction μ and the distance x = (QR), are respectively close to:





(1) 0.29 and 3.5 m
(2) 0.29 and 6.5 m
(3) 0.2 and 6.5 m
(4) 0.2 and 3.5 m

Solution: (1)



$$h - \mu l - \mu x = 0$$

$$2 = \mu(l+x) \Rightarrow \mu = \frac{2}{l+x} = \frac{2}{4\sqrt{3}} = \frac{1}{2\sqrt{3}}$$

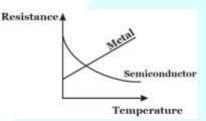
- 15. The temperature dependence of resistance of Cu and undoped Si in the temperature range 300-400 K, is best described by:
 - (1) Linear increase for Cu, exponential decrease for Si.
 - (2) Linear decrease for Cu, linear decrease for Si.
 - (3) Linear increase for Cu, linear increase for Si.



(4) Linear increase for Cu, exponential increase for Si.

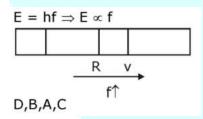
Solution: (1)

Resistance variation with temperature: Cu-metal, undoped Silicon-Semi Conductor resistance of metal increases with increase in temperature linearly resistance of semi Conductor decreases exponentially with increase in temperature.



16. Arrange the following electromagnetic radiations per quantum in the order of increasing energy:

- A: Blue light
- **B: Yellow light**
- C: X-ray
- D: Radiowave
- (1) C, A, B, D
- (2) B, A, D, C
- (3) D, B, A, C (4) A, B, D, C
- Solution: (3)



- 17. A galvanometer having a coil resistance of 100Ω gives a full scale deflection, when a current of 1 mA is passed through it. The value of the resistance, which can convert this galvanometer into ammeter giving a full scale deflection for a current of 10 A, is:
 - (1) 0.1 Ω
 - (2) 3 Ω
 - (3) 0.01 Ω



(4) 2 Ω

Solution: (3)

We know that

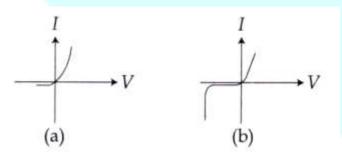
$$R_{S} = \frac{I_{G}}{1 - I_{G}} R_{G}$$
$$= \frac{1 \times 10^{-3}}{10} \times 100$$

= 0.01 Ω

18. Half-lives of two radioactive elements A and B are 20 minutes and 40 minutes, respectively. Initially, the samples have equal number of nuclei. After 80 minutes, the ratio of decayed numbers of A and B nuclei will be:

(1) 1 : 4 (2) 5 : 4 (3) 1 : 16 (4) 4 : 1 Solution: (2) t = 80 min = 4 T_A = 2T_B no. of nuclei of A decayed = $N_0 - \frac{N_0}{2^4} = \frac{15N_0}{16}$ no. of nuclei of B decayed = $N_0 - \frac{N_0}{2^2} = \frac{3N_0}{4}$ required ratio = $\frac{5}{4}$

19. Identify the semiconductor devices whose characteristics are given below, in the order (a), (b), (c), (d):



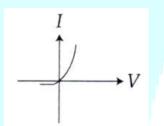


(1) Solar cell, Light dependent resistance, Zener diode, Simple diode

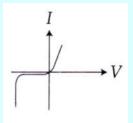
(2) Zener diode, Solar cell, Simple diode Light dependent resistance(3) Simple diode, Zener diode, Solar cell, Light dependent resistance

(4) Zener diode, Simple diode, Light dependent resistance, Solar cell

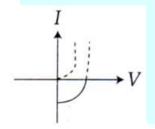
Solution: (3)



Its V-I characteristics of simple diode.



Its V-I characteristic of Zener diode.

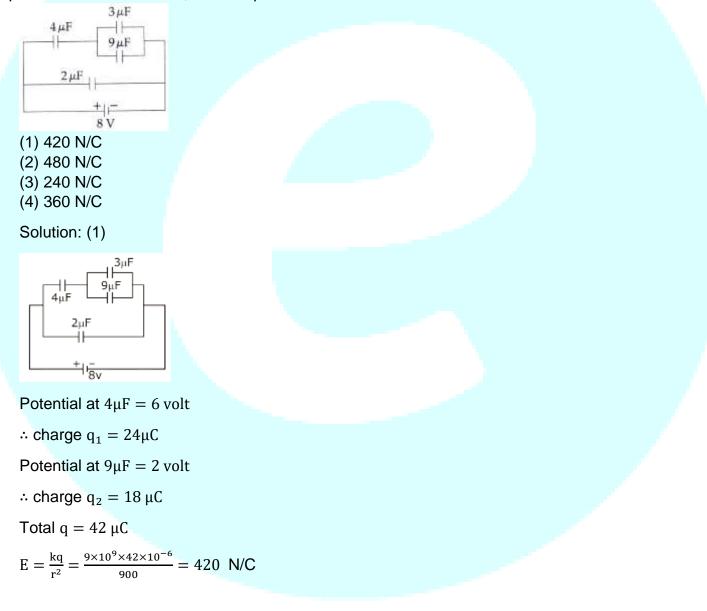


V-I characteristics of Solar cell



V-I characteristics of light dependence resistance.

20. A combination of capacitors is set up as shown in the figure. The magnitude of the electric field, due to a point charge Q (having a charge equal to the sum of the charges on the 4 μ F and 9 μ F capacitors), at a point distant 30 m from it, would equal:





21. A satellite is revolving in a circular orbit at a height 'h' from the earth's surface (radius of earth R; h<<R). The minimum increase in its orbital velocity required, so that the satellite could escape from the earth's gravitational field, is close to: (Neglect the effect of atmosphere.)

(1)
$$\sqrt{\frac{gR}{2}}$$

(2) $\sqrt{gR} (\sqrt{2} - 1)$
(3) $\sqrt{2 gR}$
(4) \sqrt{gR}
Solution: (2)
Since h<V_0 = \sqrt{2gR}
& $V_e = \sqrt{gR}$
 \therefore min velocity required
 $V_0 - V_e = \sqrt{2gR} - \sqrt{gR}$

$$V_0 - V_e = \sqrt{2gR} - \sqrt{gR}$$

$$=(\sqrt{2}-1)\sqrt{gR}$$

22. A screw gauge with a pitch of 0.5 mm and a circular scale with 50 divisions is used to measure the thickness of a thin sheet of Aluminium. Before starting the measurement, it is found that when the two jaws of the screw gauge are brought in contact, the 45th division coincides with the main scale line and that the zero of the main scale is barely visible. What is the thickness of the sheet if the main scale reading is 0.5 mm and the 25th division coincides with the main scale line?

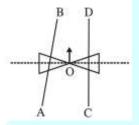
(1) 0.70 mm (2) 0.50 mm (3) 0.75 mm (4) 0.80 mm Solution: (4) $LC = \frac{0.5}{50} = 0.01 \text{ mm}$ Zero error = 0.50 - 0.45 = -0.05Thickness = $(0.5 + 25 \times 0.01) + 0.05$ = 0.5 + 0.25 + 0.05



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= 0.8 mm

23. A roller is made by joining together two cones at their vertices O. It is kept on two rails AB and CD which are placed asymmetrically (see figure), with its axis perpendicular to CD and its centre O at the centre of line joining AB and CD (see figure). It is given a light push so that it starts rolling with its centre O moving parallel to CD in the direction shown. As it moves, the roller will tend to:



(1) go straight.
 (2) turn left right alternately.
 (3) turn left.

(4) turn right.

Solution: (3)

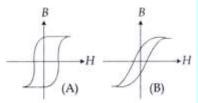
Say the distance of central line from instantaneous axis of rotation is r.

Then r from the point on left becomes lesser than that for right.

So V_{left} point = $\omega r' < \omega r = v_{right}$ point

So the roller will turn to left.

24. Hysteresis loops for two magnetic materials A and B are given below:



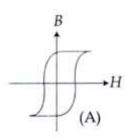
These materials are used to make magnets for electric generators, transformer core and electromagnet core. Then it is proper to use:

(1) A for transformers and B for electric generators.

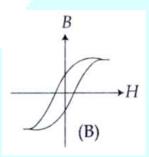
- (2) B for electromagnets and transformers.
- (3) A for electric generators and transformers.
- (4) A for electromagnets and B for electric generators.



Solution: (2)



Graph A is hard ferromagnetic material substance.



The graph of B is graph of soft ferromagnetic material which is we use to consist of electromagnets and transformers.

25. The box of a pin hole camera, of length L has a hole of radius a. It is assumed that when the hole is illuminated by a parallel beam of light of wavelength λ the spread of the spot (obtained on the opposite wall of the camera) is the sum of its geometrical spread and the spread due to diffraction. The spot would then have its minimum size (say b_{min}) when:

(1)
$$a = \sqrt{\lambda L}$$
 and $b_{\min} = \sqrt{4\lambda L}$
(2) $a = \frac{\lambda^2}{L}$ and $b_{\min} = \sqrt{4\lambda L}$
(3) $a = \frac{\lambda^2}{L}$ and $b_{\min} = \left(\frac{2\lambda^2}{L}\right)$
(4) $a = \sqrt{\lambda L}$ and $b_{\min} = \left(\frac{2\lambda^2}{L}\right)$

Solution: (1)

The diffraction angle λa cause a spreading of $\frac{L\lambda}{a}$ in the size of the spot. These become large when a (Radius) is small.

So adding of two kind of spreading (for simplicity) we get spot size is

$$a + \frac{La}{a}$$
.

Hence to find out minimum value of this







We can write it as $\sqrt{\left(a-\frac{L\lambda}{a}\right)^2+4L\lambda}$

: The minimum value is when $a = \frac{La}{a}$ i.e. the geometric and diffraction broadening are equal $\sqrt{4L\lambda}$

 \therefore When $a=\sqrt{\lambda L}$ and $b_{\min}=\sqrt{4\lambda L}$

26. A uniform string of length 20m is suspended from a rigid support. A short wave pulse is introduced at its lowest end. It starts moving up the string. The time taken to reach the support is:

 $(take g = 10 ms^{-2})$

- (1) $2\sqrt{2} s$ (2) $\sqrt{2} s$ (3) $2\pi\sqrt{2} s$ (4) 2sSolution: (1) $t = 2\sqrt{\frac{l}{g}} = 2\sqrt{2}$ second.
- 27. An ideal gas undergoes a quasi static, reversible process in which its molar heat capacity C remains constant. If during this process the relation of pressure P and volume V is given by $PV^n = constant$, then n is given by (Here C_P and C_V are molar specific heat at constant pressure and constant volume, respectively) :

(1)
$$n = \frac{C_P - C_V}{C - C_V}$$

(2)
$$n = \frac{C - C_V}{C - C_P}$$

(3)
$$n = \frac{C_P}{C_V}$$

(4)
$$n = \frac{C - C_P}{C - C_V}$$

Solution: (4)

$$PV^n = k$$

$$C = C_v + \frac{R}{1 - n}; C - C_v = \frac{R}{1 - n}$$

$$1 - n = \frac{R}{C - C_v}; n = 1 - \frac{R}{C - C_v}$$

$$n = \frac{C - C_v - R}{C - C_v}; n = \frac{C - C_v - (C_P - C_v)}{C - C_v}$$



$$n = \frac{C - C_v - C_p + C_v}{C - C_v}; n = \frac{C - C_p}{C - C_v}$$

- 28. An observer looks at a distant tree of height 10m with a telescope of magnifying power of 20. To the observer the tree appears:
 - (A) 20 times taller.
 - (B) 20 times nearer.
 - (C) 10 times taller.
 - (D) 10 times nearer.

Solution: (1)

$$\theta = \frac{10}{x}$$

$$\theta_1 = \frac{10}{x} (20)$$

Now 20 times taller.

29. In an experiment for determination of refractive index of glass of a prism by $i = \delta$, plot, it was found that a ray incident at angle 35°, suffers a deviation of 40° and that it emerges at angle 79°. In that case which of the following is closest to the maximum possible value of the refractive index?

(1) 1.7 (2) 1.8 (3) 1.5 (4) 1.6 Solution: (3) $i = 35^{\circ}, \delta = 40^{\circ}, e = 79^{\circ}$ $\delta = i + e - A$ $40^{\circ} = 35^{\circ} + 79^{\circ} - A$ $A = 74^{\circ}$ And $r_1 + r_2 = A = 74^{\circ}$ Solving these, we get $\mu = 1.5$ Since $\delta_{\min} < 40^{\circ}$



$$\mu < \frac{\sin\left(\frac{74+40}{2}\right)}{\sin 37}$$

 $\mu_{max} = 1.44$

30. A pendulum clock loses 12s a day if the temperature is 40° C and gains 4s a day if the temperature is 20° C. The temperature at which the clock will show correct time, and the co-efficient of linear expansion (α) of the metal of the pendulum shaft are respectively:

(1) 30° C; $\alpha = 1.85 \times 10^{-3}/{}^{\circ}$ C (2) 55° C; $\alpha = 1.85 \times 10^{-2}/{}^{\circ}$ C (3) 25° C; $\alpha = 1.85 \times 10^{-5}/{}^{\circ}$ C (4) 60° C; $\alpha = 1.85 \times 10^{-4}/{}^{\circ}$ C Solution: (3) $\Delta T \propto \Delta \theta$ $\frac{12}{4} = \frac{40 - \theta}{\theta - 20}$ $3\theta - 60 = 40 - \theta$ $4\theta = 100$ $\theta = 25^{\circ}$ C $\Delta T = \frac{1}{2} \alpha \Delta \theta \times T$ $4 = \frac{1}{2} \alpha 5 \times 86400$; $\frac{8 \times 10^{5}}{5 \times 86400} = \alpha$; $\frac{8000}{4320} = \alpha$

 $\alpha = 1.05 \times 10^{-5}$ °C







MATHEMATICS

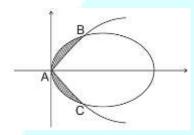
31. The area (in sq. units) of the region $\{(x, y): y^2 \ge 2x \text{ and } x^2 + y^2 \le 4x, x \ge 0, y \ge 0\}$ is:

(1) $\pi - \frac{4\sqrt{2}}{3}$ (2) $\frac{\pi}{2} - \frac{2\sqrt{2}}{3}$ (3) $\pi - \frac{4}{3}$ (4) $\pi - \frac{8}{3}$

Solution: (4)

 $y^2 = 2x$ (Area out side the parabola)

 $x^2 + y^2 \le 4x$ (Area inside the circle)



First finding point of intersection of the curves

$$x^{2} + y^{2} = 4x$$
 and $y^{2} = 2x$
 $x^{2} + 2x = 4x$
 $x^{2} = 2x$
 $x = 0, x = 2$
If $x = 0$, then $y = 0$ and if x

Co – ordinates of A(0,0) and B(2,2)

As $x \ge 0$ $y \ge 0$ only area above x - axis would be considered

= 2, then $y = \pm 2$.

$$= \left[\int_{0}^{2} \sqrt{4x - x^{2}} \, dx - \sqrt{2} \int_{0}^{2} \sqrt{x} \, dx\right]$$
$$= \left[\int_{0}^{2} \sqrt{4 - (x - 2)^{2}} \, dx - \sqrt{2} \int_{0}^{2} \sqrt{x} \, dx\right]$$
$$= \left[\left(\frac{2 - x}{2}\right) \sqrt{4x - x^{2}} + \frac{4}{2} \cdot \sin^{-1}\left(\frac{x - 2}{2}\right)\right]_{0}^{2} - \sqrt{2} \left(\frac{x^{\frac{3}{2}}}{\frac{3}{2}}\right)_{0}^{2}$$



$$= [0 - 2\sin^{-1}(-1)] - \sqrt{2} \cdot \frac{2}{3} 2\sqrt{2}]$$

$$\left[\pi - \frac{8}{3}\right]$$

32. If
$$f(x) + 2f\left(\frac{1}{x}\right) = 3x, x \neq 0$$
, and $S = \{x \in R : f(x) = f(-x)\}$; then S:

- (1) Contains exactly two elements
- (2) Contains more than two elements
- (3) Is an empty set
- (4) Contains exactly one element

Solution: (1)

$$f(x) + 2 \cdot f\left(\frac{1}{x}\right) = 3x$$
(i)

Replace x by $\frac{1}{x}$

$$f\left(\frac{1}{x}\right) + 2f(x) = \frac{3}{x} \qquad \dots \dots \dots (ii)$$

$$3f(x) = \frac{6}{x} - 3x$$

$$f(x) = \frac{2}{x} - x$$

$$\therefore \quad f(x) = f(-x)$$

Therefore $\frac{2}{x} - x = -\frac{2}{x} + x$

$$\frac{4}{x} = 2x$$

 $2 = x^{2}$

 $x = \pm \sqrt{2}$

Contains exactly two elements

33. The integral $\int \frac{2x^{12}+5x^9}{(x^5+x^3+1)^3} dx$ is equal to:





where C is an arbitrary constant.

(1)
$$\frac{x^5}{2(x^5+x^3+1)^2} + C$$

(2) $\frac{-x^{10}}{2(x^5+x^3+1)^2} + C$
(3) $\frac{-x^5}{(x^5+x^3+1)^2} + C$
(4) $\frac{x^{10}}{2(x^5+x^3+1)^2} + C$
Solution: (4)
 $\int \frac{2x^{12}+5x^9}{(x^5+x^3+1)^3} dx$

$$\int \frac{(2x^{12} + 5 + 9) dx}{x^{15} \left(1 + \frac{1}{x^2} + \frac{1}{x^5}\right)^3}$$

$$\int \frac{\left(\frac{2}{x^3} + \frac{5}{x^6}\right) dx}{\left(1 + \frac{1}{x^2} + \frac{1}{x^5}\right)^3}$$
Let $1 + \frac{1}{x^2} + \frac{1}{x^5} = t$

$$\left(-\frac{2}{x^3} - \frac{5}{x^6}\right) dx = dt$$

$$\left(\frac{2}{x^3} + \frac{5}{x^6}\right) dx = -dt$$

$$-\int \frac{dt}{t^3} = -\left(\frac{1}{(-2)t^2}\right) = \frac{1}{2 \cdot t^2}$$

$$= \frac{1}{2} \frac{1}{\left(1 + \frac{1}{x^2} + \frac{1}{x^5}\right)^2} + C = \frac{1}{2} \frac{x^{10}}{(x^5 + x^3 + 1)^2} + C$$

$$= \frac{x^{10}}{2(x^5 + x^3 + 1)^2} + C$$

34. For $x \in R$, $f(x) = |\log 2 - \sin x|$ and g(x) = f(f(x)), then:







- (1) $g'(0) = -\cos(\log 2)$
- (2) g is differentiable at x = 0 and $g'(0) = -\sin(\log 2)$
- (3) g is not differentiable at x = 0
- (4) $g'(0) = \cos(\log 2)$

Solution: (4)

In the neighborhood of $x = 0, f(x) = \log 2 - \sin x$

$$\therefore \qquad g(x) = f(f(x)) = \log 2 - \sin(f(x))$$

 $= \log 2 - son \left(\log 2 - \sin x \right)$

It is differentiable at x = 0, so

$$\therefore \qquad g'(x) = -\cos(\log 2 - \sin x) \ (-\cos x)$$

$$\therefore$$
 $g'(0) = \cos(\log 2)$

35. The centres of those circles which touch the circle, $x^2 + y^2 - 8x - 8y - 4 = 0$, externally and also touch the x – axis, lie on :

- (1) A hyperbola (2) A parabola
- (3) A circle (4) An ellipse which is not a circle

Solution: (2)

$$x^2 + y^2 - 8x - 8y - 4 = 0$$

has centre (4, 4) and radius 6.

Let (h, k) be the centre of the circle which is touching the circle externally

Then

 $\sqrt{(h-4)^{2} + (k-4)^{2}} = 6 + k$ $h^{2} - 8h + 16 + k^{2} - 8k + 16 = 36 + 12k + k^{2}$ $h^{2} - 8h - 20k - 4 = 0,$ Replacing *h* by *x* and *k* by *y* $x^{2} - 8x - 20y - 4 = 0$ Equation of parabola.



36. The sum of all real values of x satisfying the equation $(x^2 - 5x + 5)^{x^2+4x-60} = 1$ is:

(4) - 4 (1) 6 (2) 5 (3) 3 Solution: (3) $(x^2 - 5x + 5)^{x^2 + 4x - 60} = 1$ $(x^2 - 5x + 5)^{(x+10)(x-6)} = 1$ x = -10 and x = 6 will make L.H.S = 1. Also at x = 1; $(1)^{11.(-5)} = 1$ And at x = 4; $(1)^{14.(-2)} = 1$ We should also considered the case when $x^2 - 5x + 5 = -1$, and it has even power $x^2 - 5x + 6 = 0$ (x-2)(x-3) = 0So x = 2 will give = $(-1)^{even}$ At x = 2 $(-1)^{12(-4)} = 1$ So sum would be -10 + 6 + 1 + 4 + 2 = 3Hence answer is 3

37. If the 2nd, 5th and 9th term of a non – constant A.P. are in G.P., then the common ratio of this G.P. is:

(1) 1 (2)
$$\frac{7}{4}$$
 (3) $\frac{8}{5}$ (4) $\frac{4}{3}$
Solution: (4)
Let the A.P. be a, a + d, a + 2d,.....
Given $(a + d)$. $(a + 8d) = (a + 4d)^2$
 $a^2 + 9ad + 8d^2 = a^2 + 8ad + 16d^2$
 $8d^2 - ad = 0$



d[8d - a] = 0 $\therefore \quad d \neq 0$ $d = \frac{a}{8}$ So, 2^{nd} term 5^{th} term 9^{th} term Would be $\left(a + \frac{a}{8}\right)$ $\left(a + \frac{a}{2}\right)$ (a + a) $\frac{9a}{8}$ $\frac{3a}{2}$ 2aCommon Ratio : $\frac{2^{nd} term}{1^{st} term} = \frac{3a}{2.9a} \cdot 8 = \frac{4}{3}$

38. The eccentricity of the hyperbola whose length of the latus rectum is equal to 8 and the length of its conjugate axis is equal to half of the distance between its foci, is :

(4) $\frac{4}{\sqrt{3}}$

(1)
$$\frac{2}{\sqrt{3}}$$
 (2) $\sqrt{3}$ (3) $\frac{4}{3}$
Solution: (1)
 $\frac{2b^2}{a} = 8$...(i)
 $2b = \frac{1}{2} 2ae$ (ii)
 $\frac{b}{a} = \frac{e}{2}$
From (ii)
Now, $e = \sqrt{1 + \frac{b^2}{a^2}} = \sqrt{1 + \frac{e^2}{4}}$
 $e^2 = 1 + \frac{e^2}{4}$
 $\frac{3}{4}e^2 = 1$
 $e^2 = \frac{4}{3} = 1$
 $e = \frac{2}{\sqrt{3}}$



39. If the number of terms in the expansion of $\left(a - \frac{2}{x} + \frac{4}{y^2}\right)^n$, $x \neq 0$, is 28, then the sum of the coefficients of all the terms in this expansion, is :

(1) 243 (2) 729 (3) 64 (4) 2187

Solution: (2)

 $\left(a - \frac{2}{x} + \frac{4}{y^2}\right)^n$ as the question is having three variables the total number of terms would be

 $\frac{(n+1)(n+2)}{12}$ which is equal to 28

(n+1)(n+2) = 56

Which gives n = 6, and sum of coefficients would be $(1 - 2 + 4)^6 = 3^6 = 729$.

40. The Boolean Expression $(p \land \sim q) \lor q \lor (\sim p \land q)$ is equivalent to :

(1) $p \lor q$ (2) $p \lor q$ (3) $\sim p \land q$ (4) $p \land q$ Solution: (1) $(p \land \sim q) \lor q \lor (\sim p \land q)$ Set equivalent $= (A \cap \overline{B}) \cup (\overline{A} \cap B) \cup B$ $= ((A \cup B) - (A \cap B) \cup B$

$$= A \cup B$$

Hence answer is $p \lor q$.

41. Consider $f(x) = \tan^{-1}\left(\sqrt{\frac{1+\sin x}{1-\sin x}}\right)$, $x \in \left(0, \frac{\pi}{2}\right)$. A normal to y = f(x) at $x = \frac{\pi}{6}$ also passes through the point :

(1)
$$\left(\frac{\pi}{6}, 0\right)$$
 (2) $\left(\frac{\pi}{4}, 0\right)$ (3) (0,0) (4) $\left(0, \frac{2\pi}{3}\right)$

Solution: (4)

$$f(x) = \tan^{-1}\left(\sqrt{\frac{1+\sin x}{1-\sin x}}\right), x \in \left(0, \frac{\pi}{2}\right)$$







$$f'(x) = \frac{1}{1 + \left(\frac{1+\sin x}{1-\sin x}\right)} \cdot \frac{1}{2} \left(\frac{1+\sin x}{1-\sin x}\right)^{-\frac{1}{2}} \cdot \left(\frac{\cos x(1-\sin x) + \cos(1+\sin x)}{(1-\sin x)^2}\right) \text{ at } x = \frac{\pi}{2}$$

$$f'(x) = \frac{1}{2} \cdot \frac{1}{2} \left(\frac{1}{\sqrt{3}}\right) \left(\frac{\sqrt{3}}{\frac{1}{4}}\right) = \frac{1}{2}$$
Slope of tangent = $\frac{1}{2}$
So slope of normal = -2
Also at $x = \frac{\pi}{6}$ $y = \tan^{-1}\sqrt{3} = \frac{\pi}{3}$.
So equation of the tangent would be $\left(y - \frac{\pi}{3}\right) = -2 \left(x - \frac{\pi}{6}\right)$
It passes through $\left(0, \frac{2\pi}{3}\right)$
42. $\lim_{n \to \infty} \left(\frac{n+1}{n^{2n}}, \frac{(n+2)\dots 3n}{n^{2n}}\right)^{\frac{1}{n}}$ is equal to :
$$(1) \frac{9}{e^2} \qquad (2) \ 3 \log 3 - 2 \qquad (3) \ \frac{18}{e^4} \qquad (4) \ \frac{27}{e^2}$$
Solution: (4)
 $\lim_{n \to \infty} \left(\frac{(n+1) \ (n+2)\dots 3n}{n^{2n}}\right)^{\frac{1}{n}}$
Let $y = \left(\frac{(n+1) \ (n+2)\dots (2n+n)}{n^{2n}}\right)^{\frac{1}{n}}$
 $y = \left(\frac{(n+1) \ (n+2) \dots (2n+n)}{n} \right)^{\frac{1}{n}}$
 $\log y = \frac{1}{n} \left[\log\left(1 + \frac{1}{n}\right) + \log\left(1 + \frac{2}{n}\right) + \dots \log(1+2)\right]$
As $n \to \infty$
 $\log y = \int_{0}^{2} \log(1+x) \ dx$

Integrating by parts



$$\log y = \int_{0}^{2} 1.\log(1+x) \ dx$$

$$= (x \cdot \log(1+x))_{0}^{2} - \int_{0}^{2} \frac{1}{1+x} x$$

$$= (x \log(1+x))_{0}^{2} - \int_{0}^{2} \left(\frac{1+x}{1+x}\right) + \int_{0}^{2} \frac{1}{1+x}$$

$$= (x \log(1+x))_{0}^{2} - (x)_{0}^{2} + (\log(1+x))_{0}^{2}$$

$$= (2 \log 3 - 0) - (2 - 0) + (\log 3 - \log 1)$$

$$= 3 \log 3 - 2$$
Since $\log y = 3 \log 3 - 2$

$$= y = \frac{e^{\log 27}}{e^{2}} = \frac{27}{e^{2}}$$

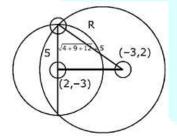
$$= \frac{27}{e^{2}}$$

43. If one of the diameters of the circle, given by the equation, $x^2 + y^2 - 4x + 6y - 12 = 0$, is a chord of a circle S, whose centre is at (-3, 2), then the radius of S is:

(1) 5 (2) 10 (3) $5\sqrt{2}$ (4) $5\sqrt{3}$

Solution: (4)

The centre of the given circle $x^2 + y^2 - 4x + 6y - 12 = 0$ is (2, -3) and the radius is 5.



The distance between the centres $5\sqrt{2}$ and radius is 5. The triangle OPQ is a right angled triangle

$$OQ = \sqrt{(5\sqrt{2})^2 + 5^2} = \sqrt{(5\sqrt{3})^2} = 5\sqrt{3}$$



Hence answer is $5\sqrt{3}$

44. Let two fair six – faced dice A and B be thrown simultaneously. If E_1 is the event that die A shows up four, E_2 is the event that die B shows up two and E_3 is the event that the sum of numbers on both dice is odd, then which of the following statement is NOT true ?

- (1) E_1 and E_3 are independent
- (2) E_1, E_2 and E_3 are independent
- (3) E_1 and E_2 are independent
- (4) E_2 and E_3 are independent

Solution: (2)

 $E_1 \rightarrow A$ show up 4

 $E_2 \rightarrow B$ shows up 2

 $E_3 \rightarrow$ Sum is odd (i.e., even + odd or odd + even)

$$P(E_1) = \frac{6}{6.6} = \frac{1}{6}$$
$$P(E_2) = \frac{6}{6.6} = \frac{1}{6}$$
$$3 \times 3 \times 2$$

$$P(E_3) = \frac{1}{6.6} = \frac{1}{2}$$

$$P(E_1 \cap E_2) = \frac{1}{6.6} = P(E_1) \cdot P(E_2)$$

1

 \Rightarrow E_1 and E_2 are independent

$$P(E_1 \cap E_3) = \frac{1.3}{6.6} = P(E_1) \cdot P(E_3)$$

 \Rightarrow E_1 and E_2 are independent

$$P(E_2 \cap E_3) = \frac{1.3}{6.6} = \frac{1}{12} = P(E_2) \cdot P(E_3)$$

 \Rightarrow $E_2 and E_3$ are independent

 $P(E_1 \cap E_2 \cap E_3) = 0$ i.e., impossible event.





- 45. A value of θ for which $\frac{2+3i\sin\theta}{1-2i\sin\theta}$ is purely imaginary, is :
- (1) $\sin^{-1}\left(\frac{\sqrt{3}}{4}\right)$ (2) $\sin^{-1}\left(\frac{1}{\sqrt{3}}\right)$

(3)
$$\frac{\pi}{3}$$

(4) $\frac{\pi}{6}$

Solution: (2)

Let $z = \frac{2+3i\sin\theta}{1-2i\sin\theta}$

Rationalizing the complex number.

$$\frac{(2+3i\sin\theta)(1+2i\sin\theta)}{1+4\sin^2\theta} = \frac{(2-6\sin^2\theta)+i(7\sin\theta)}{1+4\sin^2\theta}$$

To make it purely imaginary. It real part should be 'O'.

Hence $2 = 6 \sin^2 \theta$

$$\sin \theta = \frac{1}{\sqrt{3}}$$
$$\sin^{-1}\left(\frac{1}{\sqrt{3}}\right)$$

46. If the sum of the first ten terms of the series $\left(1\frac{3}{5}\right)^2 + \left(2\frac{2}{5}\right)^2 + \left(3\frac{1}{5}\right)^2 + 4^2 + \left(4\frac{4}{5}\right)^2 + \cdots$, is $\frac{16}{5}m$, then m is equal to :

(1) 100 (2) 99 (3) 102 (4) 101

Solution: (4)

$$\left(\frac{8}{5}\right)^{2} + \left(\frac{12}{5}\right)^{2} + \left(\frac{16}{5}\right)^{2} \dots \dots 10 \text{ terms}$$
$$T_{n} = \left(\frac{4n+4}{5}\right)^{2}$$
$$T_{n} = 16\left(\frac{n^{2}+2n+1}{25}\right)$$
$$T_{n} = \frac{16}{25}(4^{2}+2n+1)$$





$$T_n = S_n = \left(\frac{16}{25}\right) \left(\frac{n(n+1)(2n+1)}{6} + \frac{2(n)(n+1)+4}{2}\right)$$

Put $n = 10$
$$\frac{16}{25} \left(\frac{10.11.21}{6}\right) + \frac{2.10.11}{2} + 10$$

$$= \frac{16}{25} (385 + 110 + 10) = \frac{16}{25} .505$$

$$= \frac{16}{5} 101.$$

Hence m = 101

47. The system of linear equations

 $x + \lambda y - z = 0$

 $\lambda x - y - z = 0$

$$x + y - \lambda z = 0$$

Has a non -trivial solution for :

- (1) Exactly two values of λ
- (2) Exactly three values of λ
- (3) Infinitely many values of λ
- (4) Exactly one value of λ

Solution: (2)

For non – trivial solution.

$$\Delta = \begin{vmatrix} 1 & \lambda & -1 \\ \lambda & -1 & -1 \\ 1 & 1 & -\lambda \end{vmatrix} = 0$$

$$1(\lambda + 1) - \lambda(-\lambda^2 + 1) - 1(\lambda + 1) = 0$$

$$(\lambda + 1) - \lambda(1 - \lambda) (1 + \lambda) - (\lambda + 1) = 0$$

$$\lambda(1 - \lambda) (1 + \lambda) = 0$$

$$\lambda = 0, \lambda = 1, \lambda = -1$$



G

Exactly there value of λ .

48. If the line, $\frac{x-3}{2} = \frac{y+2}{-1} = \frac{z+4}{3}$ lies in the plane, lx + my - z = 9, then $l^2 + m^2$ is equal to : (1) 5 (2) 2 (3) 26 (4) 18 Solution: (2) $\frac{x-3}{2} = \frac{y+2}{-1} = \frac{z+4}{2}$ lies in lx + my - z = 9The point (3, -2, -4) lies as the plane. So it should satisfy the equation of the plane. 3l - 2m + 4 = 93l - 2m = 5(i) The direction ratio 2, -1, 3 should be perpendicular to the line 2(l) - 1.(m) - 3 = 02l - m = 3(ii) l = 1 and m = -1 $l^2 + m^2 = 1 + 1 = 2$ *.*.. Hence Option [2] is correct

49. If all the words (with or without meaning) having five letters, formed using the letters of the word SMALL and arranged as in a dictionary; then the position of the word SMALL is :

(1) 52^{nd} (2) 58^{th} (3) 46^{th} (4) 59^{th}

Solution: (2)

SMALL

Total number of words formed would be $\frac{L5}{L2} = 60$

When arranged as per dictionary. The words starting from A

$$A - - - - \frac{\mathbf{L4}}{\mathbf{L2}} = 12$$

The words standing from L

 $L - - - - = \bot 4 = 24$



The words starting form M

$$M - - - - = \frac{\lfloor 4}{\lfloor 2} = 12$$

The words starting from

$$SA - - - = \frac{L3}{L2} = 3$$
$$SL - - - L3 = 6$$

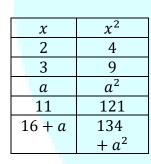
SMALL = 1

Rank would be 12 + 24 + 12 + 3 + 6 + 1 = 58

50. If the standard deviation of the numbers 2, 3, a and 11 is 3.5, then which of the following is true ?

- (1) $3a^2 34a + 91 = 0$ (3) $3a^2 - 26a + 55 = 0$
- (2) $3a^2 23a + 44 = 0$ (4) $3a^2 - 32a + 84 = 0$

Solution: (4)



$$\sqrt{\frac{\sum x^2}{4}} - \left(\frac{\sum x_i}{4}\right)^2$$

$$\sqrt{\frac{134+a^2}{4} - \left(\frac{16+a}{4}\right)^2} = \frac{35}{10}$$
$$\frac{1}{2}\sqrt{134+a^2 - \frac{(16+a)^2}{4}} = \frac{7}{2}$$



 $\sqrt{536 + 4a^2 - 256 - a^2 - 32a} = 7$

51. A wire of length 2 units is cut into two parts which are bent respectively to form a square of side = x units and a circle of radius = r units. If the sum of the areas of the square and the circle so formed is minimum, then:

(1) $x = 2r$ (2) $2x =$ Solution: (1)	r (3) $2x = (\pi + 4)r$	$(4) (4-\pi)x = \pi r$	
x Square x	r		
Given that $4x + 2\pi r = 2$			
i.e., $2x + \pi r = 1$			
$\therefore \qquad r = \frac{1-2x}{\pi} \qquad \dots$	(i)		
Area $A = x^2 + \pi x^2$			
$= x^2 + \frac{1}{\pi} (2x - 1)^2$			
For min vale of area A			
$\frac{dA}{dx} = 0$ given $x = \frac{2}{\pi + 4}$	(ii)		
From (i) and (ii)			
$r=rac{1}{\pi+4}$	(iii)		
\therefore $x = 2r$			
52 let $n = \lim_{n \to \infty} (1 + \tan^2 \sqrt{x})$	$\frac{1}{2x}$ then log p is equal to :		

52. Let $p = \lim_{x \to 0+} (1 + \tan^2 \sqrt{x})^{\frac{1}{2x}}$, then log p is equal to : (1) $\frac{1}{2}$ (2) $\frac{1}{4}$ (3) 2 (4) 1 Solution: (1)



Let p = $\ln(1 + \tan^2 \sqrt{x})^{\frac{1}{2x}}$.

The limit is of the form $(1 + 0)^{\alpha} = e^{0.\alpha}$

 $e^{\frac{\tan\sqrt{x} \cdot \tan\sqrt{x}}{\sqrt{x}} \cdot \frac{1}{2}}$ $\lim_{x \to 0+} p = e^{\frac{1}{2}}$ $\log p = \log e^{\frac{1}{2}} = \frac{1}{2}$ $= \frac{1}{2}$

53. Let P be the point on the parabola, $y^2 = 8x$ which is at a minimum distance from the centre C of the circle, $x^2 + (y+6)^2 = 1$. Then the equation of the circle, passing through C and having its centre at P is:

- (1) $x^2 + y^2 \frac{x}{4} + 2y 24 = 0$
- (2) $x^2 + y^2 4x + 9y + 18 = 0$
- (3) $x^2 + y^2 4x + 8y + 12 = 0$

(4)
$$x^2 + y^2 - x + 4y - 12 = 0$$

Solution: (3)

 $y^2 = 8x$ is the equation of the given parabola. If P is a point at minimum distance from (0, -6) then it should be normal to the parabola at P.

Slope of tangent

- $\frac{2dy}{dx} \cdot y = 8$ $\frac{dy}{dx} = \frac{4}{y}.$
- \therefore Slope of normal = $\left(-\frac{y}{4}\right)$

Any point on the parabola would be $\left(\frac{y^2}{8}, y\right)$, and hence slope of the normal would be

$$\frac{(y+6)}{\frac{y^2}{8}} = -\frac{y}{4}$$





$$(y+6) = -\frac{y^3}{32}$$

At y = -4, LHS = RHS

$$(2) = +\frac{64}{32} = 2$$

At
$$y = -4 x = 2$$

So point *P*(2, −4).

Radius of the desired circle would be $\sqrt{2^2 + 2^2} = 2\sqrt{2}$,

So equation of the circle would be $\sqrt{(x-2)^2 + (y+4)^2} = 2\sqrt{2}$

 $x^2 - 4x + 4 + y^2 + 8y + 16 = 8$

 $x^2 + y^2 - 4x + 8y + 12 = 0$

54. If a curve y = f(x) passes through the point (1, -1) and satisfies the differential equation, y(1 + xy)dx = x dy, then $f\left(-\frac{1}{2}\right)$ is equal to :

(1) $\frac{2}{5}$ (2) $\frac{4}{5}$ (3) $-\frac{2}{5}$ (4) $-\frac{4}{5}$

Solution: (2)

Given differential equation

$$ydx + xy^{2}dx = xdy$$

$$\Rightarrow \quad \frac{xdy - ydx}{y^{2}} = xdx$$

$$\Rightarrow \qquad -d\left(\frac{x}{y}\right) = d\left(\frac{x^2}{2}\right)$$

Integrating we get

$$=\frac{x}{y}=\frac{x^2}{2}+C$$

- \therefore It is passes through (1, -1)
- $\therefore \qquad 1 = \frac{1}{2} + C \implies C = \frac{1}{2}$

$$\therefore \qquad x^2 + 1 + \frac{2x}{y} = 0 \quad \Rightarrow \quad y = \frac{-2x}{x^2 + 1}$$



$$\therefore \qquad f\left(-\frac{1}{2}\right) = \frac{4}{5}$$

55. Let \vec{a}, \vec{b} and \vec{c} be three unit vectors such that $\vec{a} \times (\vec{b} \times \vec{c}) = \frac{\sqrt{3}}{2}(\vec{b} + \vec{c})$. If \vec{b} is not parallel to \vec{c} , then the angle between \vec{a} and \vec{b} is :

(1)
$$\frac{2\pi}{3}$$
 (2) $\frac{5\pi}{6}$ (3) $\frac{3\pi}{4}$ (4) $\frac{\pi}{2}$

Solution: (2)

$$\vec{a} \times (\vec{b} \times \vec{c}) = \frac{\sqrt{3}}{2} (\vec{b} + \vec{c})$$

$$(\vec{a} \cdot \vec{c}) \vec{b} - (\vec{a} \cdot \vec{b}) \vec{c} = \frac{\sqrt{3}}{2} \vec{b} + \frac{\sqrt{3}}{2} \vec{c}$$

On comparing the coefficient of \vec{c} On both the sides.

$$\vec{a} \cdot \vec{b} = -\frac{\sqrt{3}}{2}$$
$$|\vec{a}| \cdot |\vec{b}| \cos \theta = -\frac{\sqrt{3}}{2}$$
$$\cos \theta = -\frac{\sqrt{3}}{2}$$
$$5\pi$$

$$\theta = \frac{5\pi}{6}$$

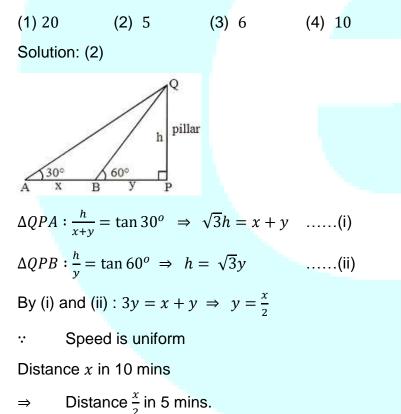
56. If $A = \begin{bmatrix} 5a & -b \\ 3 & 2 \end{bmatrix}$ and A adj $A = A A^{T}$, then 5a + b is equal to : (1) 4 (2) 13 (3) -1 (4) 5 Solution: (4) $A = \begin{bmatrix} 5a & -b \\ 3 & 2 \end{bmatrix}$ and $A^{T} = \begin{bmatrix} 5a & 3 \\ -b & 2 \end{bmatrix}$

 $AA^{T} = \begin{bmatrix} 25a^{2} + b^{2} & 15a - 2b \\ 15a - 2b & 13 \end{bmatrix}$



Now, A adj $A = |A|I_2 = \begin{bmatrix} 10a + 3b & 0\\ 0 & 10a + 3b \end{bmatrix}$ Given $AA^T = A adj A$ 15a - 2b = 0(i) 10a + 3b = 13(ii) Solving we get 5a = 2 and b = 3 $\therefore \qquad 5a + b = 5$

57. A man is walking towards a vertical pillar in a straight path, at a uniform speed. At a certain point A on the path, he observes that the angle of elevation of the top of the pillar is 30° . After walking for 10 minutes from A in the same direction, at a point B, he observes that the angle of elevation of the top of the pillar is 60° . Then the time taken (in minutes) by him, from B to reach the pillar, is :



58. The distance of the point (1, -5, 9) from the plane x - y + z = 5 measured along the line x = y = z is :





(1)
$$\frac{10}{\sqrt{3}}$$
 (2) $\frac{20}{3}$ (3) $3\sqrt{10}$ (4) $10\sqrt{3}$

Solution: (4)

Equation of line parallel to x = y = z through

$$(1, -5, 9)$$
 is $\frac{x-1}{1} = \frac{y+5}{1} = \frac{z-9}{1} = \lambda$

If $P(\lambda + 1, \lambda - 5, \lambda + 9)$ be point of intersection of line and plane.

$$\Rightarrow \quad \lambda + 1 - \lambda + 5 + \lambda + 9 = 5$$

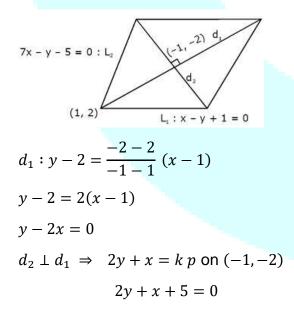
$$\Rightarrow \lambda = -10$$

- \Rightarrow Coordinates point are (-9, -15, -1)
- \Rightarrow Required distance = $10\sqrt{3}$

59. Two sides of a rhombus are along the lines, x - y + 1 = 0 and 7x - y - 5 = 0. If its diagonals intersect at (-1, -2), then which one of the following is a vertex of this rhombus ?

(1) $\left(\frac{1}{3}, -\frac{8}{3}\right)$ (2) $\left(-\frac{10}{3}, -\frac{7}{3}\right)$ (3) (-3, -9) (4) (-3, -8)

Solution: (1)





Non P.O.I. of d_2 and L_1 x - y + 1 = 0 x + 2y + 5 = 0 -3y - 4 = 0 $y = -\frac{4}{3}$ And P.O.I. of d_2 and L_2 x + 2y + 5 = 0 14x - 2y - 10 = 0And $y = -\frac{8}{3}$ 15x - 5 = 0 $\Rightarrow \qquad x = \frac{1}{3}$

60. If $0 \le x < 2\pi$, then the number of real values of x, which satisfy the equation $\cos x + \cos 2x + \cos 3x + \cos 4x = 0$, is :

(1) 7 (2) 9 (3) 3 (4) 5 Solution: (1) $2\cos 2x\cos x + 2\cos 3x\cos x = 0$ $\Rightarrow 2\cos x(\cos 2x + \cos 3x) = 0$ $2\cos x 2\cos \frac{5x}{2}\cos \frac{x}{2} = 0$ $x = \frac{\pi}{2}, \frac{3\pi}{2}, \pi, \frac{\pi}{5}, \frac{3\pi}{5}, \frac{7\pi}{5}, \frac{9\pi}{5}$ 7 Solutions.

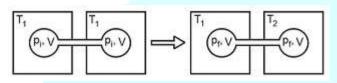






CHEMISTRY

61. Two closed bulbs of equal volume (V) containing an ideal gas initially at pressure p_i and temperature T_1 are connected through a narrow tube of negligible volume as shown in the figure below. The temperature of one of the bulbs is then raised to T_2 . The final pressure P_f is:



(1) $2p_i\left(\frac{T_2}{T_1+T_2}\right)$

$$(2) \qquad 2p_i \left(\frac{T_1 T_2}{T_1 + T_2}\right)$$

(3)
$$p_i\left(\frac{T_1T_2}{T_1+T_2}\right)$$

$$(4) \qquad 2p_i\left(\frac{T_1}{T_1+T_2}\right)$$

Solution: (1)

Given two closed bulbs of equal volume (v) containing ideal gas initially of pressure p_i and temperature T_1 which are connected by narrow tube of negligible volume.

To find final pressure P_f when one raised to T_2

No. of moles of gas doesn't change

$$(n_T)_i = (n_T)_f$$

 $\frac{P_i V}{RT_1} + \frac{P_i V}{RT_1} = \frac{P_f V}{RT_1} + \frac{P_f V}{RT_2}$

$$2\frac{P_1}{T_1} = \frac{P_f}{T_1} + \frac{P_f}{T_2}$$

- 62. Which one of the following statements about water is FALSE?
- (1) There is extensive intramolecular hydrogen boding in the condensed phase.
- (2) Ice formed by heavy water sinks in normal water.
- (3) Water is oxidized to oxygen during photosynthesis
- (4) Water can act both as an acid and as a base



Solution: (1)

- (i) There is extensive intermolecular hydrogen bonding in the condensed phase instead of intramolecular H bonding.
- (ii) Ice formed by heavy water sinks in normal water due to higher density of D_2O than normal water.
- (iii)

$$6CO_2 + 6H_2O \xrightarrow{hv} C_6H_{12}O_6 + 6O_2$$

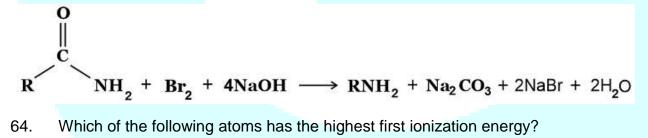
(iv) Water can show amphiprotic nature and hence water can act both as an acid a base.

63. In the Hofmann bromamide degradation reaction, the number of moles of NaOH and Br_2 used per mole of amine produced are:

- (1) Two moles of NaOH and two moles of Br₂
- (2) Four moles of NaOH and one mole of Br_2
- (3) One mole of NaOH and one mole of Br₂
- (4) Four moles of NaOH and two moles of Br_2

Solution: (2)

To find number of moles of NaOH and Br_2 used per mole of amine produced.



- (1) K
- (2) Sc
- (3) Rb
- (4) Na

Solution: (2)

Na is the smallest element in the IA group elements and it has highest IE among K, Rb



G

Sc has lowest effective nuclear charge

Effective nuclear charge $\times \frac{1}{1F}$

Sc has low effective nuclear charge than Na.

So it has I.E. among given elements.

65. The concentration of fluoride, lead, nitrate and iron in a water sample from an underground lake was found to be 1000 ppb, 40 ppb, 100 ppm and 0.2 ppm, respectively. This water is unsuitable for drinking due to high concentration of:

- (1) Nitrate
- (2) Iron
- (3) Fluoride
- (4) Lead

Solution: (1)

Concentration	of fluoride	= 1000 PPb
---------------	-------------	------------

	= 1 PPm
Concentration of lead	= 40 PPb
	= 0.04 PPm
Concentration of nitrate	= 100 PPm
Concentration of iron	= 0.2 PPm

High concentration of nitrate

66. The heats of combustion of carbon and carbon monoxide are -393.5 and -283.5 kJ mol⁻¹, respectively. The heat of formation (in kJ) of carbon monoxide per mole is:

- (1) 676.5
- (2) -110.5
- (3) 110.5
- (4) 676.5

Solution: (2)

Given heat of combustion of carbon and carbon monoxide are -393.5 and - 283.5 kJ mol⁻¹, respectively

(i) $C + O_2 \rightarrow CO_2$ $\Delta H_1 = -393.5 \text{ kJ mol}^{-1}$





(ii) $CO + \frac{1}{2}O_2 \rightarrow CO_2 \quad \Delta H_2 = -283.5 \text{ kJ mol}^{-1}$

To find heat of formation of CO per mole.

i.e. $C + \frac{1}{2}O_2 \rightarrow CO$ (ii) × (2) $2CO + O_2 \rightarrow 2CO_2 \quad \Delta H_3 = -283.5 \times 2 \text{ kJ mol}^{-1}$ $2CO_2 \rightarrow 2CO + O_2 \quad \Delta H_4 = 567 \text{ kJ mol}^{-1}$ (i) × (2) $2C + 2O_2 \rightarrow 2CO_2 \quad \Delta H_5 = -393.5 \times 2 \text{ kJ mol}^{-1}$ $= -787 \text{ kJ mol}^{-1}$ $2C + O_2 \rightarrow 2CO \quad \Delta H_6 = -220 \text{ kJ mol}^{-1}$ For one mole of CO,

$$\Delta H = \frac{-220}{2} = -110 \text{ kJ mol}^{-1}$$

67. The equilibrium constant at 298 K for a reaction $A + B \rightleftharpoons C + D$ is 100, If the initial concentration of all the four species were 1 M each, then equilibrium concentration of D (in mol L⁻¹) will be:

- (1) 1.818
- (2) 1.182
- (3) 0.182
- (4) 0.818

Solution: (1)

K at 298 K for the reaction

 $A + B \rightleftharpoons C + D$ is 100

Given initial concentration of all four species is 1 M.

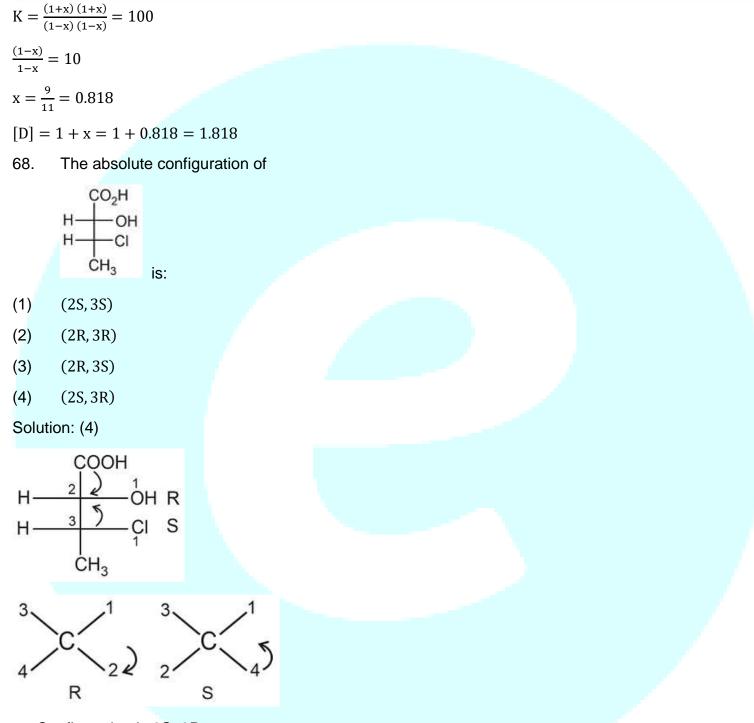
At t = 0,

 $\therefore \quad \frac{A}{1} + \frac{B}{1} \rightleftharpoons \frac{C}{1} + \frac{D}{1}$

At equilibrium,

 $\begin{array}{c} A+B\\ 1-x \quad 1-x \end{array} \rightleftharpoons \begin{array}{c} C+D\\ 1+x \quad 1+x \end{array}$





∴ Configuration is 2S, 3R.

69. For a linear plot of log $\left(\frac{x}{m}\right)$ versus log p in a Freundlich adsorption isotherm, which of the following statements is correct? (k and n are constants)

(1) Only $\frac{1}{n}$ appears as the slope





- (2) $\log\left(\frac{1}{n}\right)$ appears as the intercept
- (3) Both k and $\frac{1}{n}$ appear in the slope term
- (4) $\frac{1}{n}$ appears as the intercept

Solution: (1)

According to Freundlich isotherm

$$\frac{x}{m} = k. p^{\frac{1}{n}}$$

 $\log \frac{x}{m} = \log k + \frac{1}{n} \log P$

So intercept is log k and slope is $\frac{1}{n}$

- 70. The distillation technique most suited for separating glycerol from spent lye in the soap industry is:
- (1) Steam distillation
- (2) Distillation under reduced pressure
- (3) Simple distillation
- (4) Fractional distillation

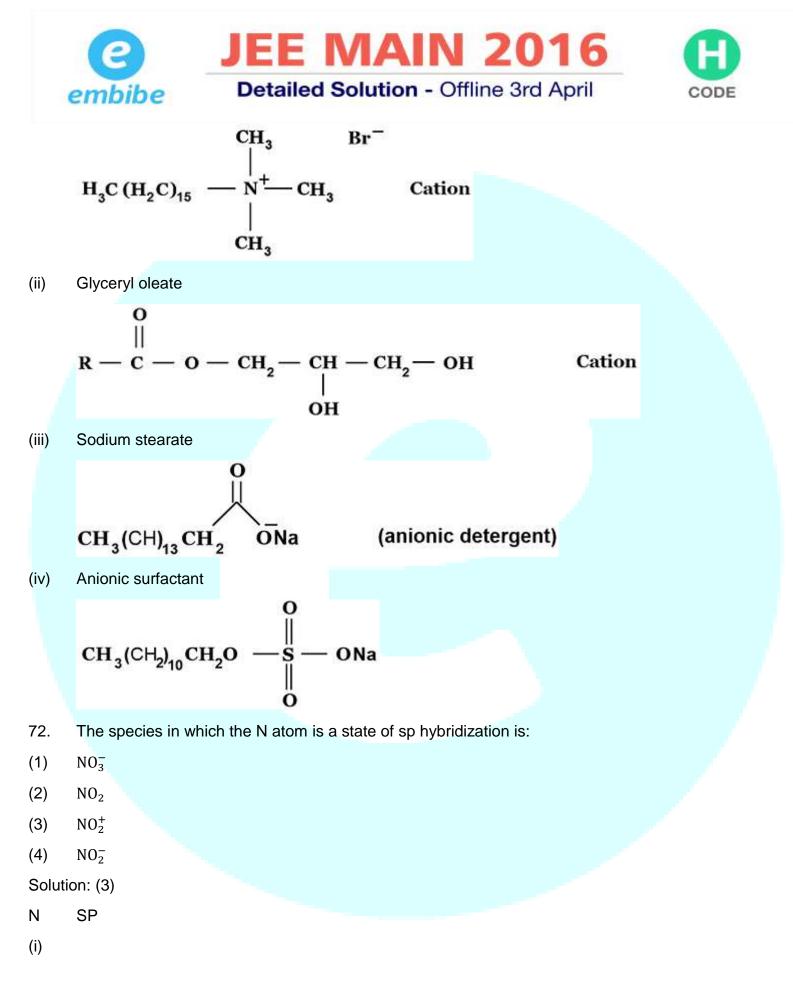
Solution: (2)

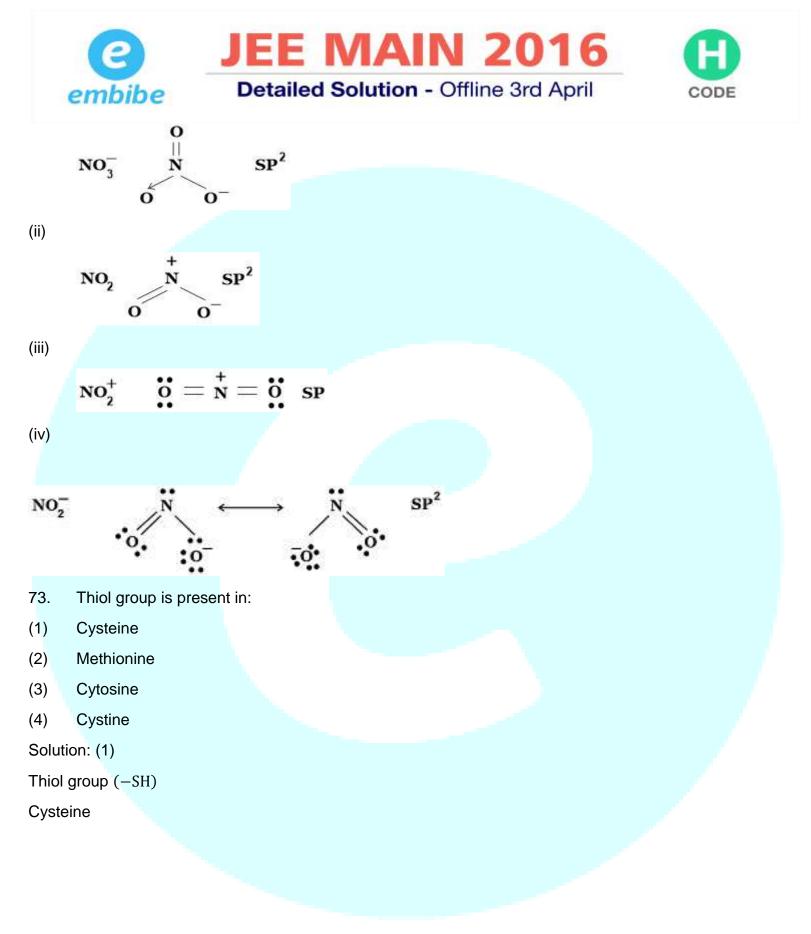
Glycerol (B.P. 290°C) is separated from spent – lye in the soap industry by distillation under reduced pressure, as for simple distillation very high temperature is required which might decompose the component.

- 71. Which of the following is an anionic detergent?
- (1) Cetyltrimethyl ammonium bromide
- (2) Glyceryl oleate
- (3) Sodium stearate
- (4) Sodium lauryl sulphate

Solution: (4)

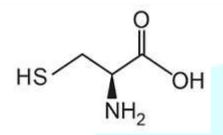
(i) Cetyltrimethyl ammonium bromide











- 74. Which one of the following ores is best concentrated by froth floatation method?
- (1) Galena
- (2) Malachite
- (3) Magnetite
- (4) Siderite

Solution: (1)

Froth floatation method is used for concentration of sulphide ores.

- Galena \rightarrow Pbs Ţ
- Which of the following statements about low density polythene is FALSE? 75.
- (1) Its synthesis required dioxygen or a peroxide initiator as a catalyst
- (2)It is used in the manufacture of buckets, dust - bins etc.
- (3)Its synthesis requires high pressure
- (4) It is a poor conductor of electricity

Solution: (2)

Low density polythene: It is obtained by the polymerization of ethene high pressure of 1000-2000 atm. at a temp. of 350 K to 570 K in the pressure of traces of dioxygen or a peroxide initiator.

Low density polythene is chemically inert and poor conductor of electricity. It is used for manufacture squeeze bottles. Toys and flexible pipes.

- Which of the following compounds is metallic and ferromagnetic? 76.
- (1) VO_2
- (2) MnO_2
- (3) TiO_2
- (4) CrO_2



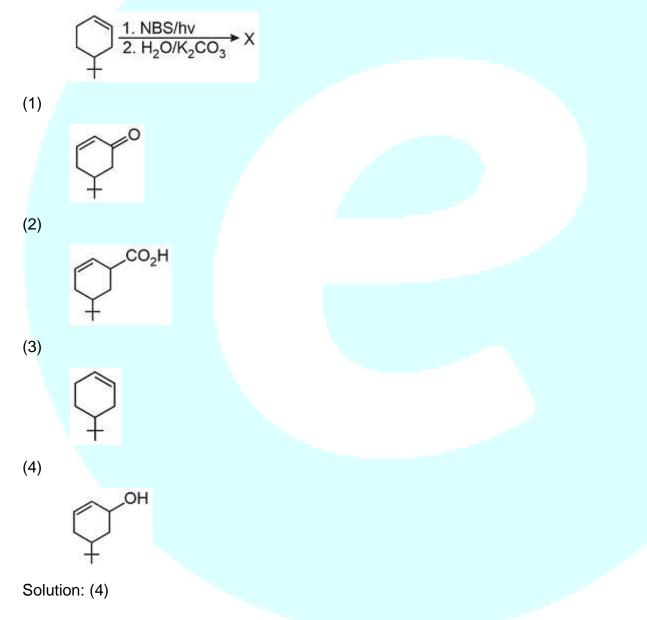
Solution: (4)

d - block elements are metals.

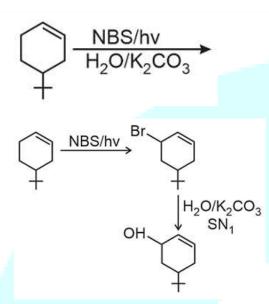
MnO₂ and CrO₂ exhibit strong attraction to magnetic fields and are able to retain their magnetic properties.

MnO₂ is antiferromagnetic and CrO₂ is ferromagnetic.

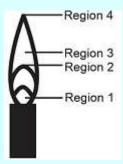
77. The product of the reaction give below is:





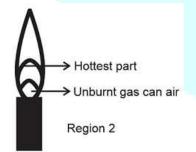


78. The hottest region of Bunsen flame shown in the figure below is:



- (1) Region 3
- (2) Region 4
- (3) Region 1
- (4) Region 2

Solution: (4)





79. At 300 K and 1 atm, 15mL of a gaseous hydrocarbon requires 375 mL air containing 20% O_2 by volume for complete combustion. After combustion the gases occupy 330 mL. Assuming that the water formed is in liquid form and the volumes were measured at the same temperature and pressure, the formula of the hydrocarbon is:

(1)
$$C_4 H_8$$

- (2) $C_4 H_{10}$
- (3) $C_3 H_6$
- (4) $C_3 H_8$

Solution: (Bonus or 4)

Volume of N_2 in air = $375 \times 0.8 = 300 \ ml$

Volume of O_2 in air = $375 \times 0.2 = 75 \ ml$

$$C_{x}H_{y} + \left(x + \frac{y}{4}\right)O_{2} \rightarrow xCO_{2}(g) + \frac{y}{2}H_{2}O(\ell)$$

$$15ml \qquad 15\left(x + \frac{y}{4}\right) \qquad 15x \qquad -$$

After combustion total volume

$$330 = V_{N_2} + V_{CO_2}$$

$$330 = 300 + 15x$$

Volume of O_2 used

$$15\left(x+\frac{y}{4}\right) = 5$$
$$x+\frac{y}{4} = 5$$

So hydrocarbon is $= C_2 H_{12}$

None of the option matches it therefore it is a BONUS.

Alternatively







$$C_{x}H_{y} + \left(x + \frac{y}{4}\right)O_{2} \rightarrow xCO_{2}(g) + \frac{y}{2}H_{2}O(\ell)$$

$$15ml \qquad 15\left(x + \frac{y}{4}\right) \qquad 15x \qquad -$$

$$0 \qquad 0 \qquad 0$$

Volume of O_2 used

$$15\left(x+\frac{y}{4}\right) = 75$$
$$x+\frac{y}{4} = 5$$

If further information (i.e., 330 ml) is neglected, option (C_3H_8) only satisfy the above equation.

- 80. The pair in which phosphorous atoms have a formal oxidation state of + 3 is:
- (1) Orthophosphorous and hypophospheric acids
- (2) Pyrophosphorous and pyrophosphoric acids
- (3) Orthophosphorous and pyrophosphorous acids
- (4) Pyrophosphorous and hypophosphoric acids

Solution: (3)

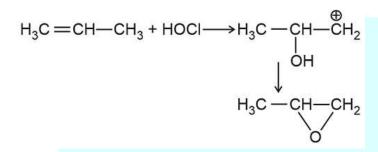
Acid	Formula	Formal oxidation state of phosphorous
Pyrophosphorous acid	$H_4P_2O_5$	+3
Pyrophosphoric acid	$H_4P_2O_7$	+5
Orthophosphorous acid	H ₃ PO ₃	+3
Hypophosphoric acid	$H_4P_2O_6$	+4

Both pyrophosphorous and orthophosphorous acid have +3 formal oxidation state

- 81. The reaction of propene with HOCI ($Cl_2 + H_20$) proceeds through the intermediate:
- (1) $CH_3 CH(OH) CH_2^+$
- $(2) \qquad CH_3 CHCl CH_2^+$
- (3) $CH_3 CH^+ CH_2 OH$
- $(4) \qquad CH_3 CH^+ CH_2 CI$



Solution: (4)



82. 2 - chloro - 2 - methylpentane on reaction with sodium methoxide in methanol yields:

(i)

(ii)

(iii)

- (1) iii only
- (2) i and ii
- (3) All of these
- (4) i and iii

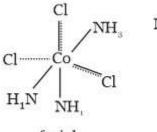
Solution: (3)

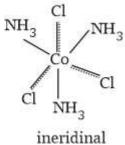


$$\begin{array}{c} \text{Cl} & & \text{H}_{3}\text{C}-\text{C}-\text{CH}_{2}-\text{CH}_{2}-\text{CH}_{3} \xrightarrow{\text{NaOCH}_{3}} \text{H}_{3}\text{C}=\text{C}-\text{CH}_{2}-\text{CH}_{2}-\text{CH}_{3}+\text{NaCI}+\text{CH}_{3}\text{OH} \\ & & \text{CH}_{3} \\ & & \text{CH}_{3} \\ & & \text{(Major)} \end{array}$$

$$\begin{array}{c} \text{H}_{3}\text{C}-\text{C}=\text{CH}_{2}-\text{CH}_{2}-\text{CH}_{3}+\text{NaCI}+\text{CH}_{3}\text{OH} \\ & & \text{C}\text{H}_{3} \\ & \text{(Minor)} \end{array}$$

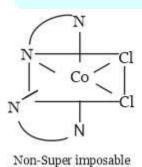
- 83. Which one of the following complexes shows optical isomerism?
- (1) trans $[Co(en)_2 Cl_2] Cl$
- (2) $[Co(NH_3)_4 Cl_2] Cl$
- (3) $[Co (NH_3)_3 Cl_3]$
- (4) cis $[Co(en)_2 Cl_2]Cl$
- (en = ethylenediamine)
- Solution: (4)
- Geometrical isomers,

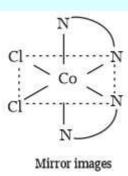




facial

cis [Co(en)₂Cl₂]Cl



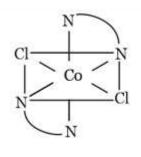


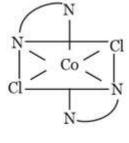
trans $[Co(en)_2Cl_2]Cl$

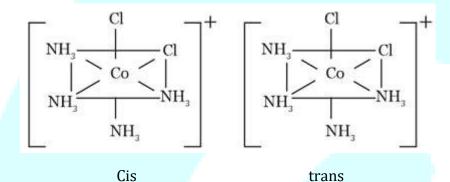












- 84. The main oxides formed on combustion of Li, Na and K in excess of air are, respectively:
- (1) Li_2O_2 , Na_2O_2 and KO_2

(2)
$$Li_2O$$
, Na_2O_2 and KO_2

- (3) Li_2O , Na_2O and KO_2
- (4) LiO_2 , Na_2O_2 and K_2O

Solution: (2)

In 1A group

Li on $r \times n$ with excess air

 $4\text{Li} + 0_2 \rightarrow 2\text{Li}_20$

Na on $r \times n$ with excess air

 $2Na + O_2 \rightarrow Na_2O_2$

K on $r \times n$ with excess air

 $K + O_2 \rightarrow KO_2$

85. 18 g glucose $(C_6H_{12}O_6)$ is added to 178.2 g water. The vapor pressure of water (in torr) for this aqueous solution is:

(1) 752.4



- (2) 759.0
- (3) 7.6
- (4) 76.0

Solution: (1)

 $\frac{\Delta P}{p_0}$ = mol. Fraction of glucose

$$\frac{\frac{760 - P_{\text{Soln}}}{760}}{760} = \frac{\frac{W_1}{Mwt_1}}{\frac{W_1}{M.wt_1} + \frac{W_2}{M.wt_2}} = \frac{\frac{18}{180}}{\frac{18}{180} + \frac{178.2}{18}} = \frac{0.1}{0.1 + 9.9} = \frac{1}{100}$$

$$760 - P_{Soln} = \frac{760}{100}$$

 $P_{Sol} = 752.4$

86. The reaction of zinc with dilute and concentrated nitric acid, respectively, produces:

- (1) NO and N_2O
- (2) NO_2 and N_2O
- (3) N_2O and NO_2
- (4) NO_2 and NO

Solution: (3)

Zn on reaction with HNO₃

 $4\text{Zn} + 10\text{HNO}_3 \rightarrow 4\text{Zn}(\text{NO}_3)_2 + \text{N}_2\text{O} + 5\text{H}_2\text{O}$

 $\text{Zn} + 4\text{HNO}_{3(\text{con})} \rightarrow \text{Zn}(\text{NO}_3)_2 + 2\text{NO}_2 + 2\text{H}_2\text{O}$

87. Decomposition of H_2O_2 follows a first order reaction. In fifty minutes the concentration of H_2O_2 decreases from 0.5 to 0.125 M in one such decomposition. When the concentration of H_2O_2 reaches 0.05 M, the rate of formation of O_2 will be:

- (1) $2.66 \,\mathrm{L\,min^{-1}}$ at STP
- (2) $1.34 \times 10^{-2} \text{ mol min}^{-1}$
- (3) $6.93 \times 10^{-2} \text{ mol min}^{-1}$

(4)
$$6.93 \times 10^{-4} \text{ mol min}^{-1}$$

Solution: (4)

 $2\mathrm{H}_2\mathrm{O}_2 \rightarrow 2\mathrm{H}_2\mathrm{O} + \mathrm{O}_2$





 $[O_2] = \frac{[H_2O_2]}{2} = \frac{[H_2O]}{2}$

For, $t_{\frac{1}{2}}$, H_2O_2 decreases to 0.125M from 0.5M

So,
$$2 \times t_{\frac{1}{2}} = 50$$

$$t_{\frac{1}{2}} = 25$$

$$t_{\frac{1}{2}} = \frac{0.69314}{K}$$

$$K = \frac{0.69314}{25}$$

$$[0_2] = \frac{1}{2} \times \frac{0.69314}{25}$$

$$= 6.93 \times 10^{-4} \text{ mol min}^{-1}$$

88. The pair having the same magnetic moment is:

[At. No. : Cr = 24, Mn = 25, Fe = 26, Co = 27]

(1)
$$[Mn (H_2 0)_6]^{2+}$$
 and $[Cr (H_2 0)_6]^{2-}$

- (2) $[CoCl_4]^{2-}$ and $[Fe(H_2O)_6]^{2+}$
- (3) $[Cr(H_2O)_6]^{2+}$ and $[CoCl_4]^{2-}$

(4)
$$[Cr(H_2O)_6]^{2+}$$
 and $[Fe(H_2O)_6]^{2+}$

Solution: (4)

In option A: $[Mn(H_2O)_6]^{2+}(3d^5)$ with

WFL,
$$\int_{\Delta_0}^{11} = 5$$
-unpaired electrons

& $[Cr(H_2O)_6]^{2+}$, $Cr^{2+}(3d^4)$ with W.F.L.,

In option B: $[CoCl_4]^{2-}$, $Co^{2+}(3d^7)$ with W.F.L.,





$$\frac{1}{1} \frac{1}{1}$$

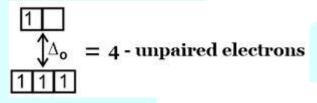
$$\int_{\text{td}}^{\Delta_{\text{td}}} = 3 \text{- unpaired electrons}$$

$$11 11$$

& $[Fe(H_2O)_6]^{2+}$, $Fe^{2+}(3d^6)$ with W.F.L.,

 $\begin{array}{c}
1 \\
1 \\
1
\end{array}$ $\begin{array}{c}
1 \\
1
\end{array}$

In option C: $[Cr(H_2O)_6]^{2+}$, $Cr^2 + (3d^4)$ with W.F.L.,



& $[CoCl_4]^{2-}$, Co^{2+} (3d⁷) with W.F.L.,

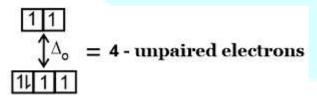
 $\begin{array}{c}
1 \\
1 \\
1 \\
1
\end{array}$ $\begin{array}{c}
\uparrow \triangle_{td} = 3 - unpaired electrons \\
\hline
1 \\
1 \\
1
\end{array}$

In option D: $[Cr(H_2O)_6]^{2+}$, $Cr^{2+}(3d^4)$ with W.F.L.,

$$1$$

$$1^{\Delta_0} = 4$$
- unpaired electrons
$$1111$$

& $[Fe(H_2O)_6]^{2+}$, $Fe^{2+}(3d^6)$ with W.F.L.,





G

Here both complexes have same unpaired electrons i.e. = 4

- 89. Galvanization is applying a coating of:
- (1) Cu
- (2) Zn
- (3) Pb
- (4) Cr

Solution: (2)

Galvanization is the process of applying zinc coating to steel (or) iron, to prevent rusting

90. A stream of electrons from a heat filament was passed between two charge plates kept at a potential difference V esu. If e and m are charge and mass of an electron, respectively, then the value of $\frac{h}{\lambda}$ (where λ is wavelength associated with electron wave) is given by:

- (1) $\sqrt{\text{meV}}$
- (2) $\sqrt{2 \text{ meV}}$
- (3) me V
- (4) 2 me V

Solution: (2)

Given stream of electron from heated filament was passed between two charge plates at potential difference V

e, m are charge and mass of electron

$$V = \frac{E}{e}$$
$$eV = \frac{1}{2} \times m \times V^{2}$$
$$\lambda = \frac{h}{mv}, V = \frac{h}{m\lambda}$$
$$eV = \frac{1}{2} \times m \times \left[\frac{h}{m\lambda}\right]^{2}$$
$$\frac{h}{\lambda} = \sqrt{2 \text{ meV}}$$